

# Conservative & accurate geometric transport methods for discontinuous variables in turbulent multi-physics two-phase flows

MODELING & COMPUTING COMPLEX FLOWS MINISYMPOSIUM  
SIAM – CSE 2015

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CORNELL UNIVERSITY



Cornell University  
Computational Thermo-Fluids  
Laboratory

## Some acknowledgments

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### Contributors

- Dr. Mark Owkes (now Assistant Professor in Mechanical Engineering at Montana State University)
- Dr. Jeremy McCaslin (now with ANSYS Fluent)
- Dr. Peter Brady (now at LANL).

### Funding sources

- NSF CBET 1034506
- NSF CAREER 1351545

### Computing resources

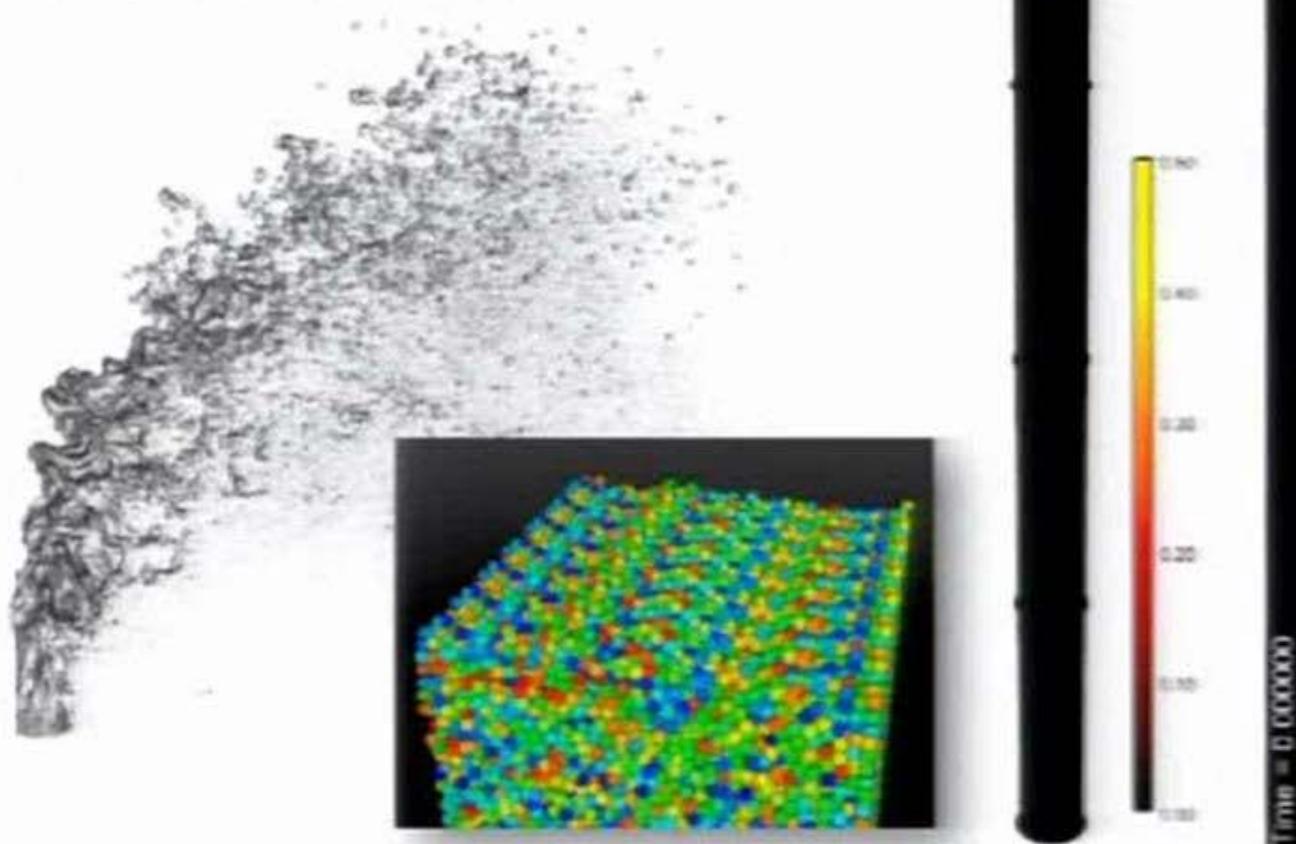
- LLNL – Sequoia & Sierra
- XSEDE – Kraken & Stampede
- ORNL – Titan
- ANL – Mira



## About us...

### Computational Thermo-Fluids Laboratory

- <http://ctflab.mae.cornell.edu>
- Focus on multiphase reacting turbulent flows
- Massively parallel computing

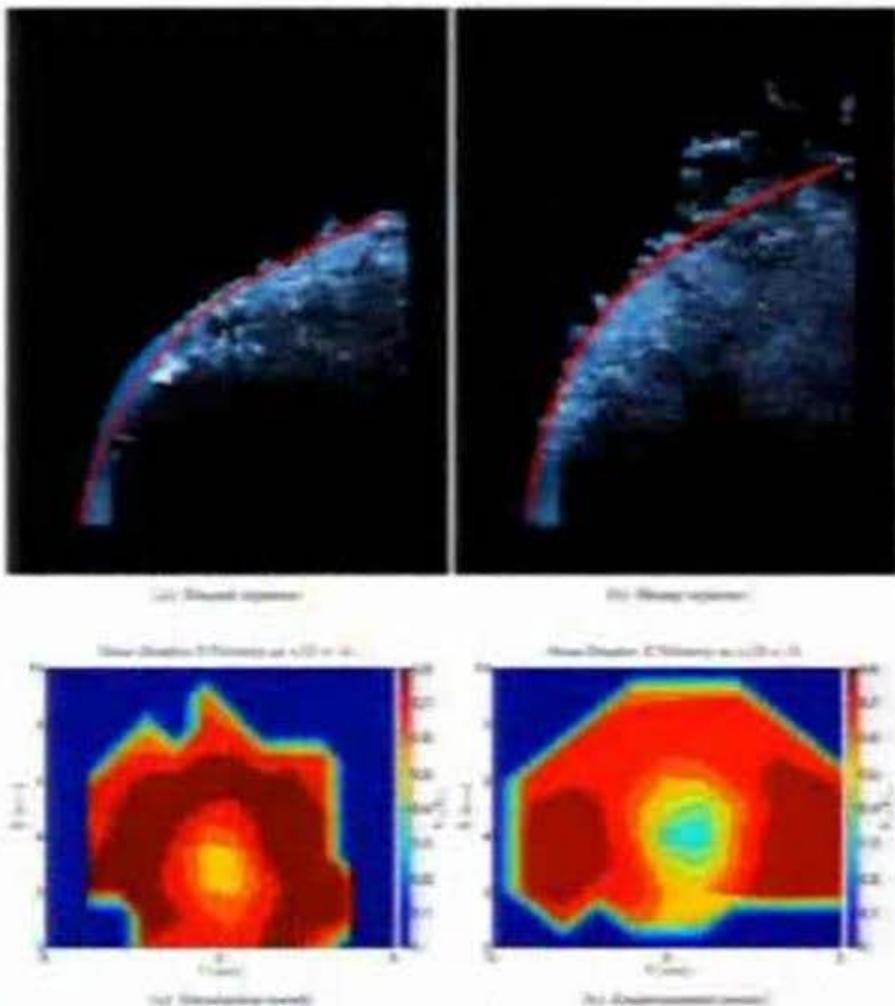




## About us...

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Mean droplet velocity at  $z/D = 15$



## Importance of liquid-gas turbulent flows





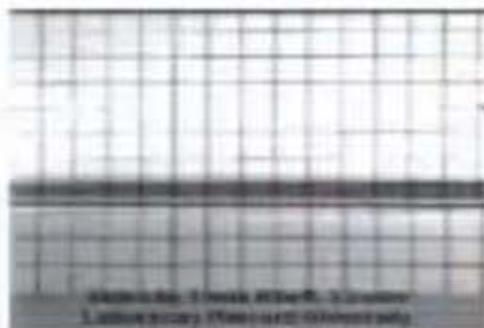
Many questions remain unanswered on liquid atomization

- What is the drop size distribution?
- Where do drops form?
- By what mechanisms?
- Can predictive models be developed?

## Some of the challenges associated with two-phase flows

### Liquid-gas flows are discontinuous

- Phase-interface is extremely thin and exhibits a singular surface tension force
- Fluid properties vary significantly across the interface



### Liquid-gas flows are strongly multi-scale

- From microscopic droplets to cm (even meters in many flows)
- Complex and frequent topology changes
- Turbulence



### Liquid-gas flows are often multi-physics

- Dirty interfaces, surfactants
- Non-isothermal, Marangoni flows, phase change, supercritical effects
- Electrostatic effects



As a consequence, liquid-gas flows are...

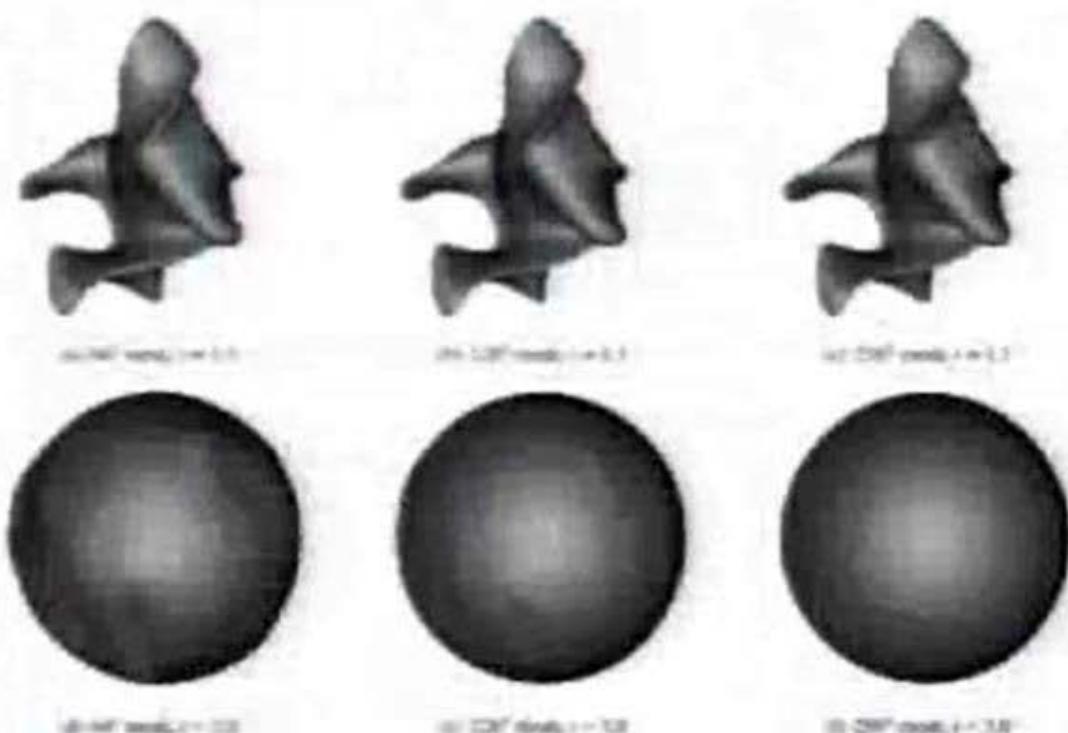
*... difficult to characterize experimentally*

*... difficult to simulate and model accurately*

## Verification exercise – Volume fraction transport

### Properties of the interface transport scheme

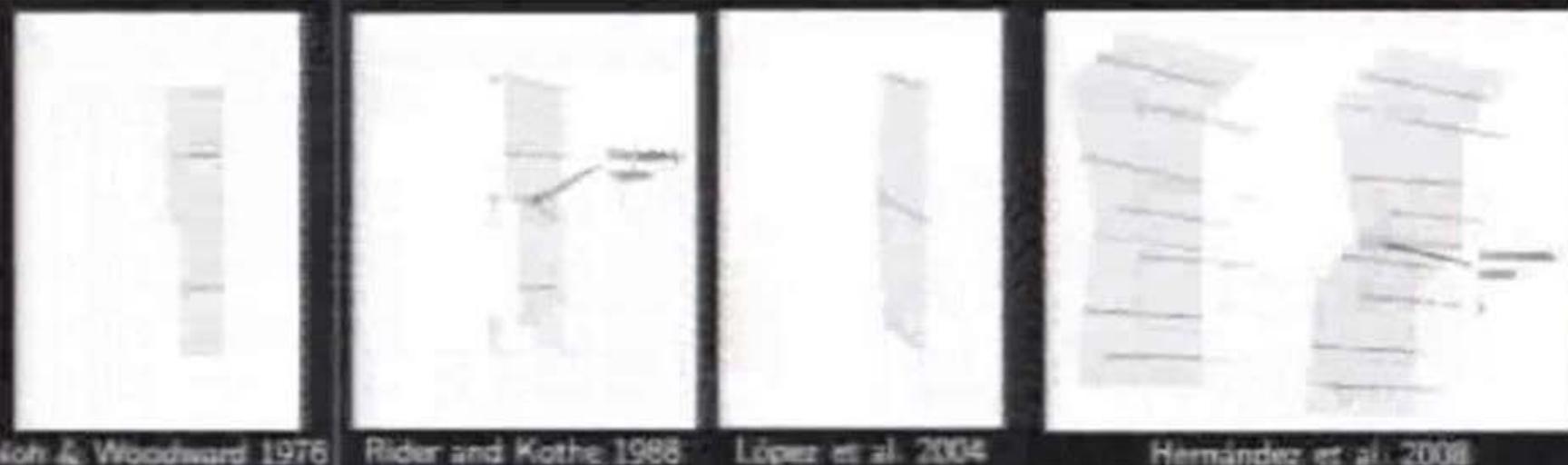
- Exactly conservative
- Exactly bounded
- Second order accurate



$N_x$	$E_{shape}$	$E_{mass}$	$E_{bound}$	Time/Timestep (s)
64	5.281e-01	5.472e-16	1.124e-17	1.61
128	9.357e-02	1.198e-15	1.198e-17	3.70
256	2.300e-02	1.290e-14	7.598e-17	12.0



## Geometric transport strategy

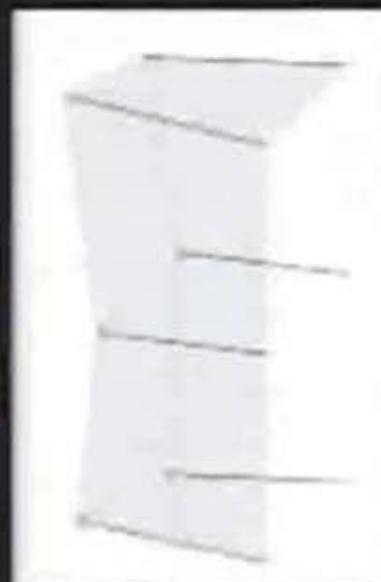


Noh & Woodward 1976

Rider and Kothe 1988

López et al. 2004

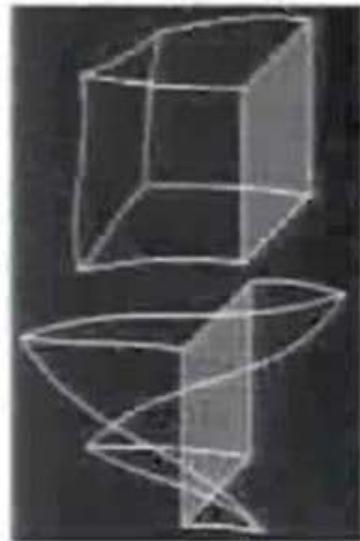
Hernández et al. 2008



- + Three-dimensional
- + Discretely conservative
- + Bounded
- Leads to many complex geometric operations

See also:

Le Chenevix & Pitsch 2013  
Ivey & Moin 2012  
Manci et al 2013  
Zhang 2013





## Simulation of turbulent EHD atomization

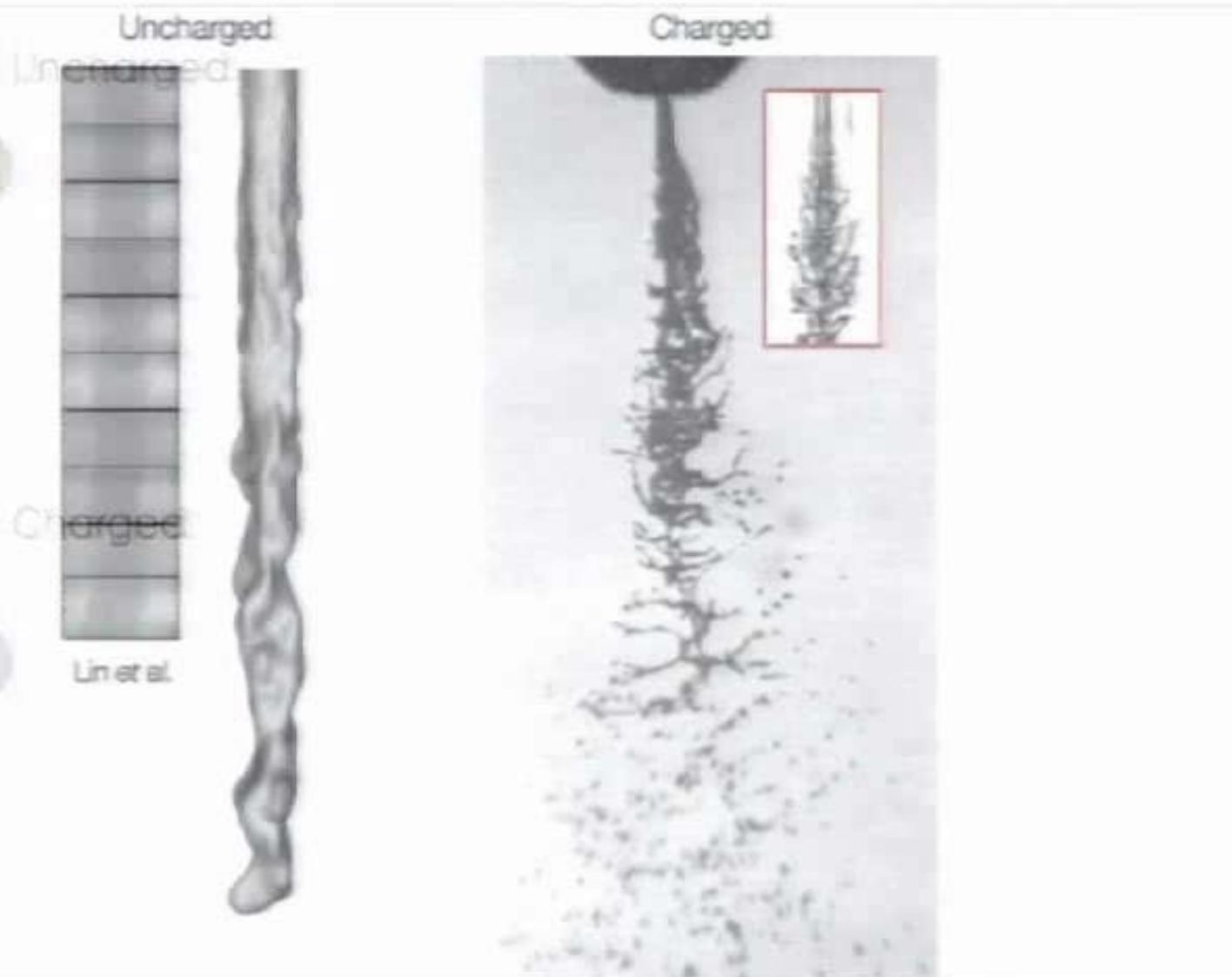
Uncharged



Charged



## Simulation of turbulent EHD atomization

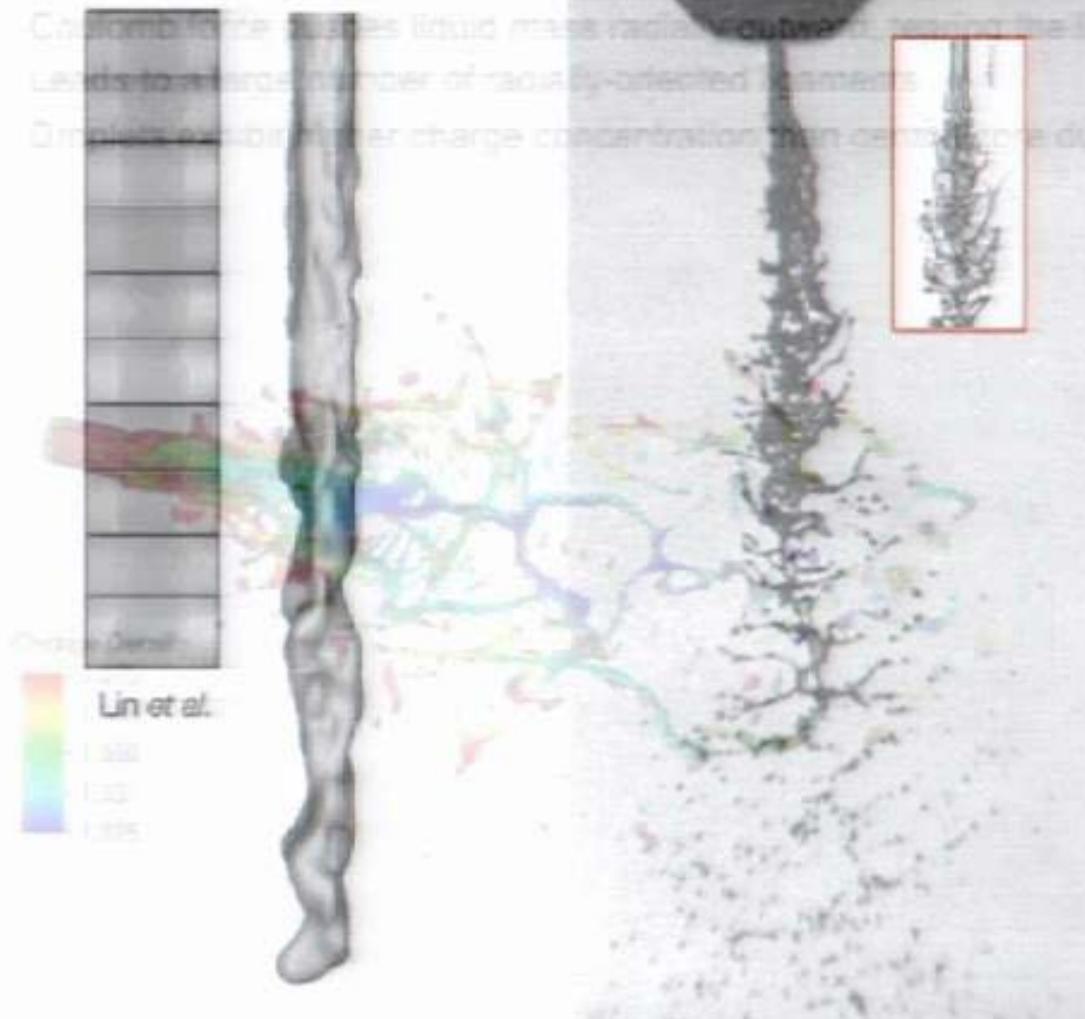




## Simulation of turbulent EHD atomization

3D simulation provides access to the internal distribution

- Charged droplets have more liquid mass retained outside the droplets due to electrostatic repulsion
- Less droplets per unit volume of nozzle-simulated moments
- Droplets contain higher charge concentration than neutrally charged due to charge drift





## Summary

- Discussed a novel **2nd order, fully conservative, consistent methodology** to transport discontinuous variables
- Accounts explicitly for flow discontinuities using
  - Planar interface representation
  - Simplex-based computational geometry toolbox
- Application to an emerging complex flow problem
  - Electrohydrodynamic atomization
- *Looking forward: focus on including phase change within the same framework*

