

From a network of ~~10,000~~ 20,000 neurons
to a smartphone app with ~~125,000~~ 160,000 users
linking scales in biological rhythms

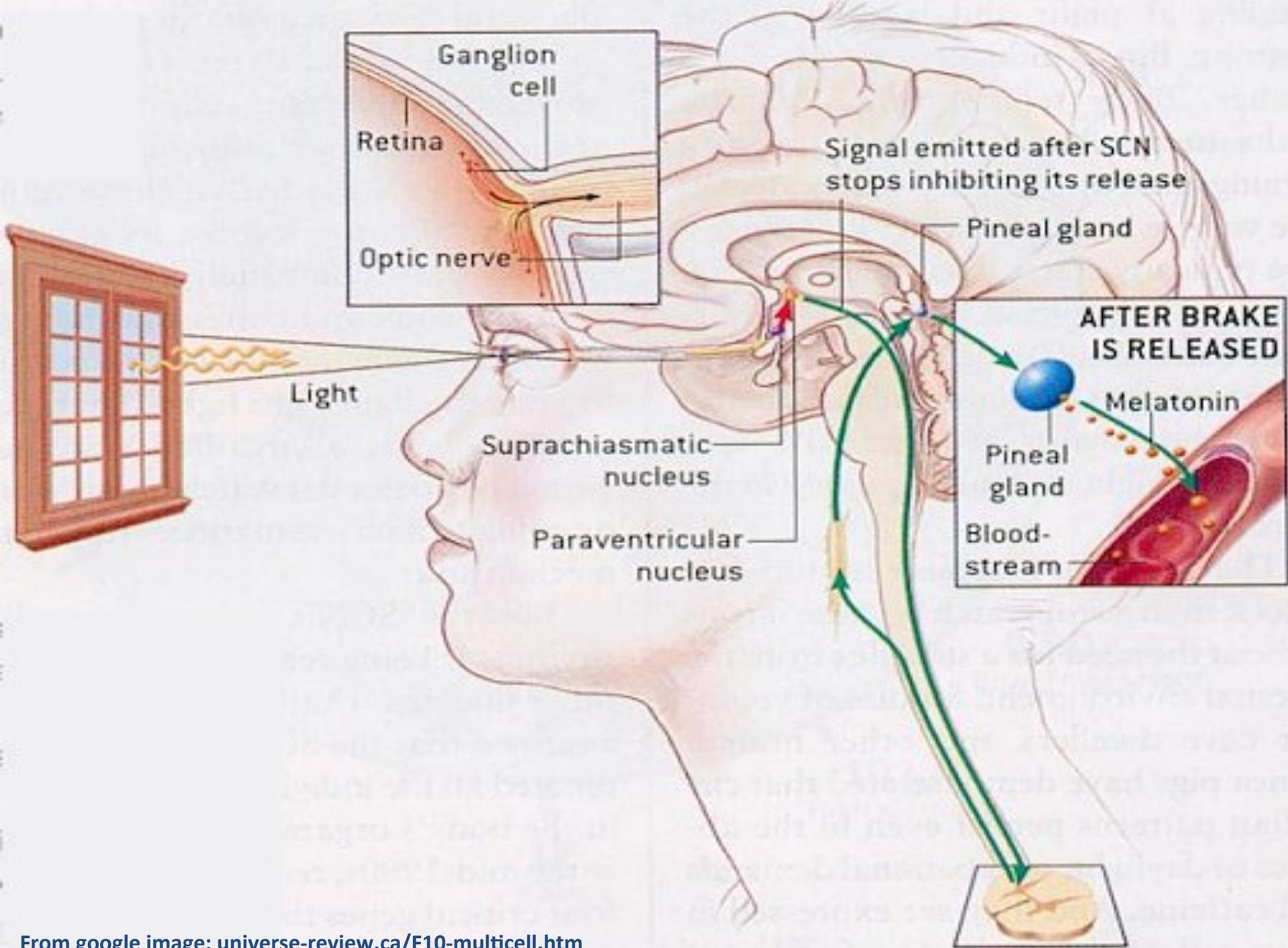


Daniel Forger

University of Michigan, Ann Arbor

Many thanks to Charles Peskin





New tools from modeling

Electrophysiology



+

Multiscale
Model

Molecular Biology



Human Behavior



Many scale of circadian research

Human Behavior



Society



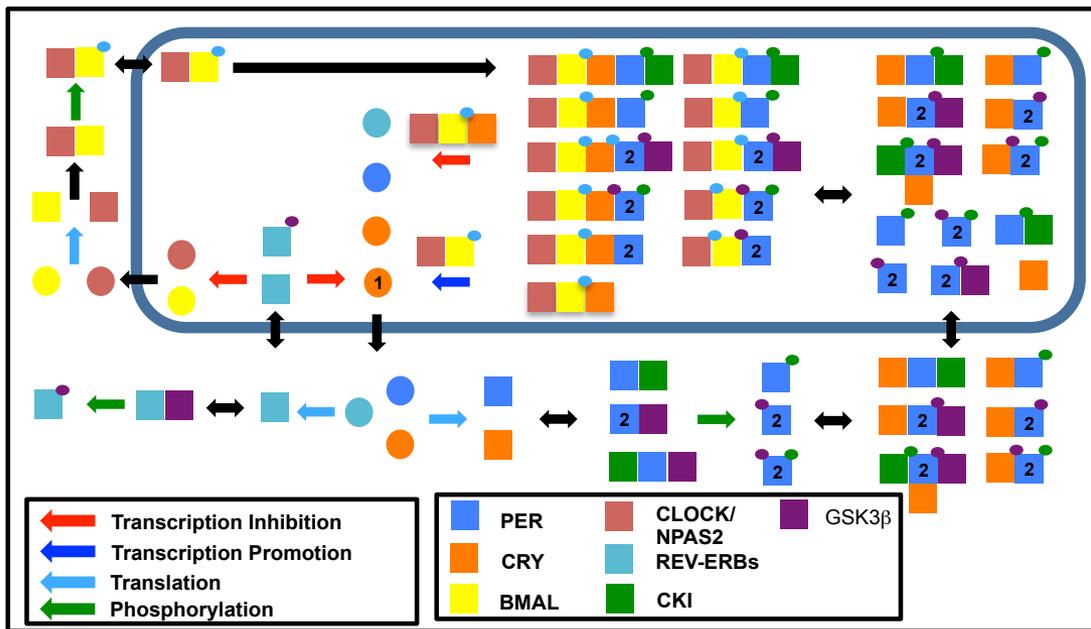
Entrain app

Build a detailed computational model of circadian timekeeping

- Biochemical model (~1000 chemical reactions)
 - Kim and Forger Molecular Systems Biology 2012
 - Min et al. Molecular Cell 2015
- Electrophysiological model (H-H type)
 - Belle et al. Science 2009
 - Diekman et al. PLoS Comp Bio 2013
- 1024 (or more) connected neurons
 - VIP (easy) GABA (hard)
- mSec timescale to weeks
(Billions of electrical signals)

DeWoskin et al. PNAS 2015

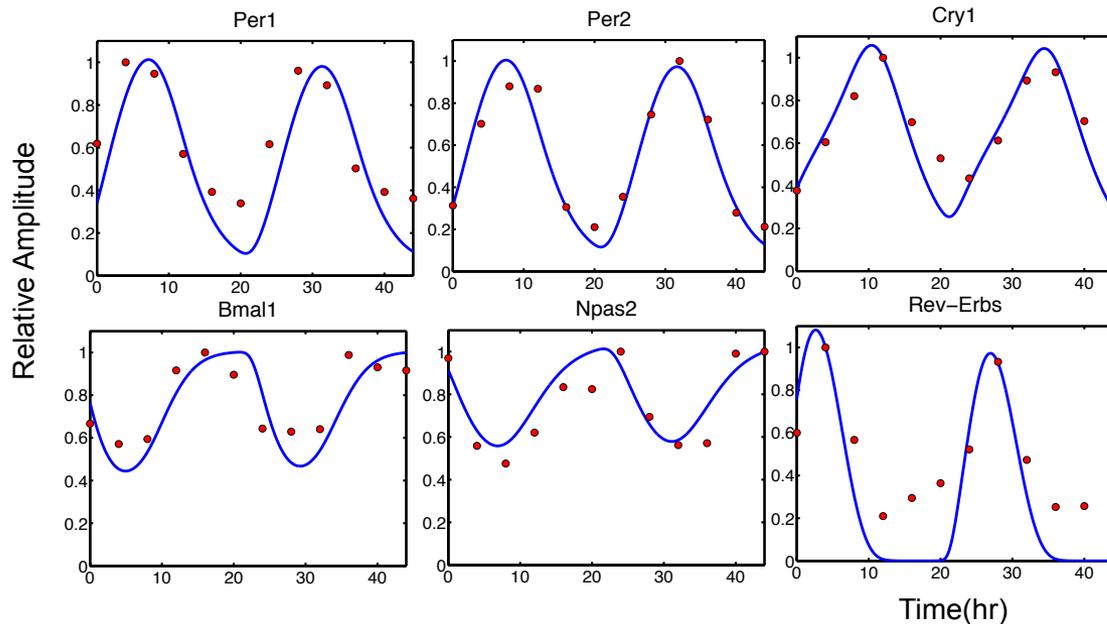
Myung et al. PNAS 2015



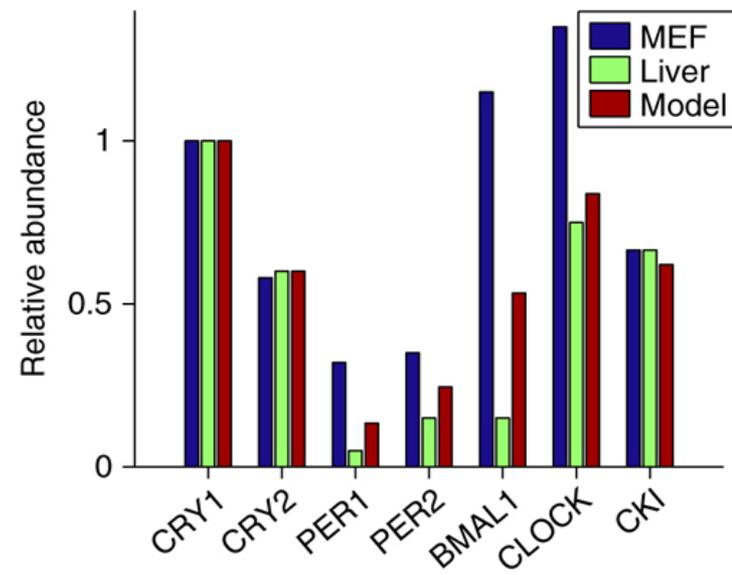
Variables	181
Kinetics	Mass-action
Measured Parameters	15
Estimated Parameters	60
Estimation	SSA
Computing	150 × 8Ghz

Forger & Peskin PNAS (2003)
 Kim & Forger, Mol Syst Biol (2012)
 Zhou et al. Molecular Cell (2015)

mRNA and Protein Timecourses

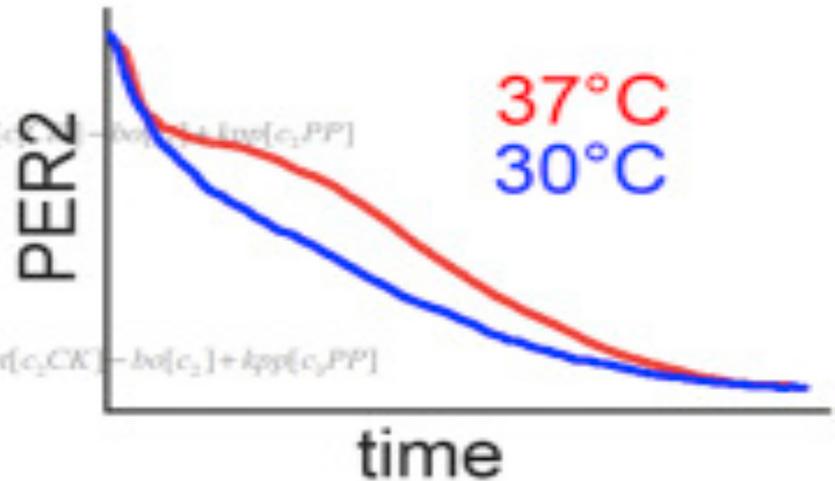
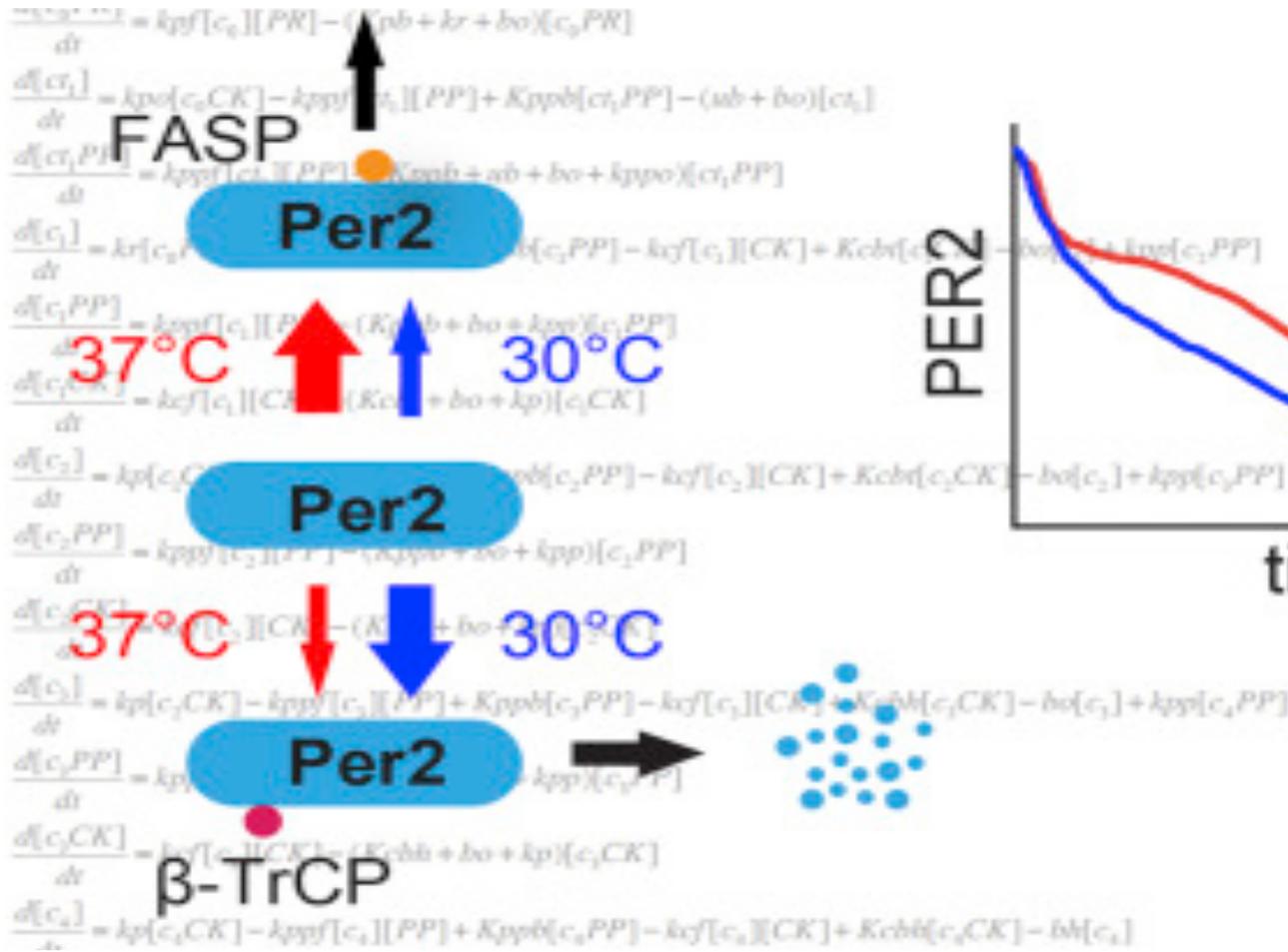


Abundance of Proteins



Phosphoswitch

With Jae Kim and Virshup lab
Zhou et al. Molecular Cell 2015



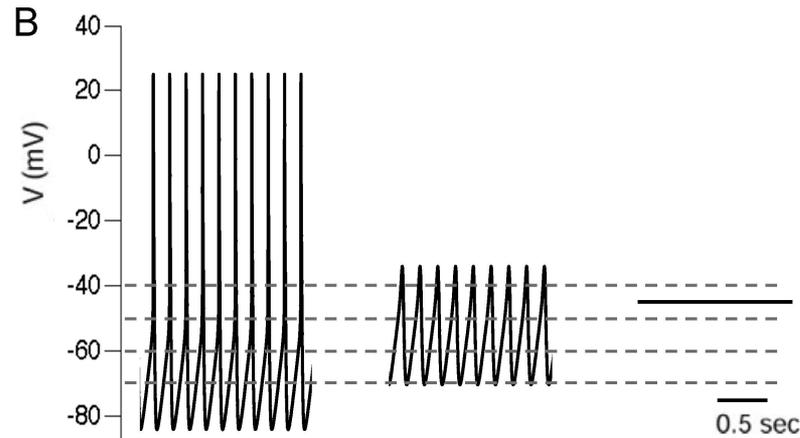
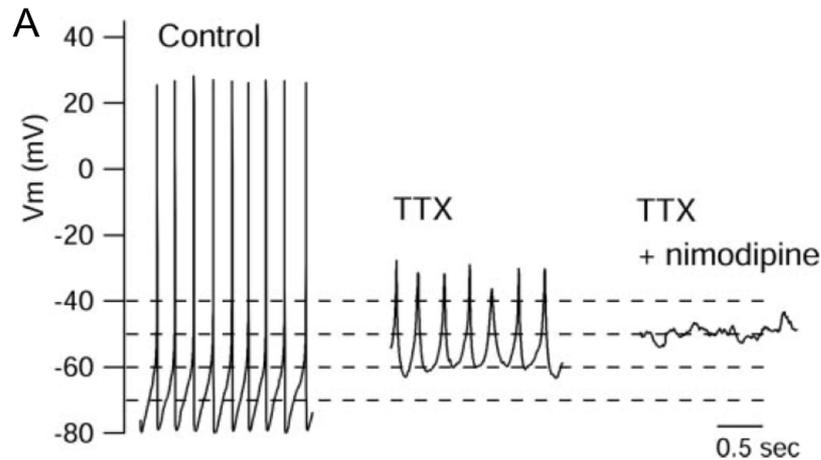
Key new challenges

- How to integrate data from protein structure in biochemical models?
- How to rapidly simulate large numbers of biochemical oscillators?



Two modes of activity of SCN neurons

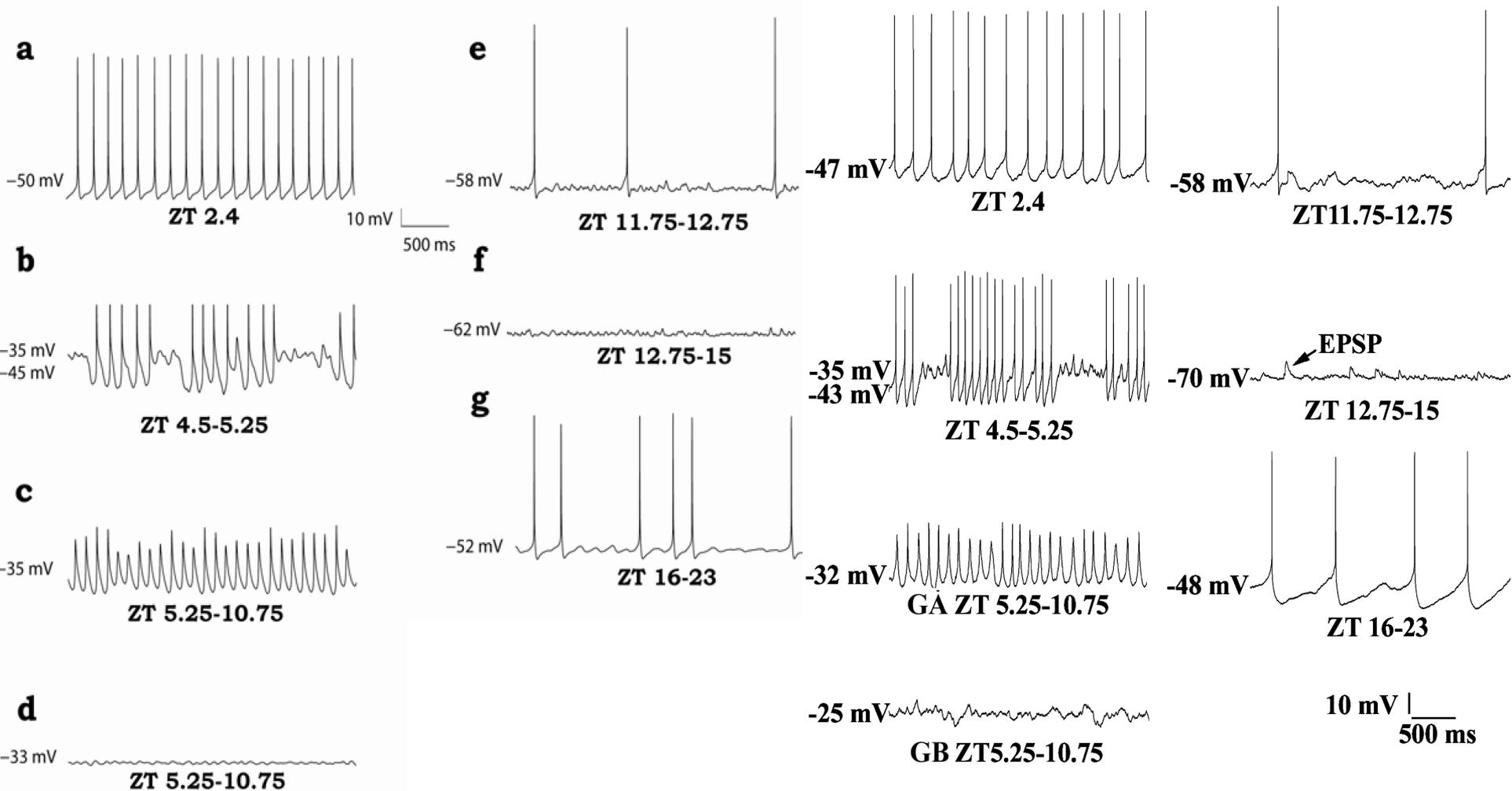
Diekman et al. PLoS Comp. Biology 2013



Mino Belle

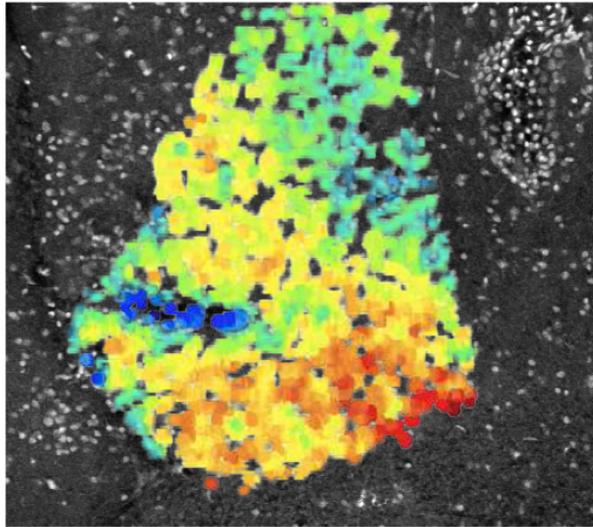
Belle, Diekman, Forger,
Piggins, Science, 2009

Per1 Cells

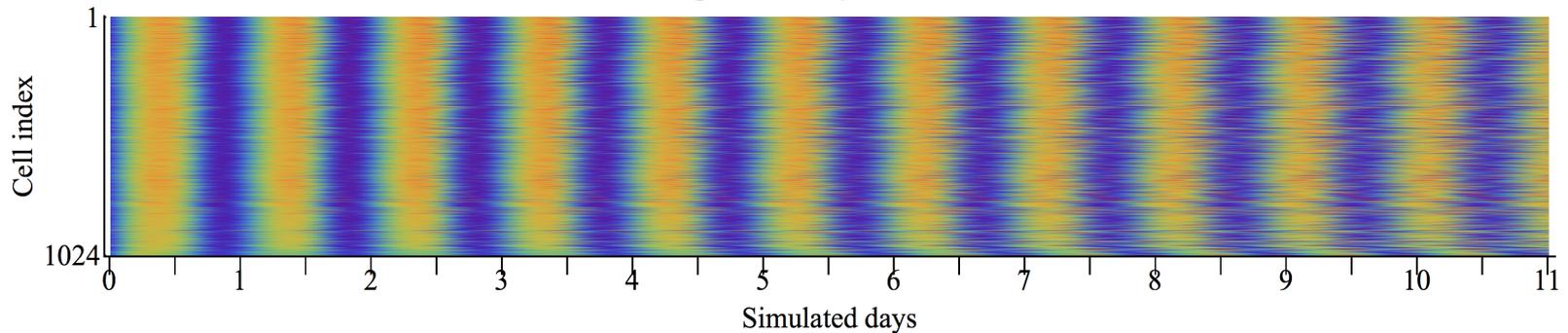
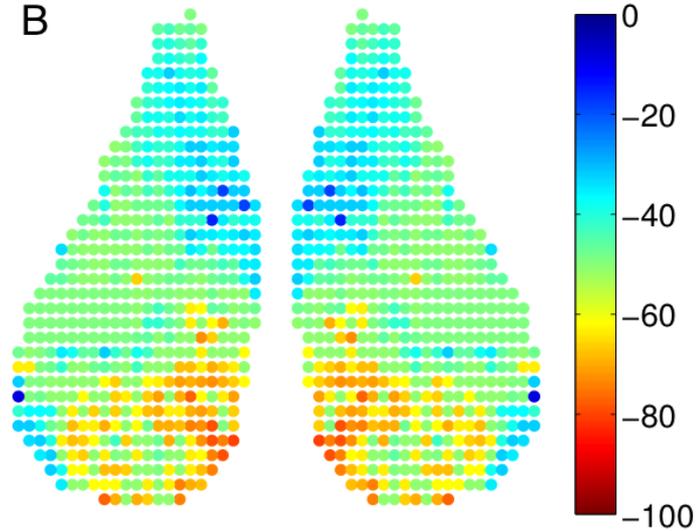


Fit data collected about GABA

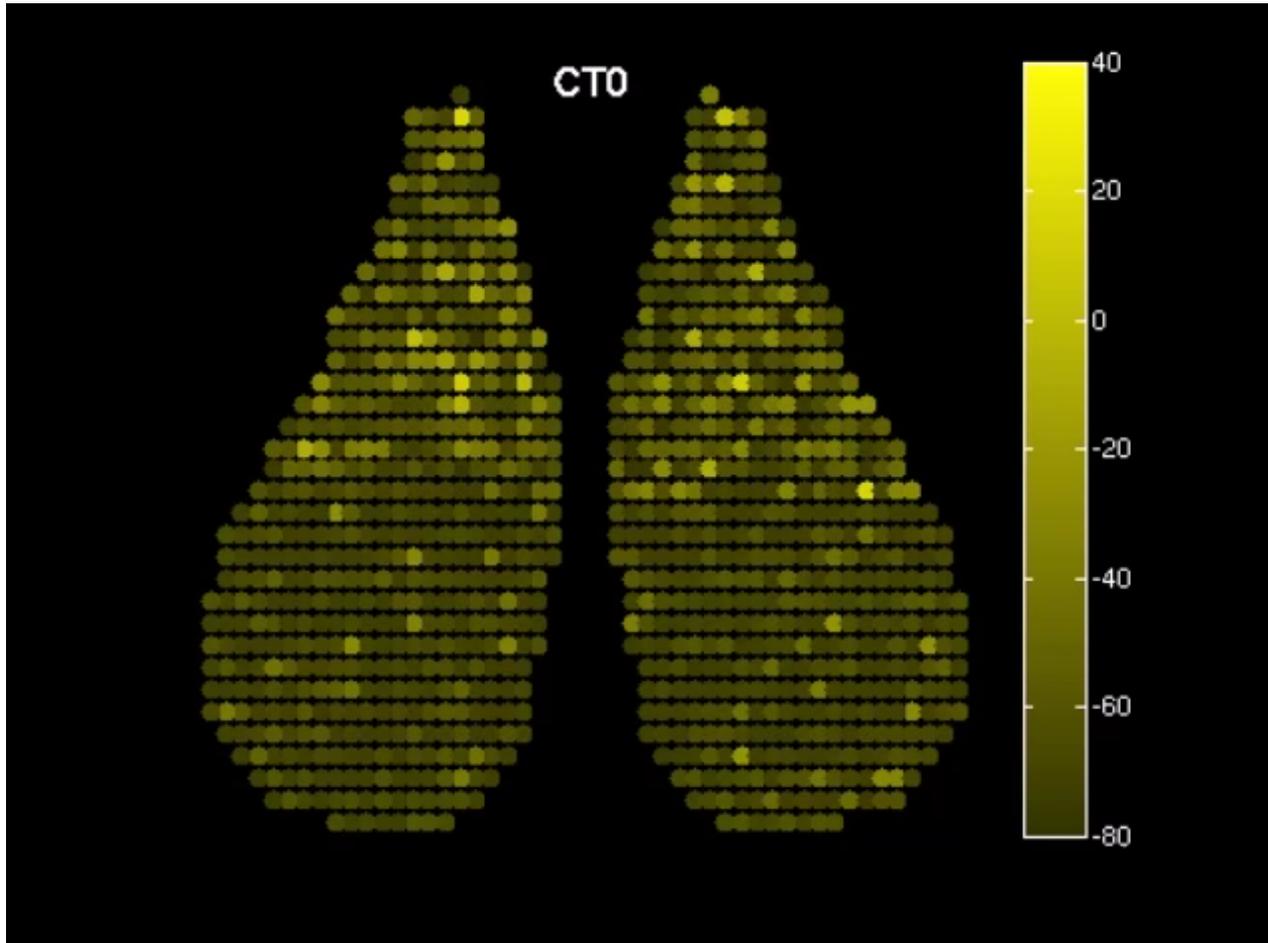
A



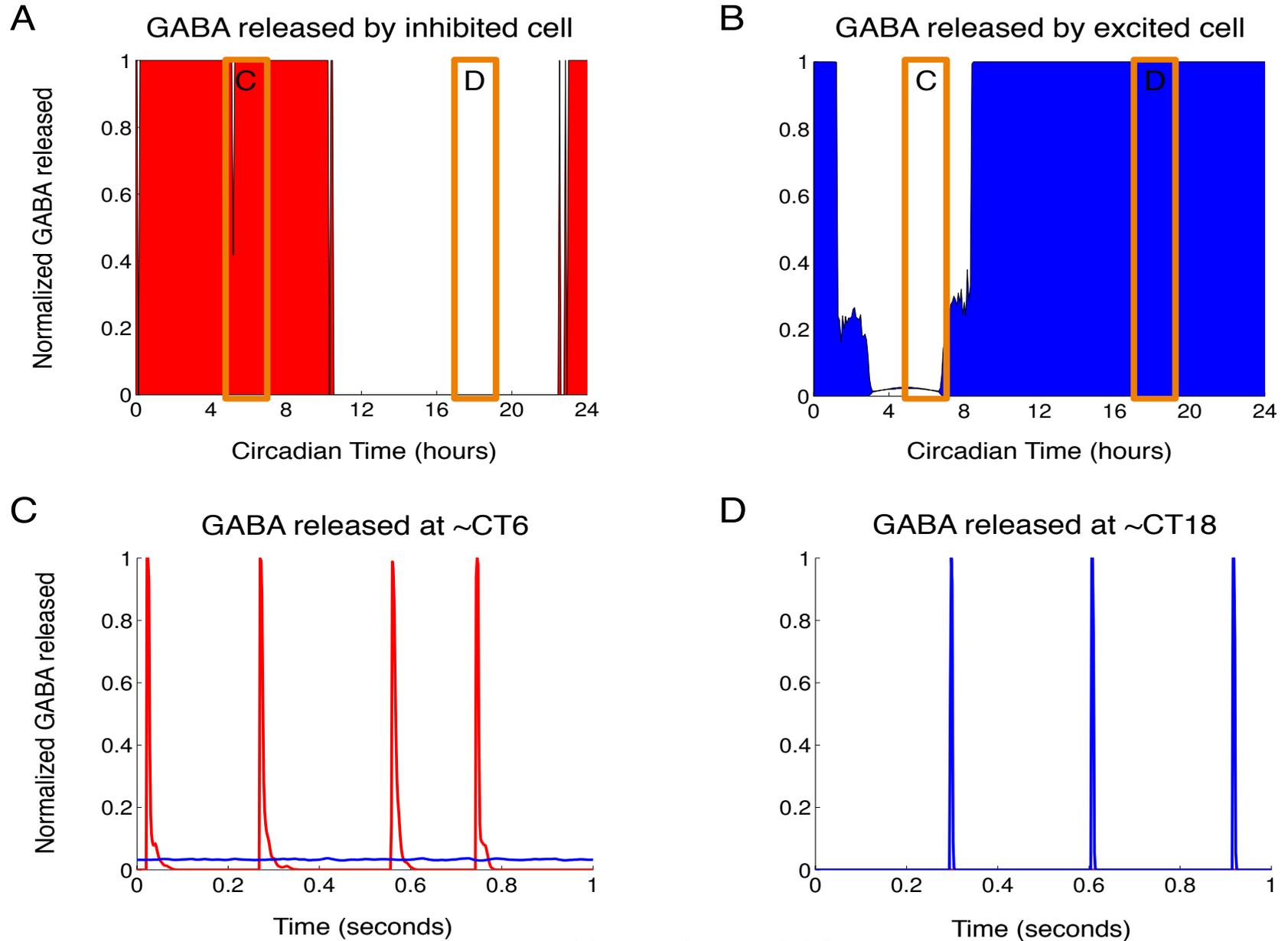
B



Electrophysiology



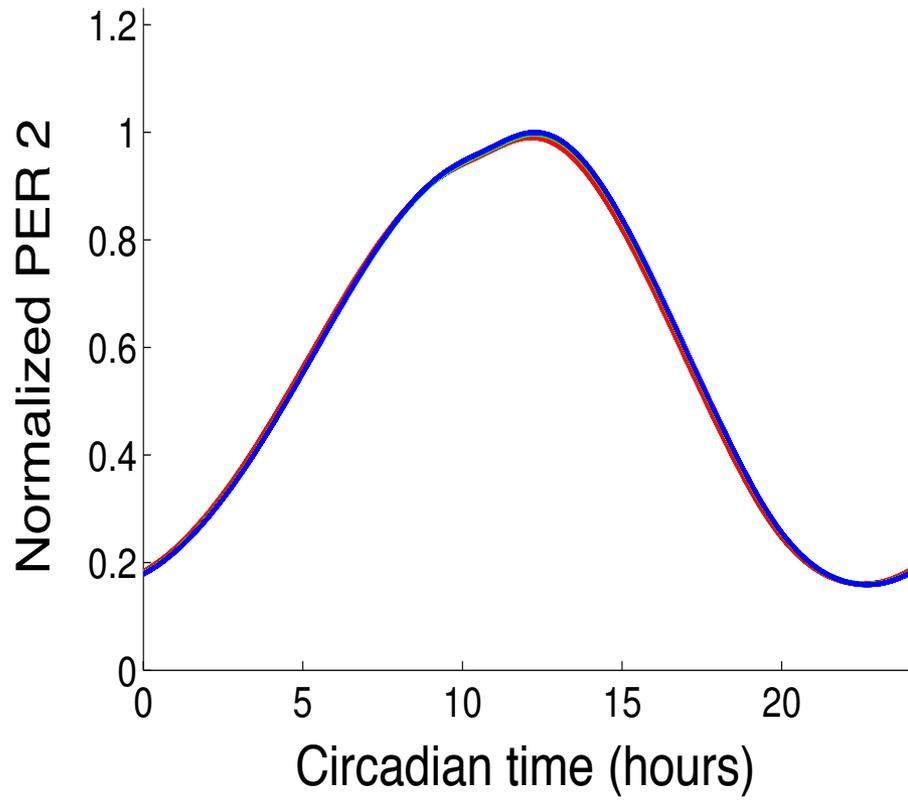
Two GABA signals



Tonic GABA controls phase distribution

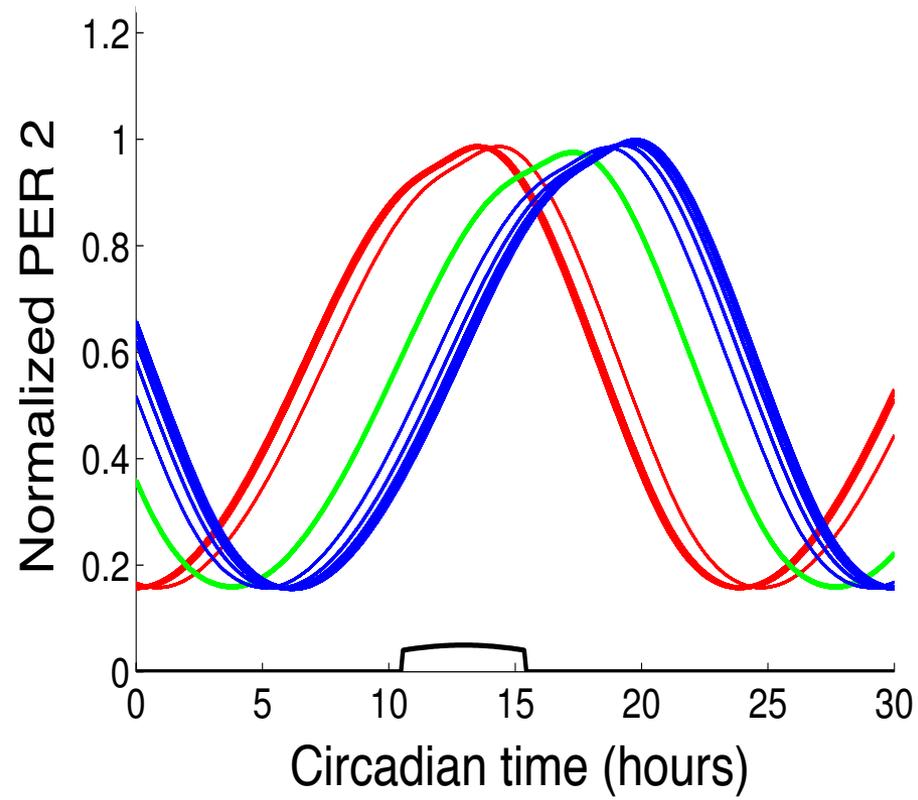
A

Five hour 10 Hz GABA stimulus

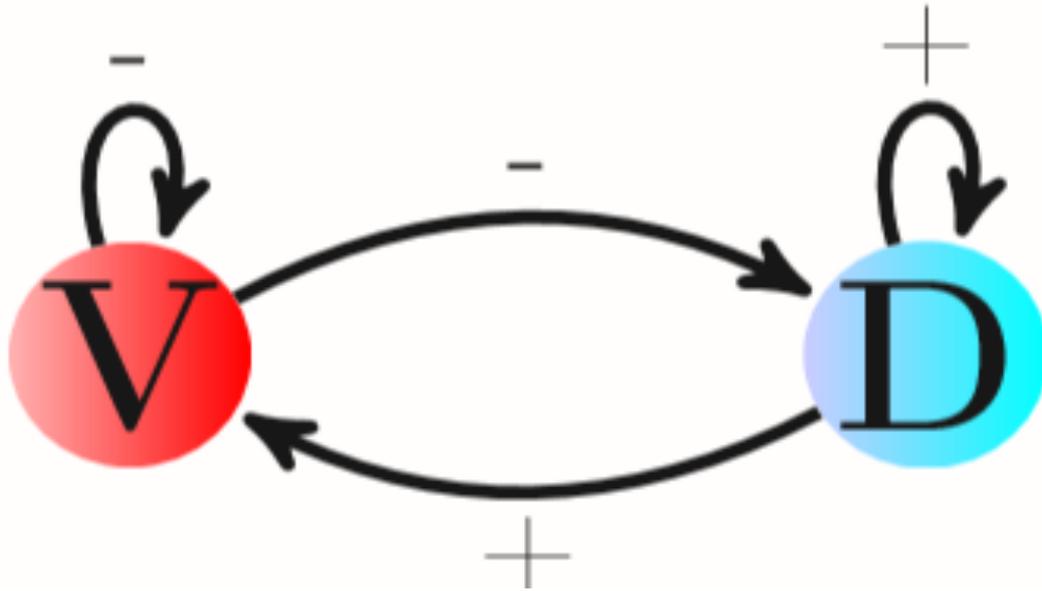


B

Five hour tonic GABA stimulus



Tonic GABA coupling in the SCN

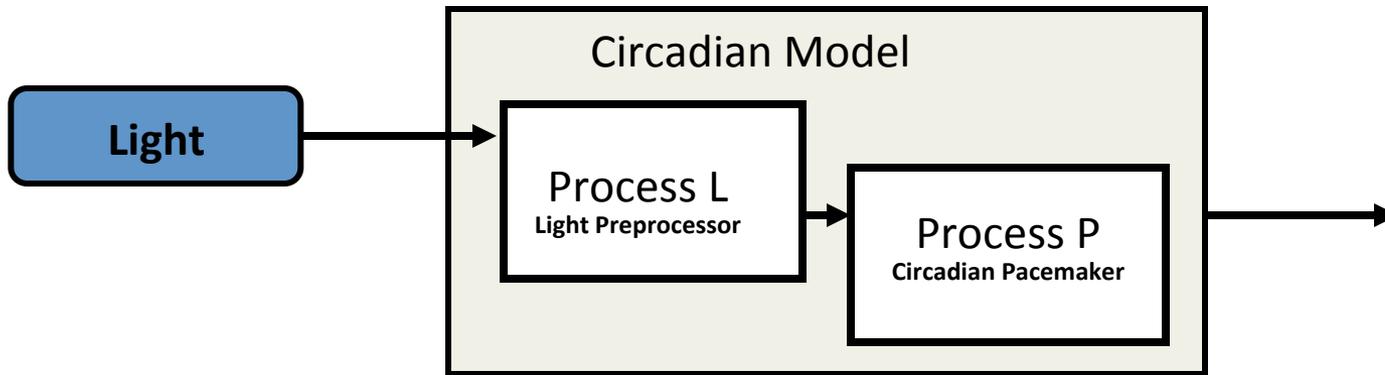


- See Myung et al. PNAS 2015 for large scale simulations and analysis of bioluminescent data
- Explained by SCN aftereffects and Ott-Antonsen theory

Key challenges

- What are all the action potentials doing?
 - Subconscious vision (Stinchcombe and collaborators)
- How can we quickly simulate this system?
 - GPU computing
 - Library method developed by Cai and colleagues
 - Exponential Integrators
 - Population density methods solved by particle methods

Human Circadian System (Forger, Klerman, Kronauer, Jewett ...)



$$\alpha(I) = 0.05 \frac{I^{0.6}}{9500^{0.6}}$$

$$\frac{dn}{dt} = \alpha(I)(1 - n) - 0.013n$$

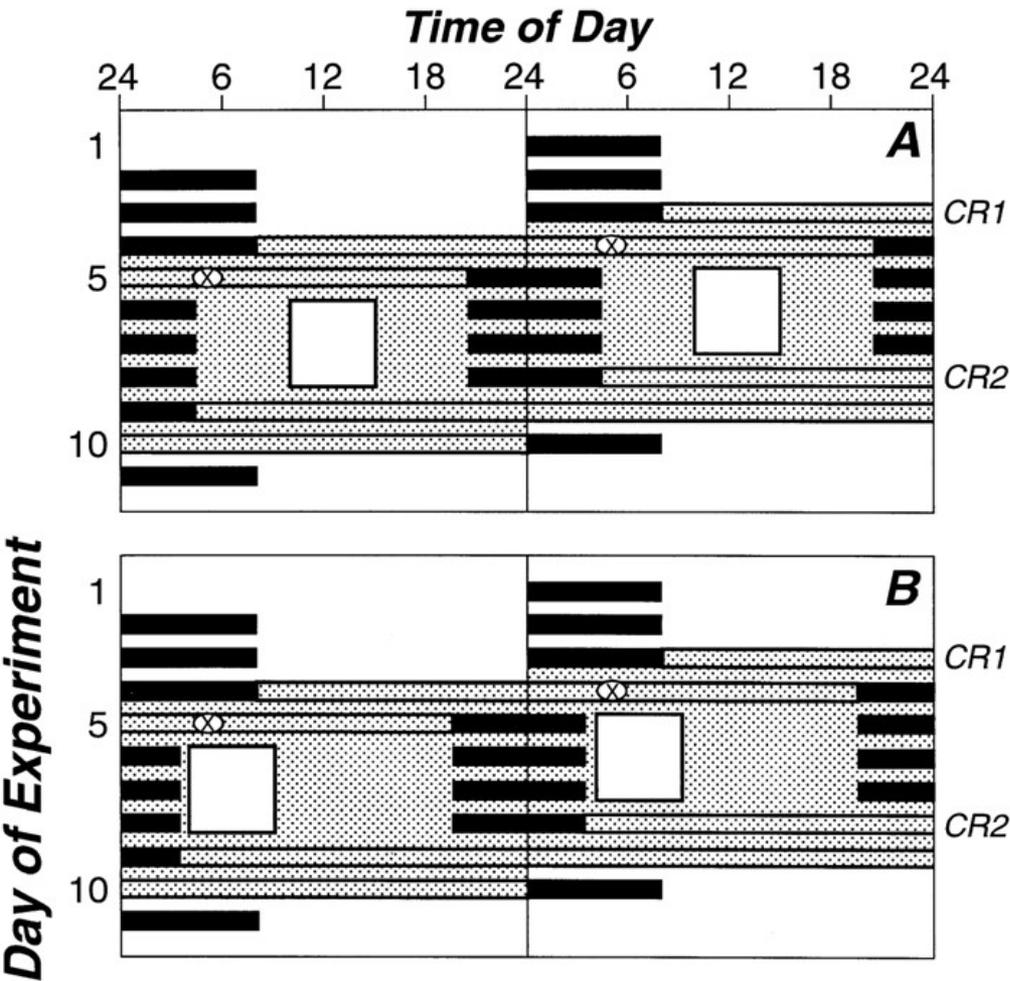
$$B(n, x, x_c) = 19.875(1 - 0.4x)(1 - 0.4x_c)\alpha(I)(1 - n)$$

$$\frac{dx}{dt} = \frac{12}{\pi} (x_c + B(n, x, x_c))$$

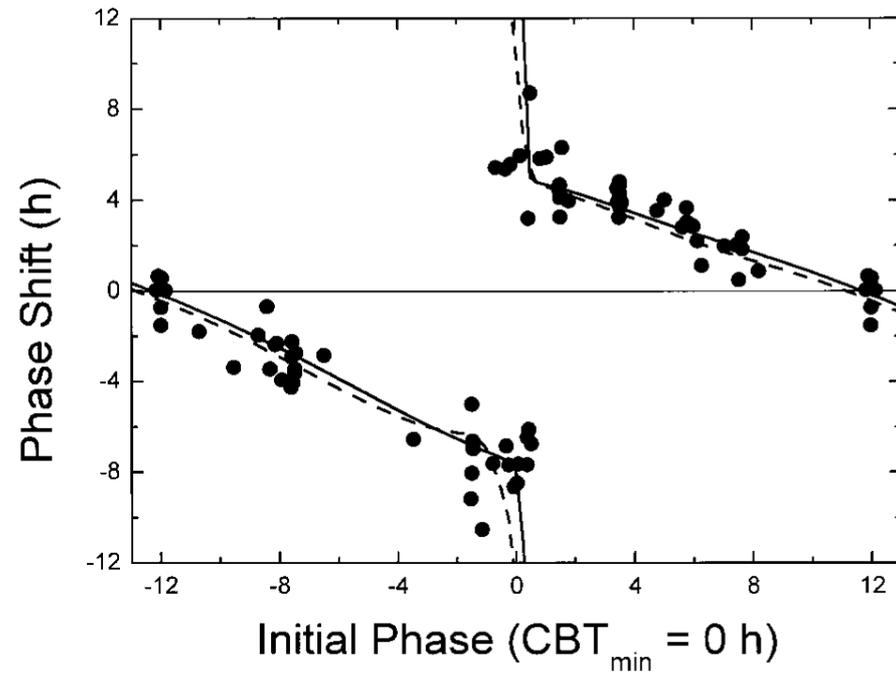
$$\frac{dx_c}{dt} = \frac{12}{\pi} \left(-x(0.9901 + 0.55B(n, x, x_c)) + 0.23 \left(x_c - \frac{4}{3}x_c^3 \right) \right)$$

Human Phase Shifting to Light

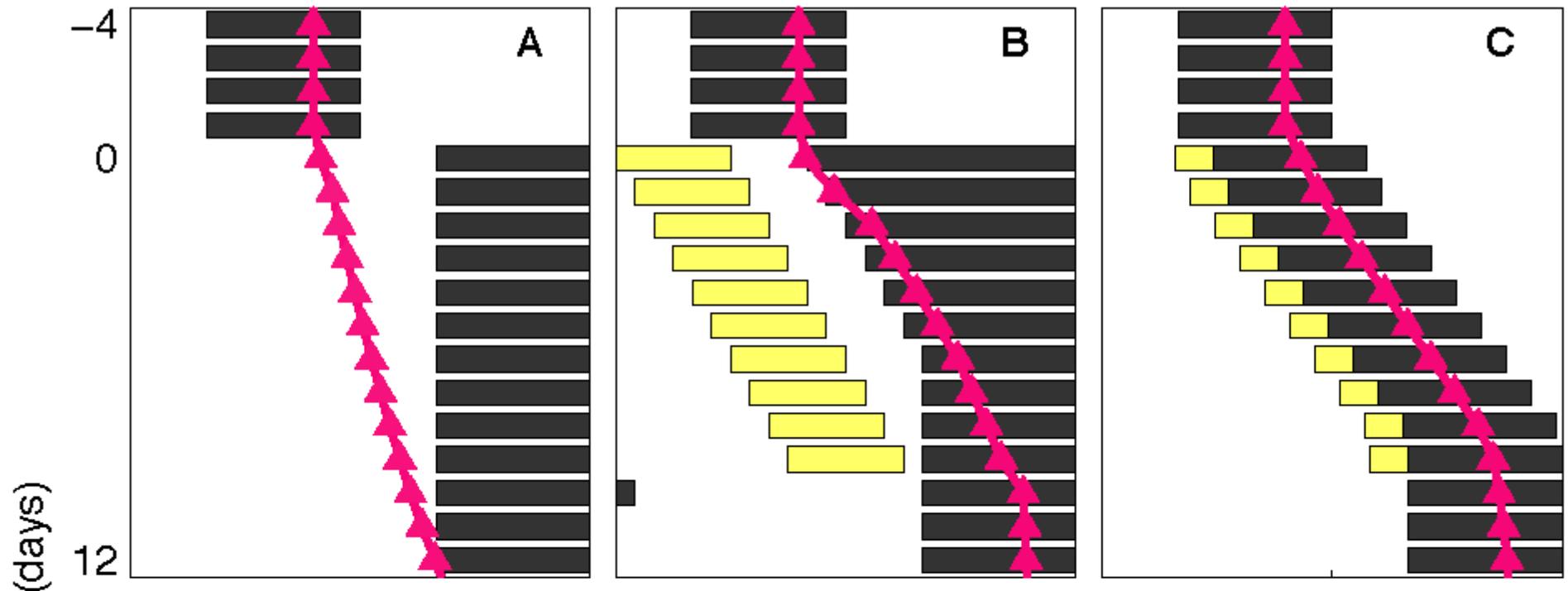
- Jewett et al. AJP 1997



- Forger et al. JBR 1999



Evaluation of Schedules

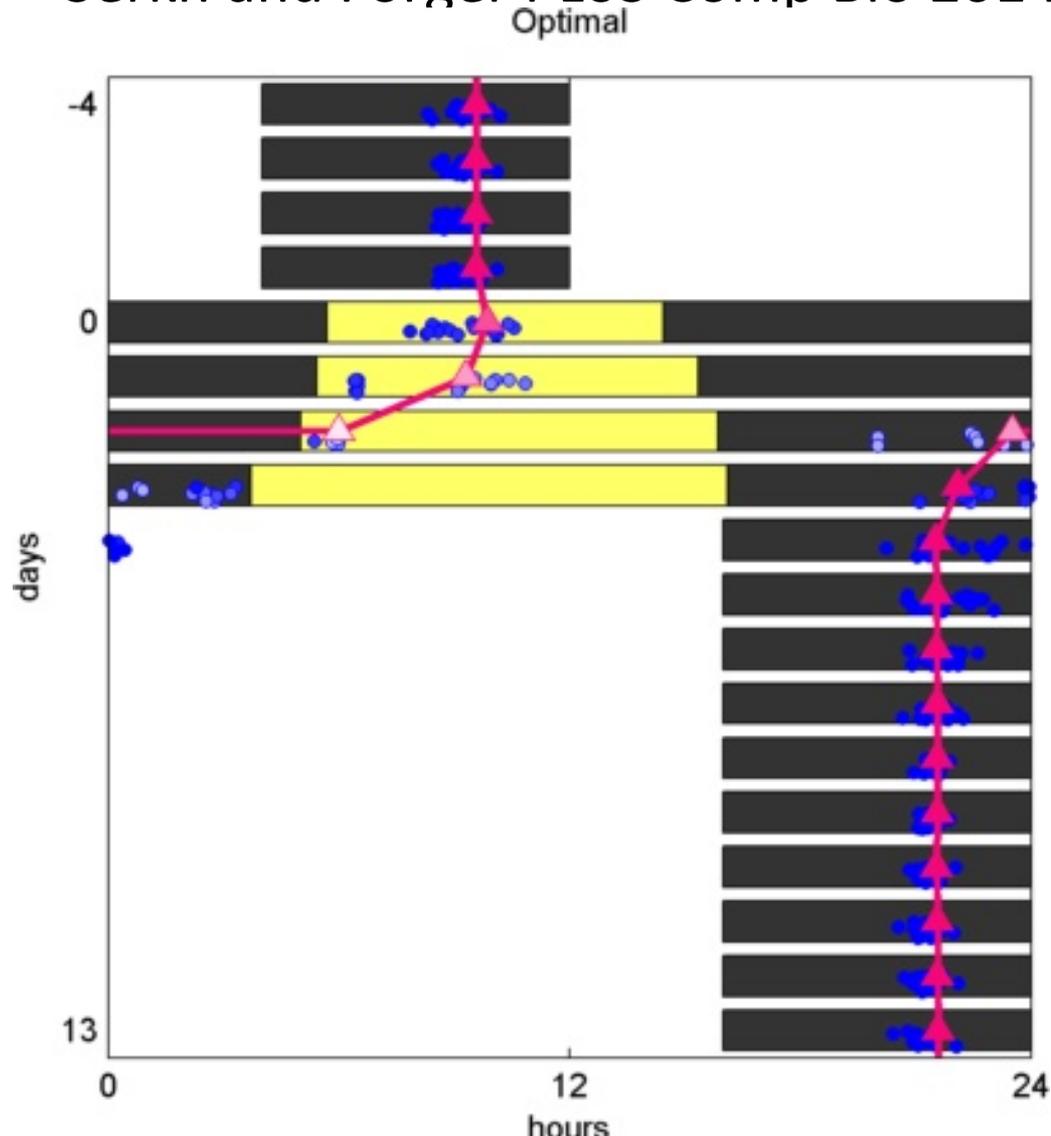


Formulating the problem in terms of optimal control

- Starting at a specified state $X(0) = a$, and dynamical system $dX/dt = f(X, u)$ choose a control, $u(t)$, such that for minimum t_f $X(t_f) = X_e(t_f)$
- Too difficult and not applicable
- Instead have a constraint that we are on the correct isochron $\psi(X(t_f), t_f) = 0$ (i.e. have correct phase)
- Have a cost function $\phi = t_f + b |A(X(t_f)) - A(X_e(t_f))|$

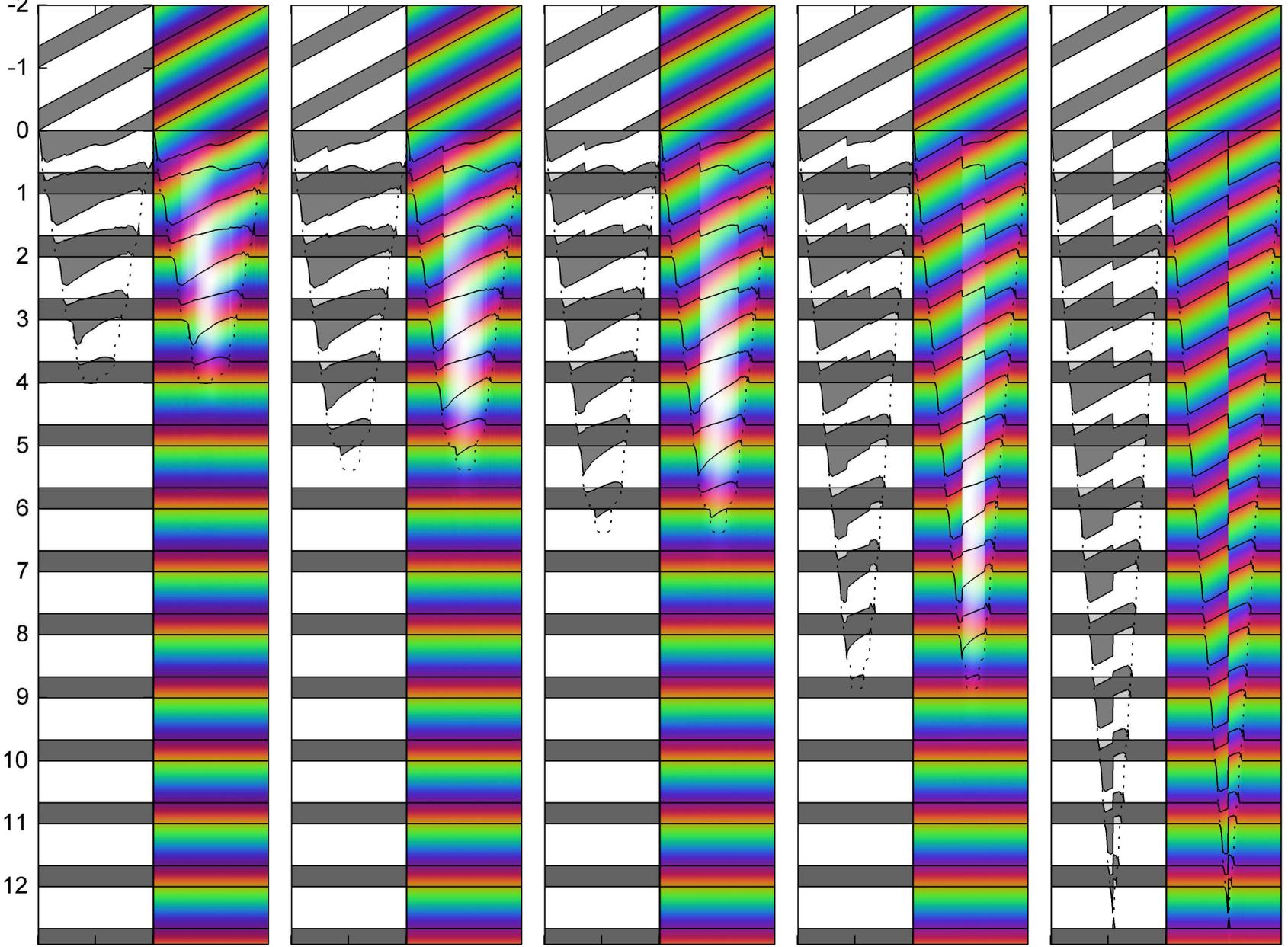
Optimal Schedules (with much mathematics)

Serkh and Forger PLoS Comp Bio 2014



Initial phase (hours)

0 12 0 12 240 12 0 12 240 12 0 12 240 12 0 12 240 12 0 12 24



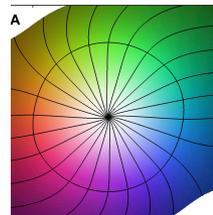
10000 lux **A**

1000 lux **B**

500 lux **C**

200 lux **D**

100 lux **E**



How to test this? Travelers...

- **We** provide an app **for free** which simulates the latest mathematical models on the iPhone and gives you our best guess at an optimal schedule.

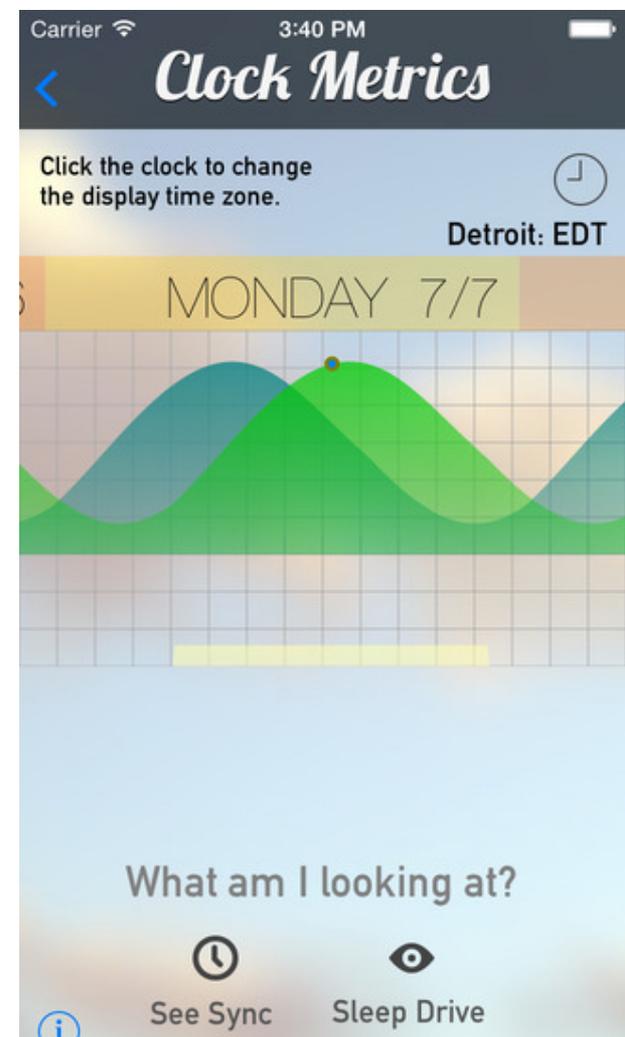
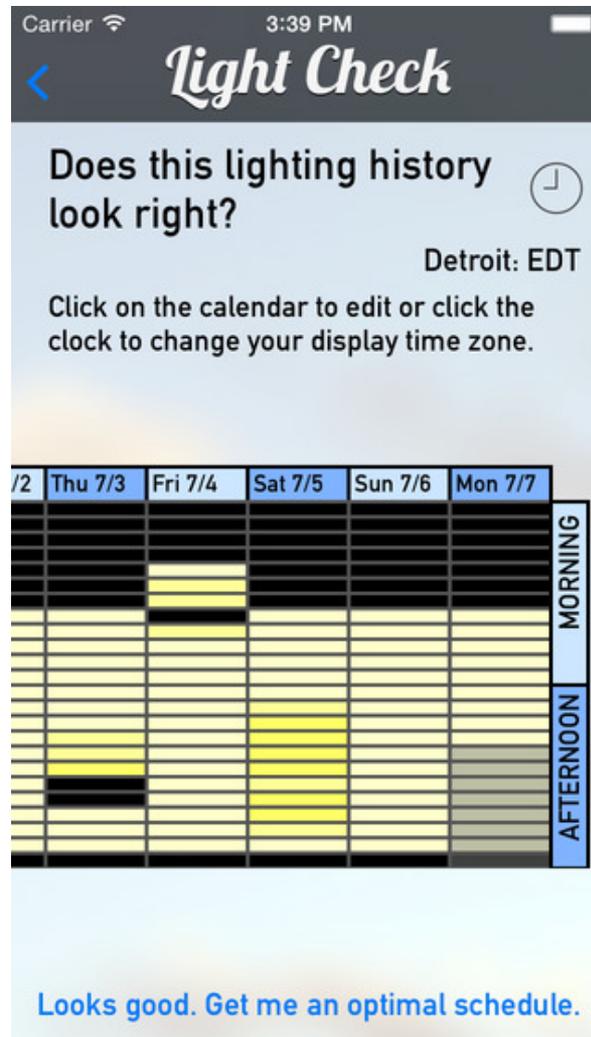
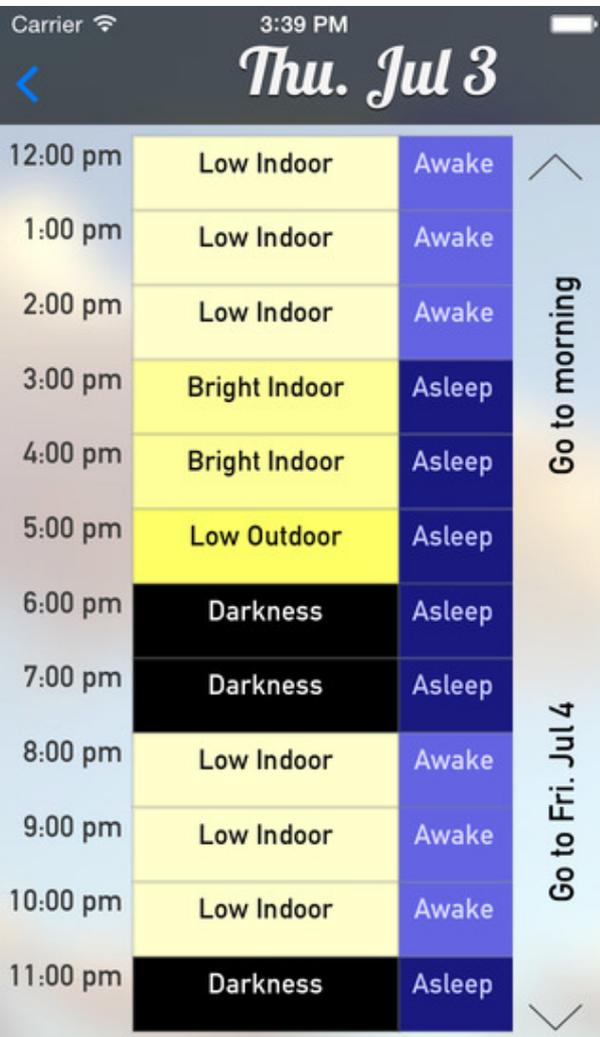
This is only available in very specialized applications

- **YOU** provide data on your lighting history, sleep-wake pattern and rate symptoms of jetlag, and demographics

This could give us the real-world data we need

ENTRAIN

(Olivia Walch and Amy Cochran)



Top 300 Free iPhone Apps for Travel

Filters: » iPhone » Travel » Free » Rank

#1		Uber Developer: Uber Technologies, Inc. Released: May 20, 2010 in Travel		18
↔	★★★★★			
#2		Expedia Hotels & Flights Developer: Expedia, Inc. Released: Apr 7, 2011 in Travel		10.9
↔	★★★★☆			
#3		Google Earth Developer: Google, Inc. Released: Oct 27, 2008 in Travel		390
↔	★★★★☆			
#4		Hotels.com – Hotel Booking and last... Developer: Hotels.com Released: Jul 11, 2008 in Travel		10.9
↔	★★★★☆			
#5		Yelp Developer: Yelp Released: Jul 11, 2008 in Travel		4.92
↔	★★★★☆			
#6		Entrain Developer: The University of Michigan Released: Apr 9, 2014 in Travel		<0
↔	★★★★☆			
#7		My Disney Experience – Walt Disney... Developer: Disney Released: Aug 2, 2012 in Travel		150
↑2	★★★★☆			

Global Assessment of Sleep

- Walch et al. Science Advances 2016
- Much media attention
- “Oh, Good Morning, Sleep Science, Welcome to the 21st Century.” Wired

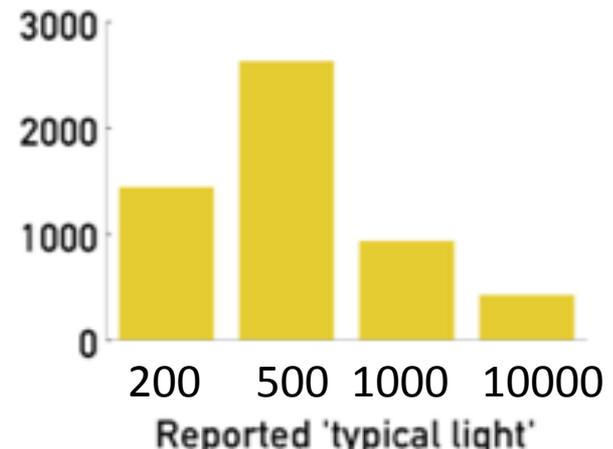
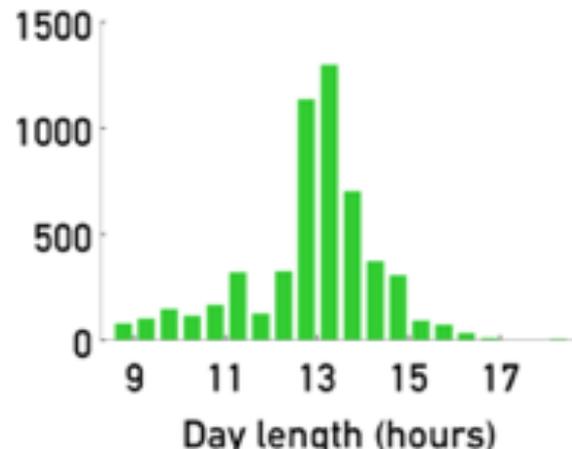
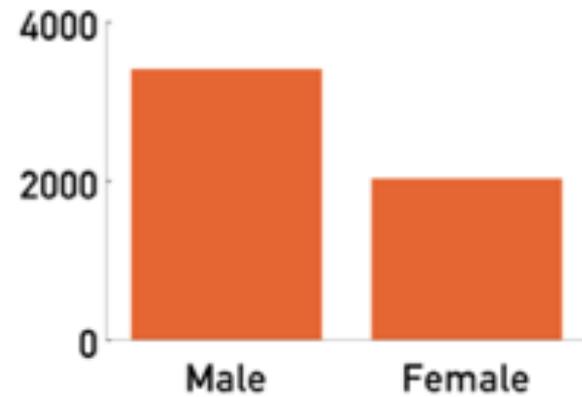
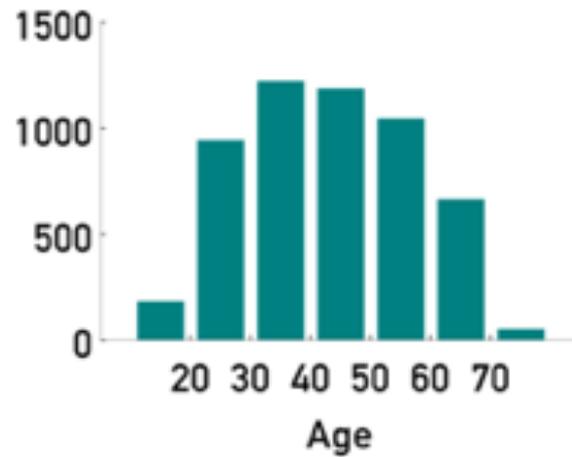


Basic Demographics

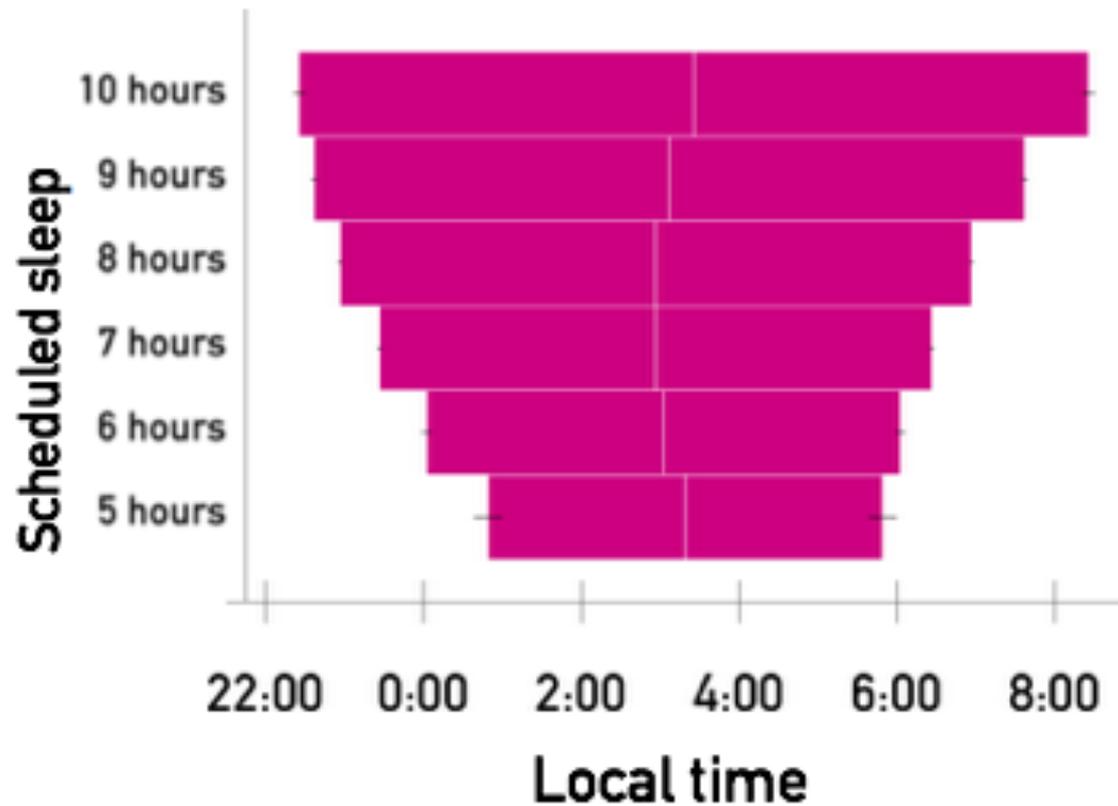
- Top three countries contributing data: the United States (45%), Australia (9%), and Canada (5%).
- Top six European countries (UK, France, Spain, Netherlands, Denmark, and Germany) contribute 15%
- Everyone else 25% (no individual country more than 2%)



Basic Demographics

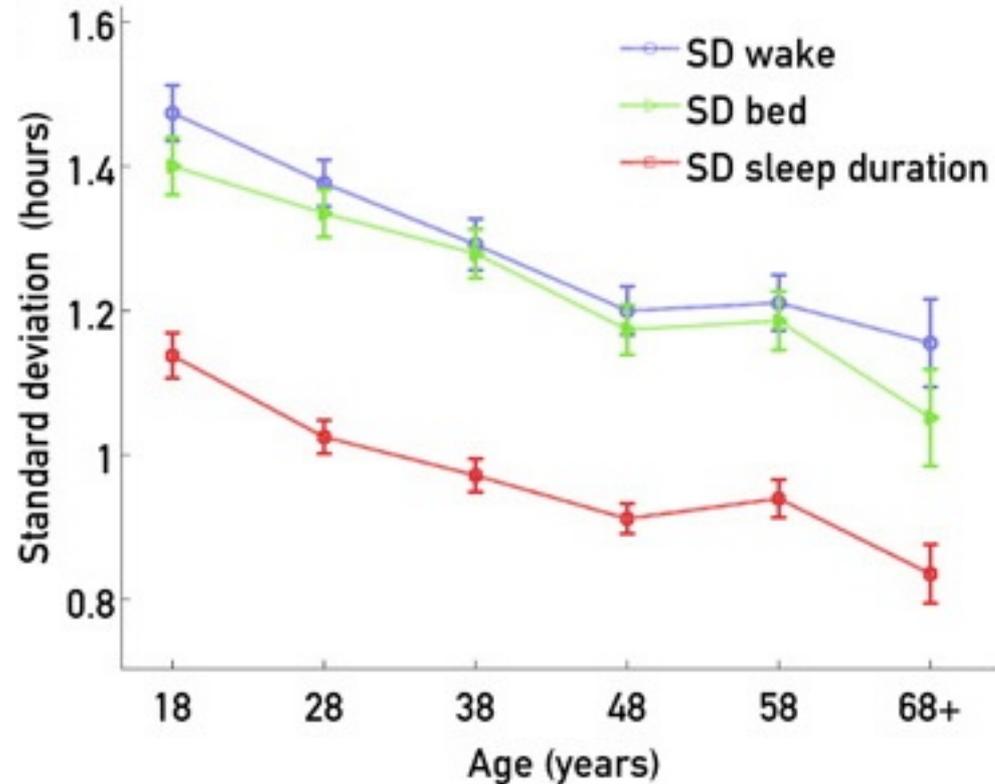


Basic Demographics



Age and Sleep:

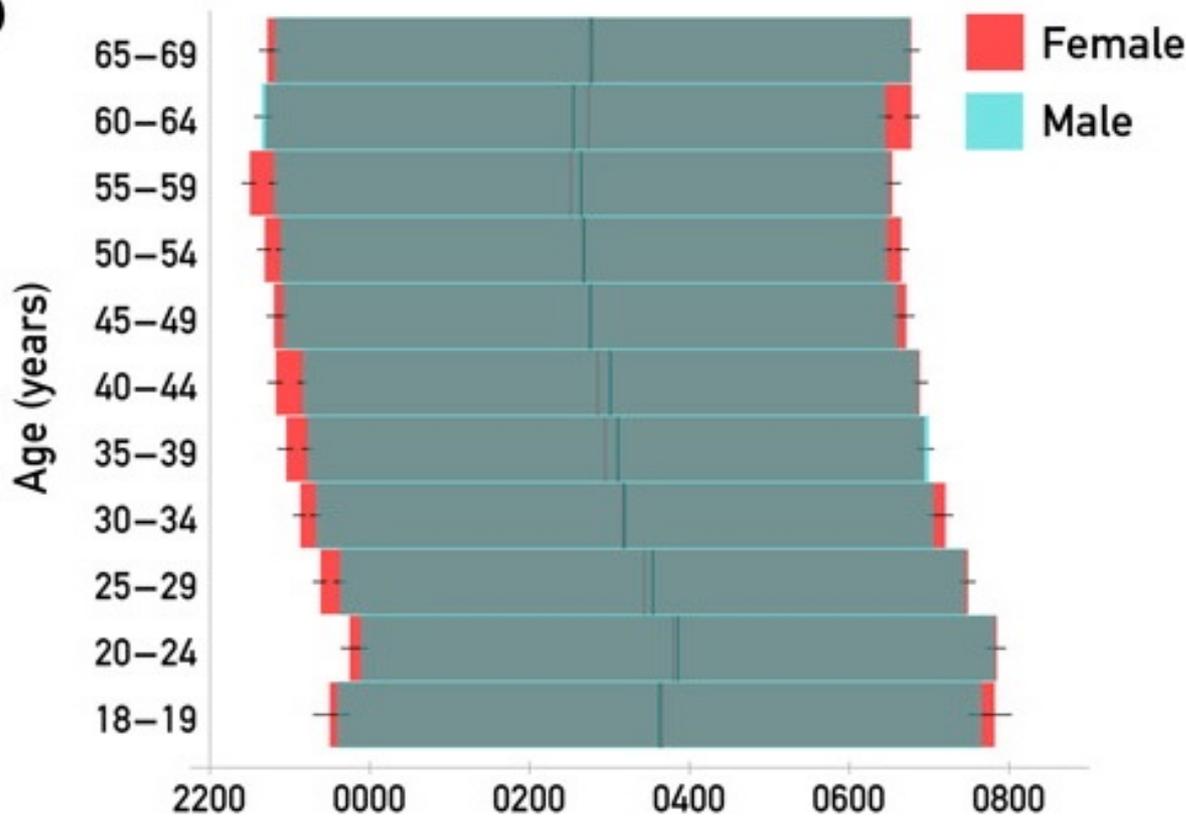
(Also works for coefficient of variation)



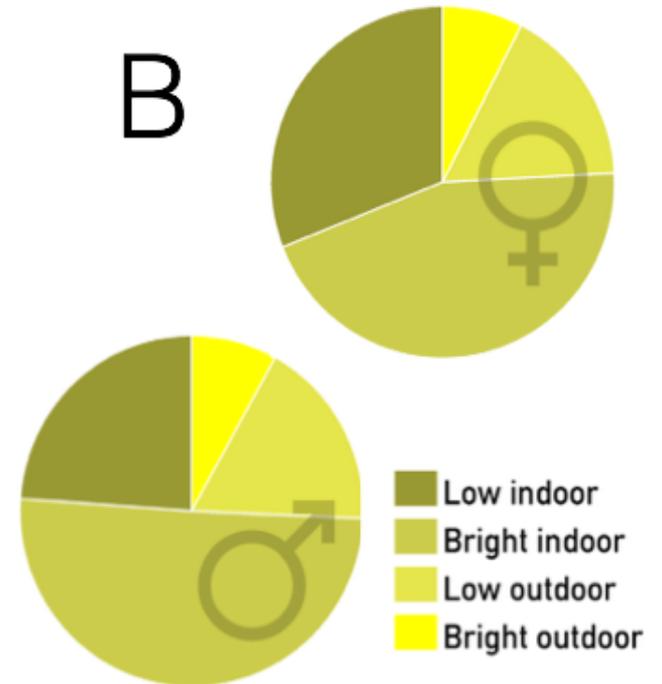
Less variability for outdoor population

Age Sleep and Gender

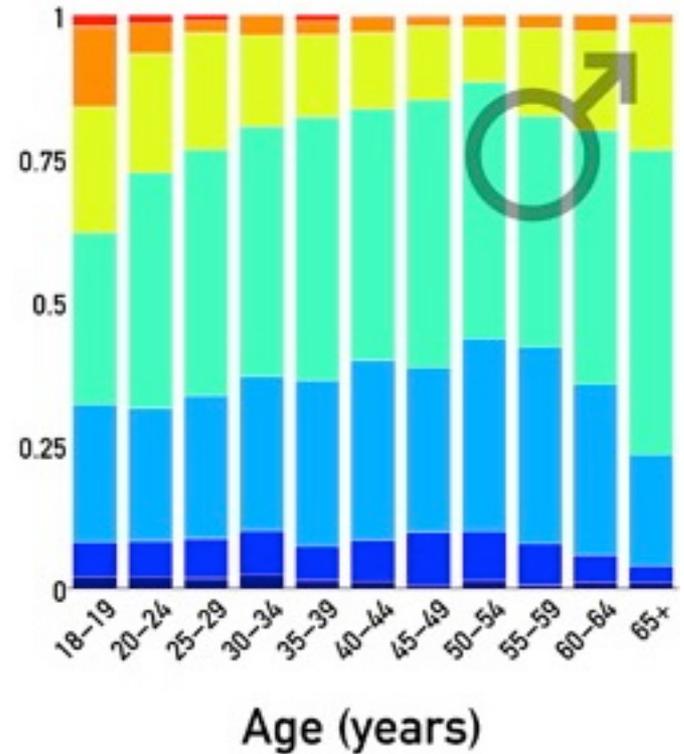
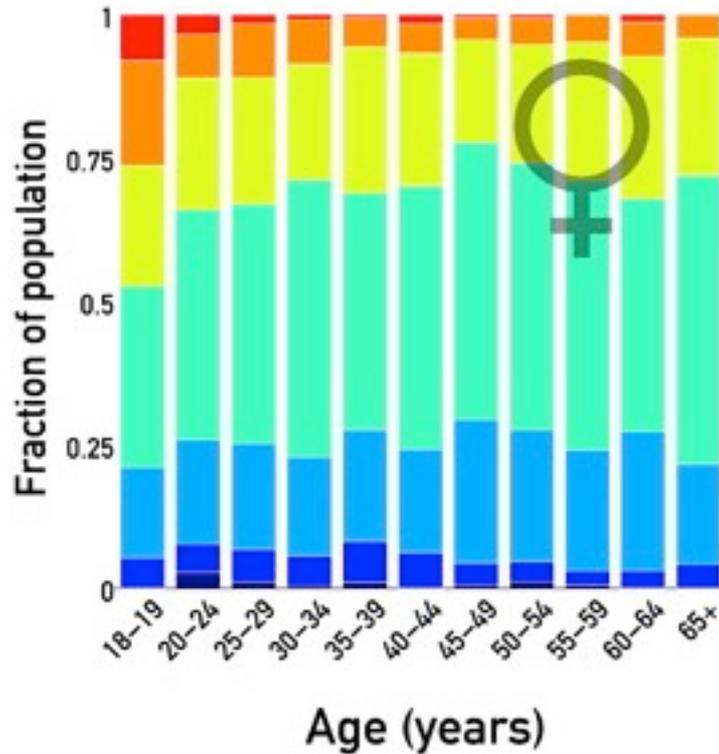
D



B



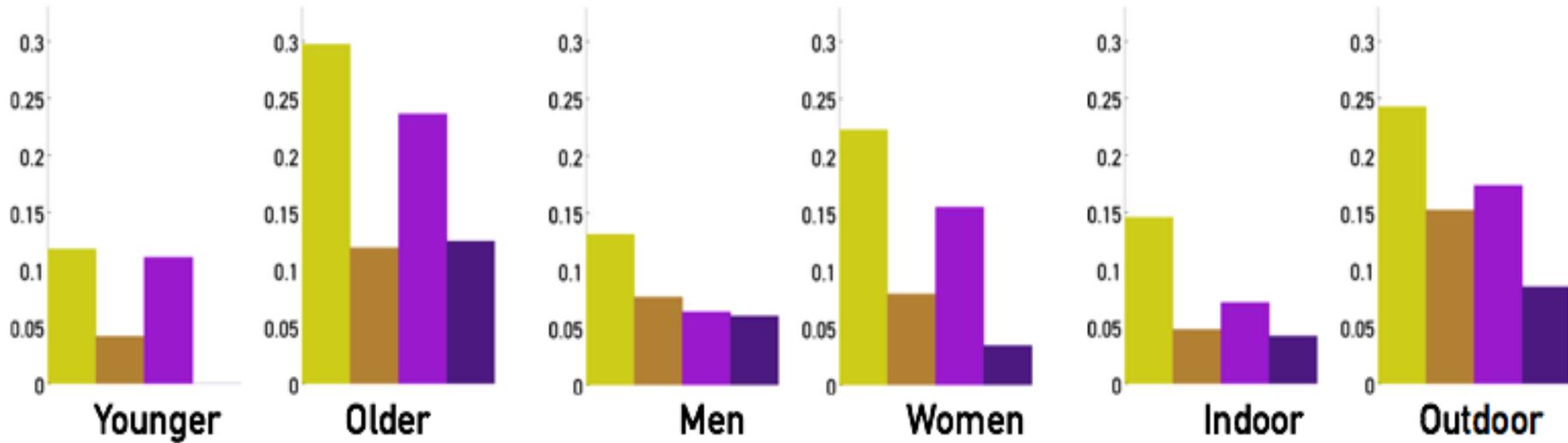
Age and Sleep



Notes from Statistical Analysis

- Age is most dominant influence on sleep timing
- Gender has the strongest influence on sleep duration.
- The shorter sleep durations during middle age can be attributed primarily to **men** and the group of population reporting **indoor light**.

Sunrise, Sunset and Sleep

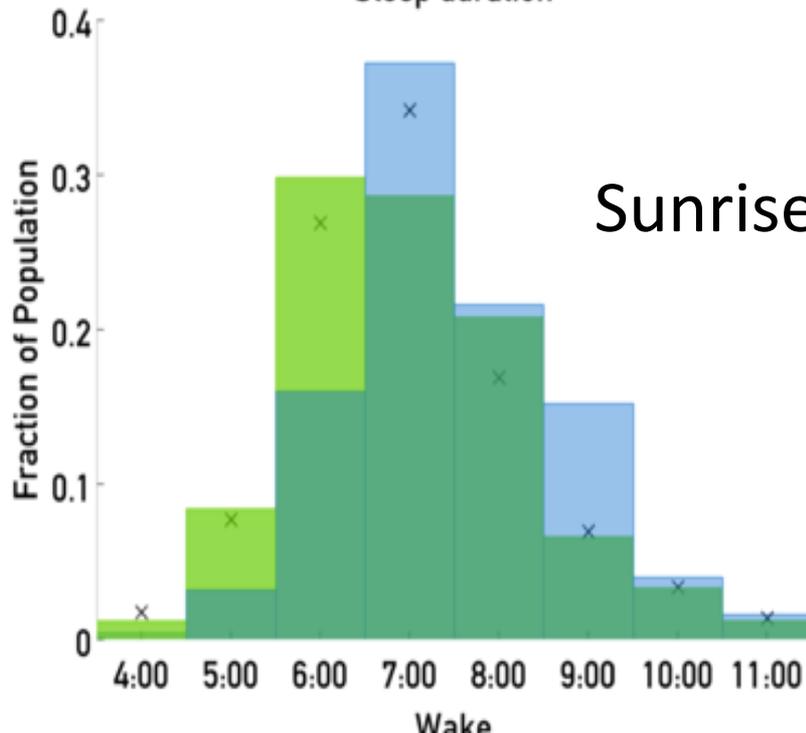
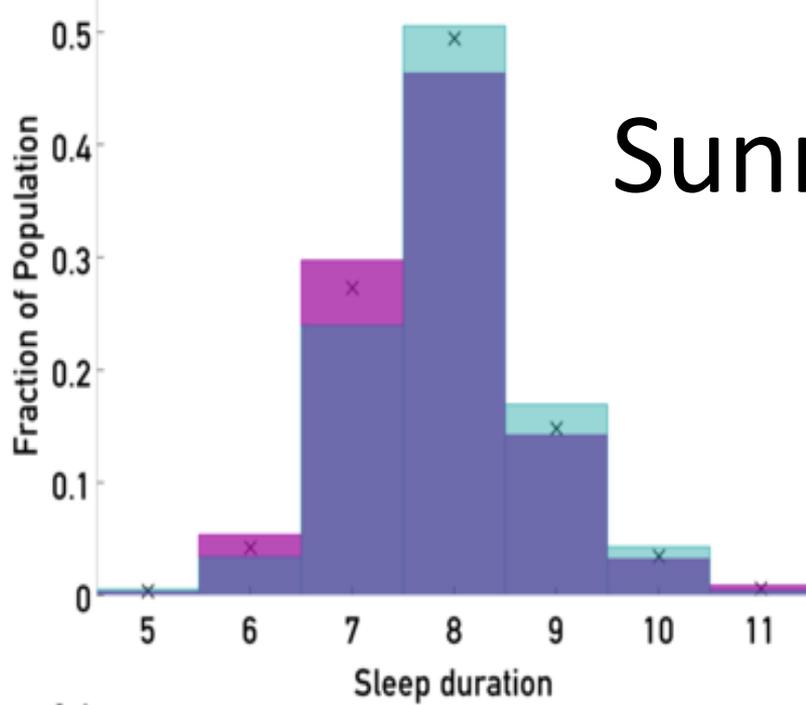


Age

Gender



Sunrise, Sunset and Sleep

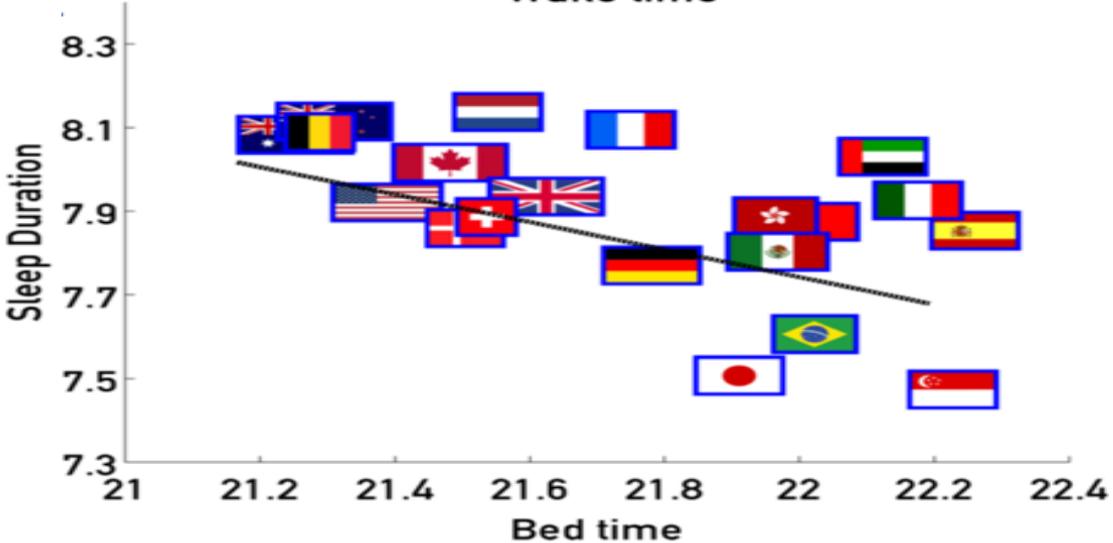
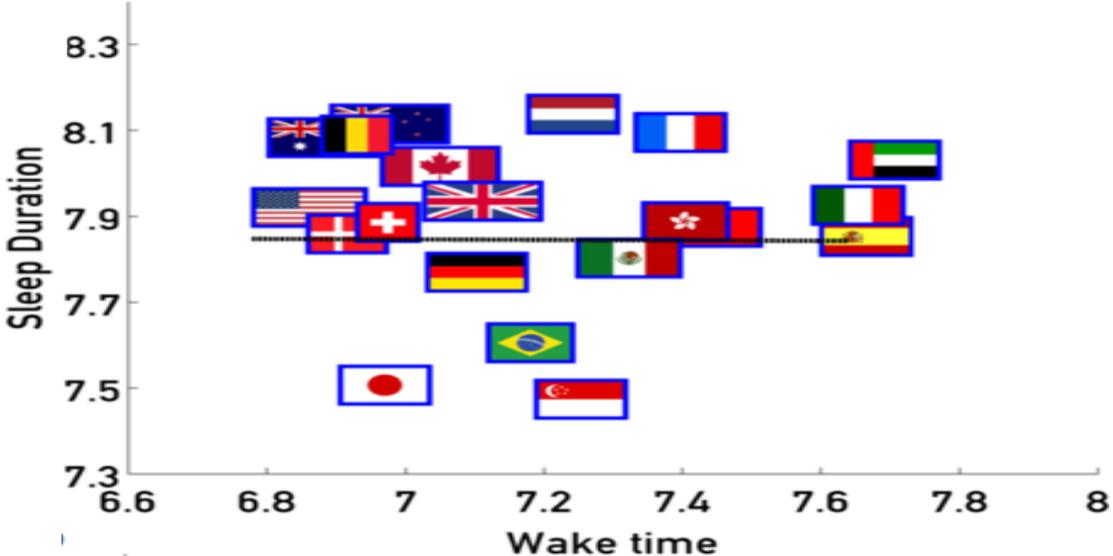


Sunrise before 5:30 or after 7:30

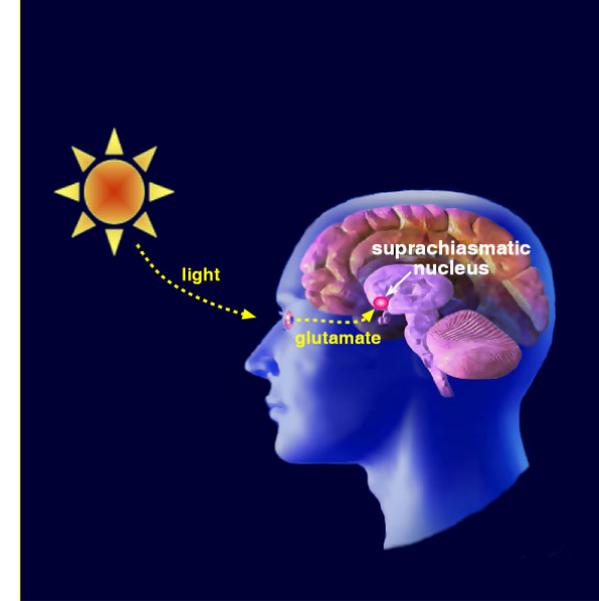
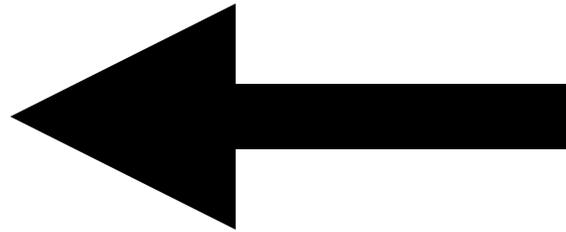
Notes from statistical analysis

- Later sunsets are correlated with more sleep, mainly through wake
 - More Sleep in summer
- Women, older, and outdoor individuals are more sensitive to changes in sunrise and sunset than men, as indicated by higher regression coefficients.
- Sunset affects wake more than bed
 - Supported by additional simulations

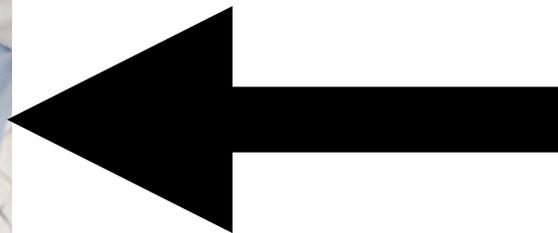
Societal Effects Through Bedtime



Conclusion

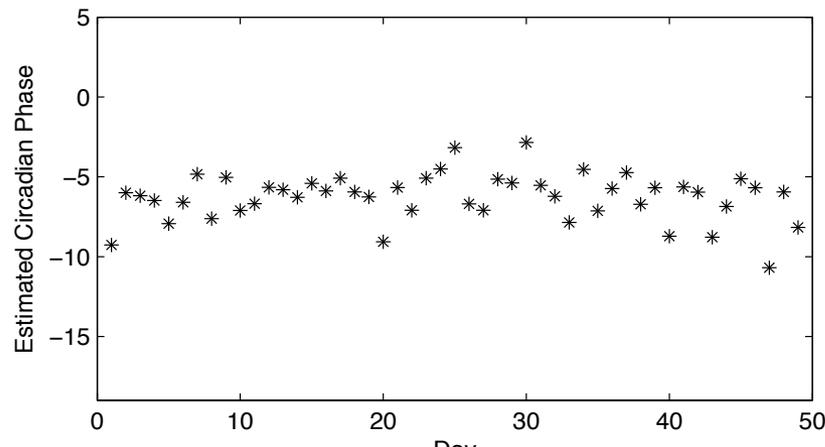
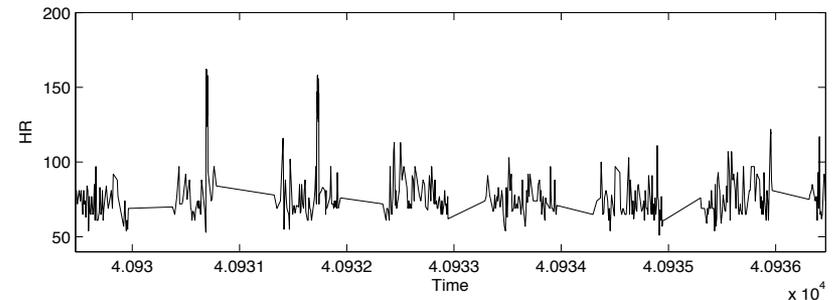
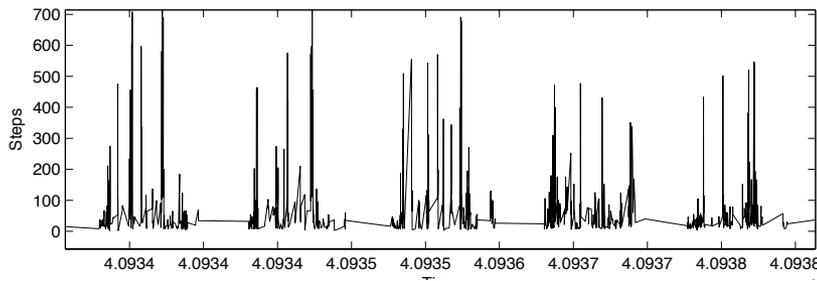


Sleep



Key challenges

- How to incorporate self reported data in models?
- How to include societal effects?
- How to analyze data from smartphones?



Thanks

- Biomathematics program at Army
- Human Frontier Science Program
- AFOSR