# Math Modeling and Sustainability: Using Service Learning Projects to Deepen Student Engagement with Modeling.

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July 10, 2018

# What are some issues facing the nation and the world that you are concerned about?

What are some issues facing the nation and the world that you are concerned about?

A goal of my presentation is to show how mathematics can be connected to these issues you care about.

# Math Modeling and Sustainability Course

Taught at various levels:

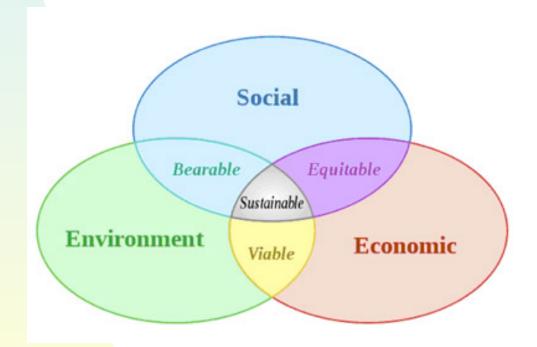
Gen Ed, math major course, senior seminar, Secondary teacher institute

Service Learning/Community Based Learning: student projects in partnership with community

Syllabus, course assignments: https://tinyurl.com/ya6e2msy

# Sustainability:

Meeting the needs of present and future generation by reconciling economic growth, social development and environmental protection.



# Education for Sustainability

# From the Cloud Institute

#### THE 9 CORE EfS STANDARDS

**Cultural Preservation & Transformation** 

Responsible Local & Global Citizenship

The Dynamics of Systems & Change

**Sustainable Economics** 

**Healthy Commons** 

Natural Laws & Ecological Principles

**Inventing & Affecting The Future** 

**Multiple Perspectives** 

**Strong Sense Of Place** 

### Topics:

Curve fitting using real data

Rates of change (derivatives)

Area under curve (integration)

- Riemann sums
- Energy is area under power curve
- Total water run-off is integral of rate of flow

## **Energy Modeling**

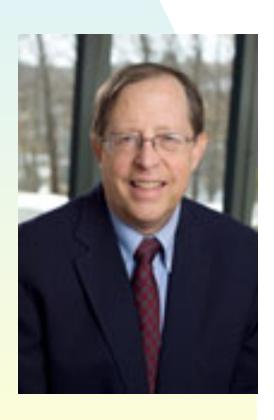
- cost of energy use; units kWh
- carbon footprint of energy generation
- potential for energy generation (solar, wind)

### Financial Modeling:

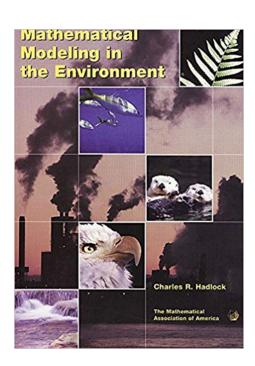
- Fixed (capital) costs, operating costs
- Pay back time
- Net present value

# Math Modeling and the Environment

Charles Hadlock, Bentley University



- Ground water flow
- Darcy's Law
- Laplace equation
- Heat flow



# Math Modeling and Sustainability Tom Pfaff, Ithaca College

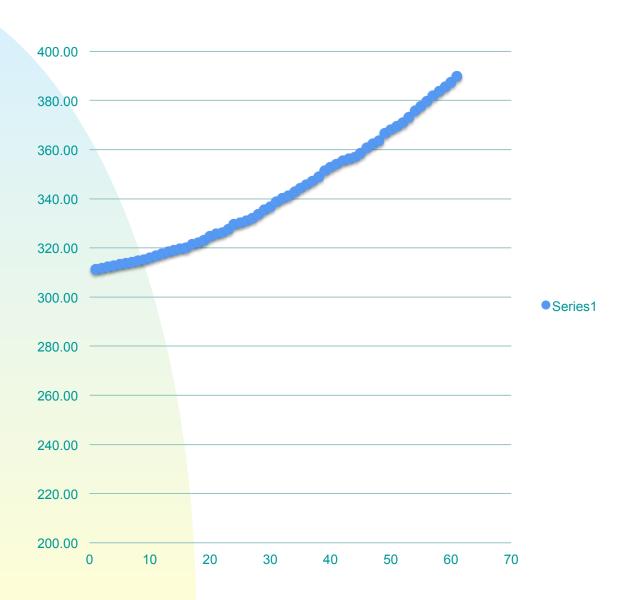


Developed teaching units on sustainability for a variety of courses

Blog site: http://sustainabilitymath.org/



# Are CO2 levels rising?



## Is it "Worth It" to Change your Light Bulbs?

Betsy Biernat and Hannah Weinstein, Bryn Mawr College

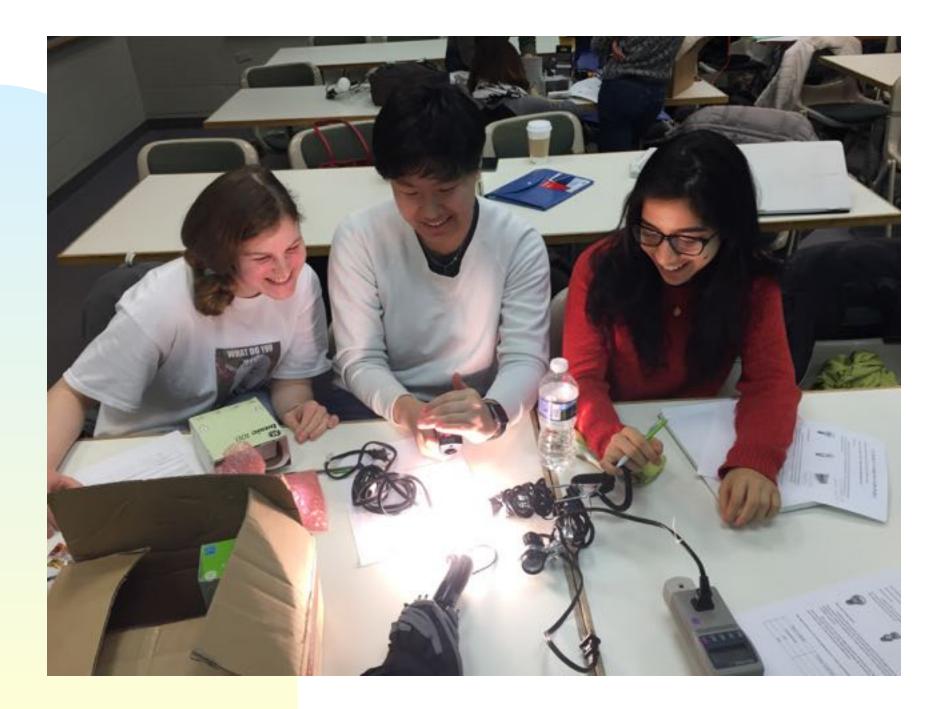
#### Brainstorm!

A light bulb in your home has burned out and you have no light bulbs stock-piled to replace it! Group brainstorm for 2 minutes: what factors would you take into account in deciding whether to buy an incandescent, CFL, or LED light bulb for your home?







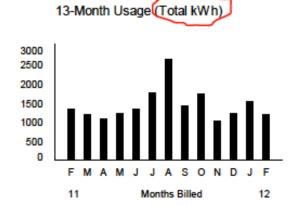


#### Home Electrical Bill

Electric Residential Service - Current Period Detail	Service 01/05/2012 to	02/06/2012 - 32 days
Customer charge	_	\$7.20
Generation Charges	1,179 kWh X \$0.0	9180 108.23
Transmission Charges	1,179 kWh X 0.0	0740 8.72
Wind Energy Service Charge	300 kWh X 0.00	2540 7.62
Distribution Charges	1,179 kWh / X 0.0	6000 70.74
State Tax Adjustment		-0.04

#### Total Current Charges

\$202.47



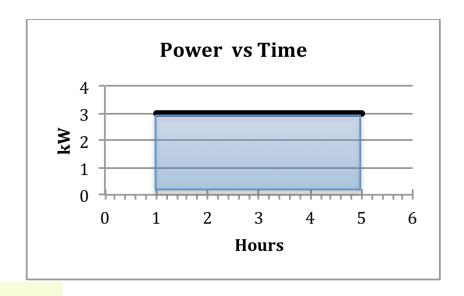
#### Your Usage Profile

Period	Usage	Avg Daily Usage	Days	Avg Daily Temp
Current Month	1,179	36.8	32	39
Last Month	1,519	47.4	32	42
Last Year	1,332	41.6	32	29

#### Units are kWh = Kilowatt hours

1. a. If a household is using 3 kW (kilowatt) of power continuously from 1pm to 5 pm (see Figure 1), how much energy is used?

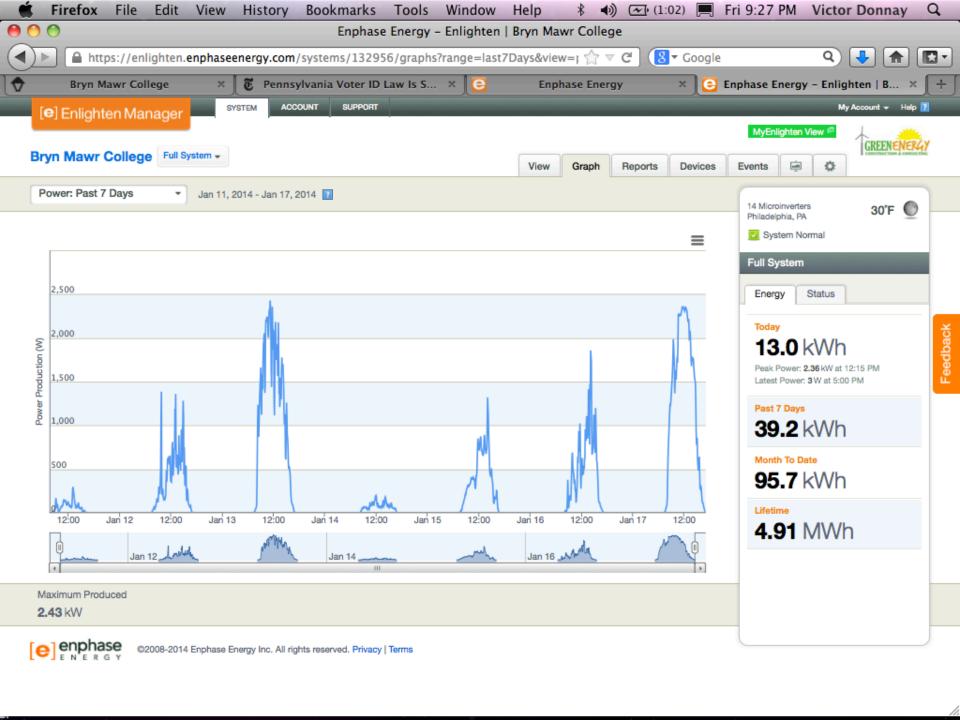
b. What is the area = height x width under the power curve for  $1 \le t \le 5$ ? Give the units for this area that you get by multiplying the units for the height by the units for the width.

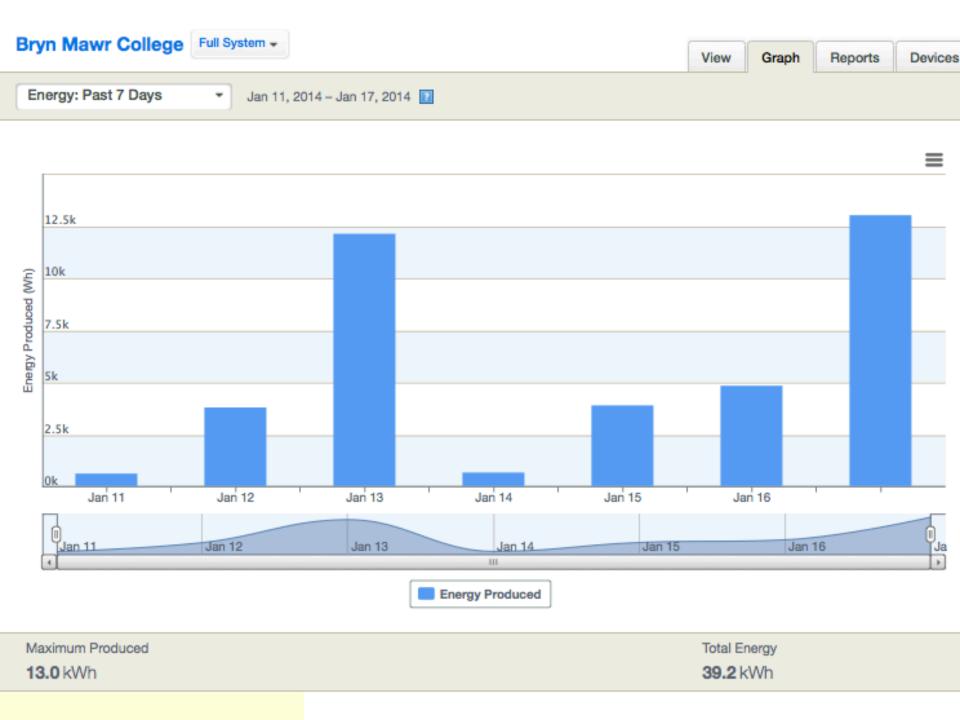


Solar Panels on Campus







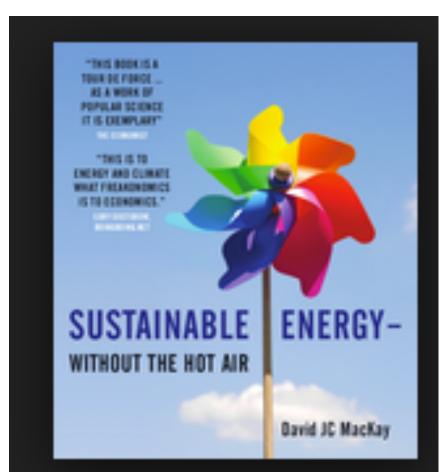


What is the relationship between power and energy? Given the power graph, how much energy is produced?



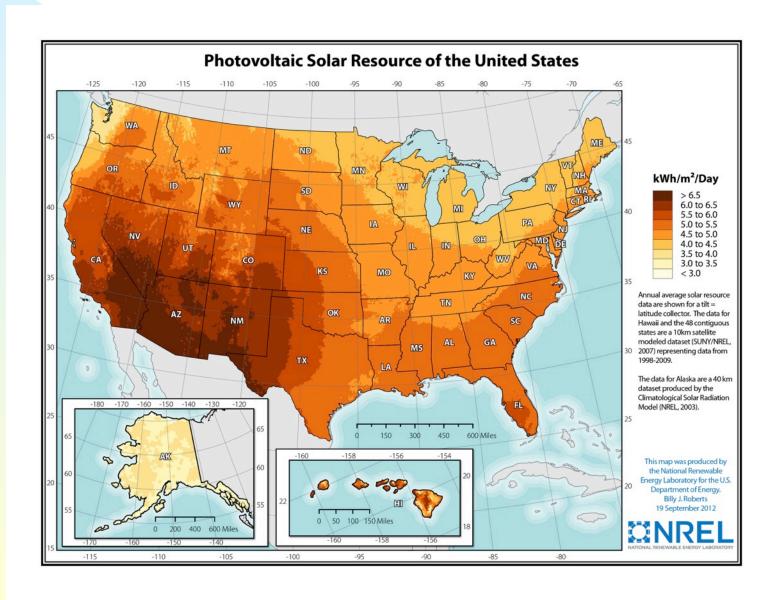
# Sustainable Energy without the Hot Air David JC MacKay

Can we meet our energy needs using renewables?



http://www.withouthotair.com/

#### National Renewable Energy Lab (NREL):www.nrel.gov/gis/solar.html



# Student Mini Presentations

## **Dockless Bike Sharing - Sustainable or Not?**

#### Charlotte Lin

- Start in San Diego in Feb & spread in North County coastal communities
- Short-term rentals based on phone app.
- Can pick up in one and leave is anywhere else within the company's service area.
- Reduce pollution & encourage more people to get out of their vehicles and exercise

#### However

- Parked bikes blocking busy sidewalks
- Riding illegally on the sidewalks
- People riding without helmets
- The idea began in China, where it spreads rapidly to more than 200 cities
- Large markets have become saturated with the service



Xiamen, Fujian province, China, on December 13, 2017.

https://www.theatlantic.com/photo/2018/03/bike-share-oversupply-in-china-huge-piles-of-abandoned-and-broken-bicycles/556268/

http://www.sandiegouniontribune.com/communities/north-county/sd-no-bike-share-20180305-story.html



### Dutch Supermarket Introduces Plastic-Free Aisle



## South Korea Reduces Capital Food Waste



Separating food waste from garbage waste is required by law





#### World Hacks: A surprising new afterlife for chewing gum

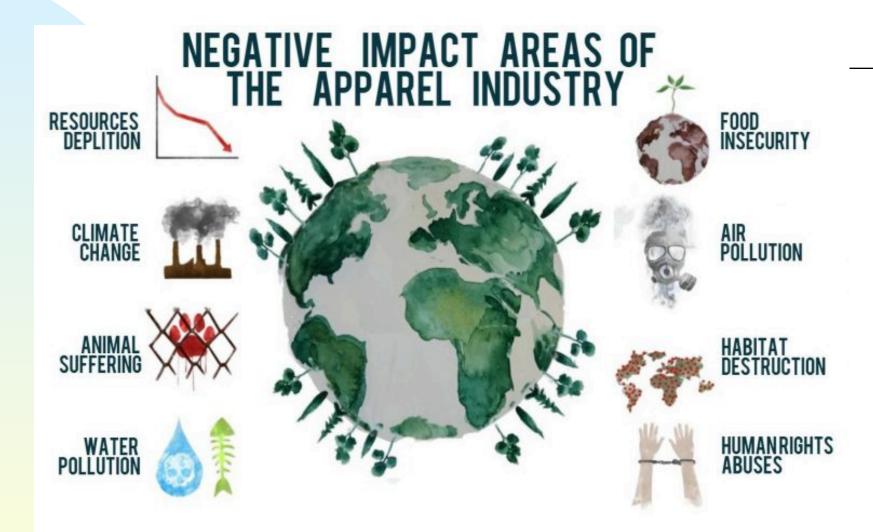
#### http://www.bbc.com/news/stories-43198104

- The second most common street litter
- UK spends £50m each year cleaning up gum
- Anna Bullus, founder of Gumdrop, is trying to reuse chewed gum and transform it into meaningful things, such as boots, phone covers, and packaging











# PUBLIC USES IN TRASH: NEW YORK'S NEWEST NATURAL WONDER





Who had the great idea of putting this park on a capped landfill?

http://www.mathaware.org/mam/2013/

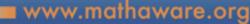
Mathematics Awareness Month - April 2013

# Mathematics of Sustainability



Balancing needs and seeking solutions for a complex changing world

To learn more about the connections between mathematics and sustainability, vis-





Joint Policy Board for Mathematics: American Mathematical Society, Mathematical Association of America, Society for Industrial and Applied Mathematics, American Statistical Association

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## TED Ed

http://ed.ted.com/lessons/is-our-climate-headed-for-mathematical-chaos-victor-j-donnay#review

# Is our climate headed for a mathematical tipping point?



# Service/Community Based Learning Sustainability Projects (Praxis)

**Mechanics** 

**Finding Projects** 

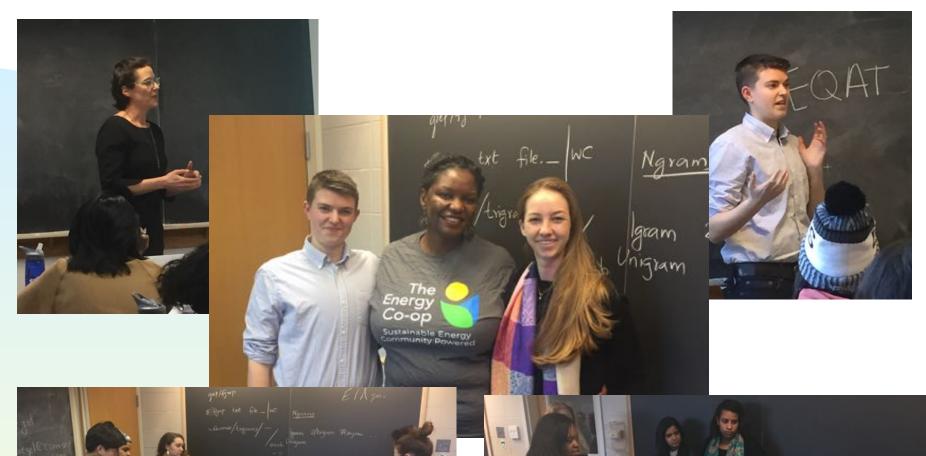
Student voice in selecting their project

Managing Expectations

Linking to learning goals

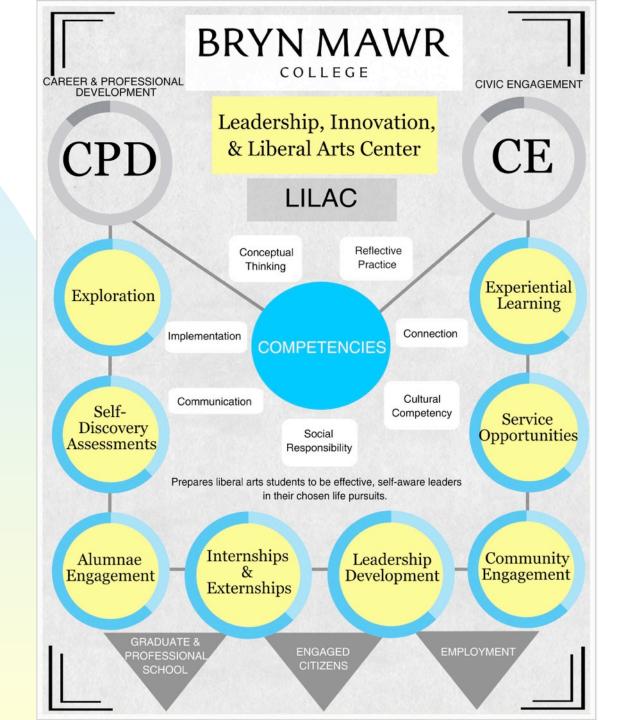
Keeping track of student progress

Final presentation/ report









### Sustainability Service Learning Projects (Praxis)

#### College Partners

#### **Dining Services:**

Trays in dining hall Composting Freight Farming\*

#### Facilities Department

Trash audits

Landfill or Incinerator

Energy savings in buildings from conservation mode

Pay back time for LED bulbs

On/Off switch for Chemistry hoods

Energy footprint for Science building renovation

#### **Admissions Office**

- Paperless admissions system

### Sustainability Service Learning Projects (Praxis)

### **Community Partners:**

Energy efficiency at Retirement Center

Math education materials on recycling for School District

Storm water management via rain gardens\*

EQAT social action: social cost of carbon\*

### Local Governments

Alternative energy system for township recreation center
Level of safety analysis for bike routes
Which city owned buildings would be best candidates for solar
panels? \*

### **Businesses:**

Comcast: Electric service vans – home garaging or central garage?\*

# Freight Farm Team: Justification of Purchase



Goal: Produce a cost benefit analysis for a Freight Farm to present to the college. Through out analysis, freight farm will make Bryn Mawr a socially responsible presence in the community in a way that well rewards the initial purchase.



## Watershed Project To reduce flooding, build rain gardens!







"The social cost of carbon is specifically focused on measuring what is the economic and health damage of emitting one more ton of carbon,"

Erin Stojan Ruccolo, Director of electricity markets for Fresh Energy.

**EQAT: The Social Cost of Carbon** 

Cost of carbon: \$40/metric ton

31% coal, 31% natural gas, 4% renewables plus nuclear

Social cost in the decade 2025-2035: \$6.5 billion

Increase renewables to 20%, decrease coal: \$2.9 billion

Savings: \$3.5 billion



Solar Team

Situation: Office of Sustainability in Philadelphia wanted to know which buildings would be the best for installing solar panels.

Which city owned buildings would be best candidates for Solar panels?



Solar Team

Situation: Office of Sustainability in Philadelphia wanted to know which buildings would be the best for installing solar panels.

#1 building, the Philadelphia Detention Center, could produce a savings of \$170,000 per year in electricity costs.

#### Comcast Team

#### Problem:

Comcast Corp. is considering replacing its gasoline-fueled vans with electric vans in its technician fleet, in order to adopt more sustainable corporate practices.

#### Our Project:

Conducting cost & benefit analysis for owning a gasolinefueled fleet vs. an electric-fueled fleet in two parking scenarios: technician home garaging, and Comcast office garaging.

#### Solution:

A 30-year lifetime cost model and Net Present Value (NPV) calculation for each scenarios.





Cost to operate a gas powered vehicle: \$3,247/yr

Electric vehicle: \$672/yr

### **Student Reaction**

"I liked that the projects we worked on were meaningful and that this course was extremely applied in nature. It was nice to do something that affected our college and/or community directly"

"The end results of all the projects were pretty satisfying; it made you feel like you were making a contribution and that you might actually be able to affect something."

### Quantitative Reasoning, Math Modeling

"the math involved in most of these applications was pretty basic"

"... there were more numbers than mathematics involved in our projects."

Using Sustainability to Incorporate Service-Learning Into a Mathematics Course: A Case Study, Victor Donnay, PRIMUS, Volume 23, Number 6, 1 May 2013, pp. 519-537(19)

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Best math senior conference everrr! - with Sebastian Tilson, Tapashi Narine, Alisha Pradhan, Hoang Ha, Victor Donnay, Lynne Ammar, Julia Yoo, Wendy Shengyun Huang, Linda Yoo and Dorothy Shu.

Tag Photo

Add Location

Like · Comment · Stop Notifications · Share

Alisha Pradhan, Lynne Ammar and Linda Yoo like this.

2 shares



Lynne Ammar Thanks Julia Iol December 12, 2012 at 12:59am · Like



Wendy Shengyun Huang A great semester

December 12, 2012 at 10:31am · Like

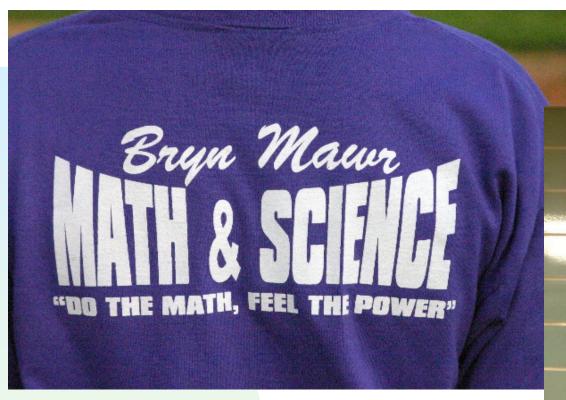


Yashaswini Singh This has been my favorite math class in all 4 years! :')

December 12, 2012 at 1:27pm · Like · △3







2012 AMS Exemplary
Department Award



## 2012 AMS Exemplary Department Award



### Haverford 2011

## Recreation and Environmental Education Center



### Math and Sustainability:

### **Cost** – Benefit Analysis for Commissioners

Bethany Giblin, Amy Veprauskas, Jenny Sichel, Teresa Palasits









#### **PROCLAMATION**

WHEREAS: the Board of Commissioners takes great pride in recognizing those people who perform outstanding contributions for the good of the township and its residents; and

WHEREAS: the Community Recreation Environmental Center will be a showcase for the residents of Haverford Township for many years, contributing to residents' health; as well as educating the residents about ways to preserve the environment and appreciate nature; and

WHEREAS: the Board of Commissioners adopted a Climate Action Plan in 2008 to serve as a model of leadership in reducing the carbon footprint in the township, and this past June, approved that a geothermal system be included in the design of the Community Center; and

WHEREAS: Katie Link and Yufan Wang, students at Bryn Mawr College, worked diligently under the direction of Professor Victor Dunnay in assisting Tim Denny to make the deadline in successfully applying for a \$300,000 grant from the Pennsylvania Energy Department Authority, to help fund the geothermal system - which will save over \$2 million dollars in energy costs; as well as greatly reducing the carbon footprint over the lifetime of the building.

NOW, THEREFORE BE IT PROCLAIMED, that the Board of Commissioners wish to formally thank Katie Link and Yufan Wang and acknowledge their extraordinary effort on this project and wish them every success as they continue their life's pursuits.

TOWNSHIP OF HAVERFORD

BY: WILLIAM F. WECHSLER

President

Attest: Lawrence J. Gentile

Township Manager/Secretary

### Sustainability Projects for Math Senior Seminar

- Trays in dining hall
- Energy savings in buildings from conservation mode.
- Pay back time for LED bulbs.
- Paperless admissions system
- Level of safety for bike routes
- On/Off switch for Chemistry hoods.
- Composting
- Trash audits
- Alternative Energy for recreation center

### Mathematics Awareness Month 2013

On Aug 30, 2012, at 8:00 AM, Robert Daverman, AMS Secretary wrote:

Dear Professor Donnay,

I am writing with hopes of interesting you in chairing the Advisory Committee for next year's Math Awareness Month. The theme will be "Mathematics and Sustainability"

### Mathematics Awareness Month 2013: The Mathematics of Sustainability

http://www.mathaware.org/mam/2013/

Essays at: <a href="http://www.mathaware.org/mam/2013/essays/">http://www.mathaware.org/mam/2013/essays/</a>

Sustainability Counts! Educational materials:

http://www.mathaware.org/mam/2013/sustainability/

### **Teaching Units:**

- CO2 levels
- Artic Sea Ice
- Solar Panels

Other Resources: <a href="http://www.mathaware.org/mam/2013/related/">http://www.mathaware.org/mam/2013/related/</a>

## The Practical, the Sublime, and the Sinister by David Shiller, Lighting Solution Development

"Why do we have a global environmental crisis? How did humanity get to this point? The deeper I dug, the more philosophical the issues became...."

Turning Point by Fritjof Capra

Descarte: Rationalist, mechanistic, and reductionist thinking

Mathematical ideas shape our worldview of man as separate from and above nature.

Our mathematics is a direct contributor to the global environmental crisis.

## Descarte "I think, therefore I am"

## Descarte "I think, therefore I am"

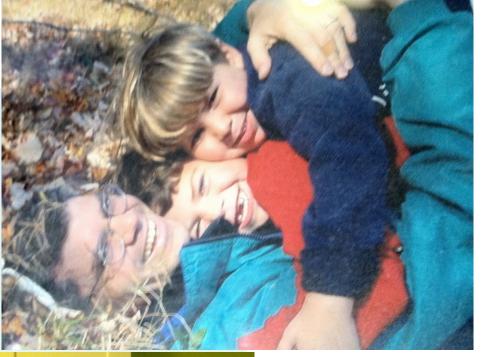
Holistic View
"We are connected to each other and to the earth, therefore we are"

### Think, Pair, Share

What do you love about nature and the environment?

## 2012 AMS Exemplary Department Award













## Math to Life Connections Final Project Multivariable Calculus

Take some topic in the world in which you are interested and some topic from our course and show how they are connected.

Thanks to Mrs. Jane Scanlon, Coopertown Elementary School, 1<sup>st</sup> grade teacher.

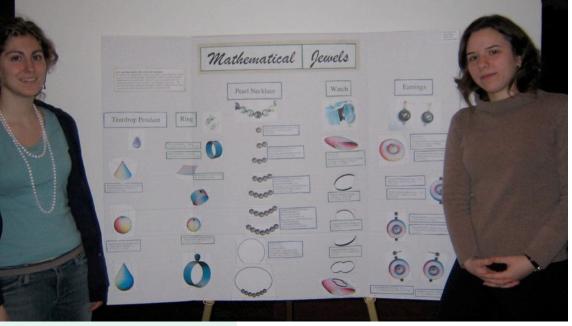
**Everyday Math Program** 

















### REU Summer Program

### REU Summer Program

## Research Experience for Undergraduates

### TEU Summer Program

### TEU Summer Program

Teaching Experience for Undergraduates

### REU Summer Program

## Teaching Experience for Undergraduates

Summer 2016:

Math Education at Brown University

Science Education at Trinity University

## How People Learn: Brain, Mind, Experience, and School

National Academy of Science Washington, D.C.

Three Key Principles

## How People Learn: Brain, Mind, Experience, and School

National Academy of Science Washington, D.C.

Three Key Principles

0. To learn, people need to be interested and motivated.

#### The New Science of Learning

#### Three Fundamental Principals of Learning

### Key Findings

1. Students come to the classroom with preconceptions about how the world works. New understandings are constructed on a foundation of existing understandings and experiences. If their initial understanding is not engaged, students may fail to grasp the new concepts and information that are taught, or they may learn for purposes of a test but revert back to their preconceptions outside the classroom.

### Implications for Teaching

1. Teachers must draw out and work with the preexisting understandings that their students bring with them including misconceptions.

#### The New Science of Learning

Three Fundamental Principals of Learning

### Key Findings

2. To develop competence in an area of inquiry, students must (a) have a deep foundation of factual knowledge, (b) understand facts and ideas in the context of a conceptual framework, and (c) organize knowledge in ways that facilitate retrieval and application.

### Implications for Teaching

matter in depth, providing many examples in which the same concept is at work and providing a firm foundation of factual knowledge. Teachers should help students organize their knowledge into a coherent structure using key concepts.

#### **The New Science of Learning**

Three Fundamental Principals of Learning

Key Findings	Implications for Teaching	
3. A "metacognitive" approach to instruction can help students learn to take control of their own learning by defining learning goals and monitoring their progress in achieving them.	3. The teaching of metacognitive skills should be integrated into the curriculum in a variety of subject areas.	

### 3 Key Principals of HPL

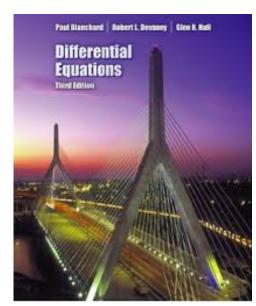
- 0. To learn, people need to be interested and motivated
- 1. Pre-existing knowledge, misconceptions, connect old and new knowledge
- 2. Factual knowledge organized around key concepts
- 3. Meta-cognition

# Applying Principles of How People Learn to our Teaching

- 1. How do we find out what students pre-existing knowledge/misconceptions are? How do we link new material to students' pre-existing knowledge?
- 2. What are the key concepts in the courses we teach? How can we determine if students have learned these key concepts?
- 3. How do we give students opportunities to think about their thinking?

### Differential Equations and Modeling

Blanchard, Devaney, Hall text
Dynamical Systems approach
Qualitative methods



Environmental/Sustainability applications

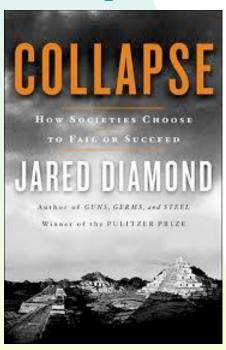
Population Growth

Bifurcations – Tipping Points

### Use Readings from Interesting Books

#### **Jared Diamond**

Collapse: How Societies Choose to Fail or Succeed.

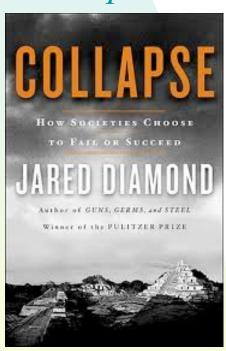


What links do you see to topics from our course?

### Use Readings from Interesting Books

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Collapse: How Societies Choose to Fail or Succeed.

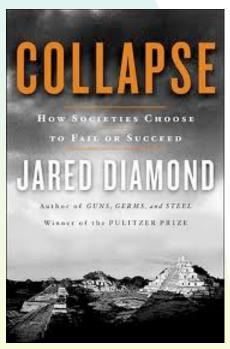


Rwanda: Genocide

### Use Readings from Interesting Books

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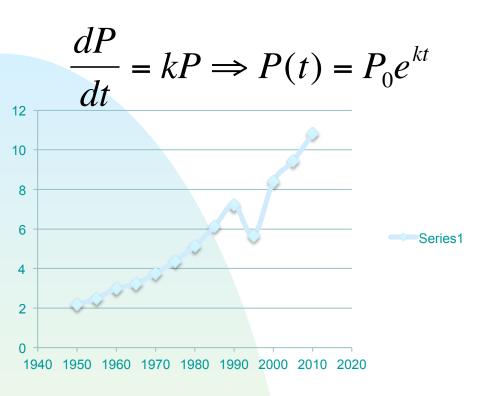


Rwanda: Genocide

Contributing factor: over-population

### Population growth: Exponential

$$\frac{dP}{dt} = kP \Rightarrow P(t) = P_0 e^{kt}$$



	Rwanda Population
Year	(millions)
1950	2.186
1955	2.485
1960	2.993
1965	3.233
1970	3.754
1975	4.359
1980	5.141
1985	6.113
1990	7.214
1995	5.664
2000	8.396
2005	9.429
2010	10.814

Population Growth (Wen Gao, BMC '07: Math and Social Justice Conference, Lafayette College 2006)

- 1. What does the book claim is the relative growth rate of the Rwanda population (k value)?
- 2. What would be the doubling time with this relative growth rate?
- 3. Looking at the population data table, calculate the relative growth rate (k) of population using the data from 1980 and 1985.
- 4. With this k value, predict Rowanda's population n in 1995. Does your prediction agree with the value given in the table? Discuss reasons for the difference.

### Population growth:

What are problems with the Exponential Model?

### Population growth:

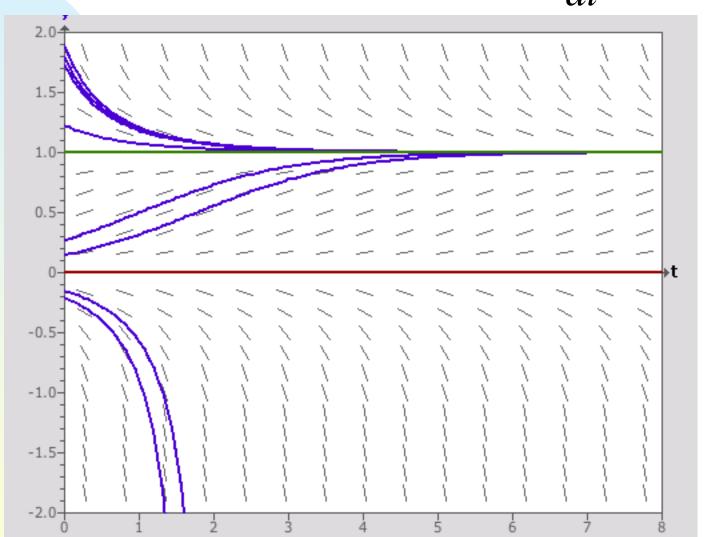
What are problems with the Exponential Model?

Logistic model – limits to growth Carrying capacity N

$$\frac{dP}{dt} = kP(1 - P/N)$$

### Logistic Population growth:

$$\frac{dP}{dt} = kP(1 - P/N)$$



Phase line

### Logistic Population growth with harvesting

"h" members of population harvested per year

$$\frac{dP}{dt} = kP(1 - P/N) - h$$

What types of populations can be "harvested"?

### Logistic Population growth with harvesting

"h" members of population harvested per year

$$\frac{dP}{dt} = kP(1 - P/N) - h$$

What types of populations can be "harvested"?





# Key Concept: Tipping Points = Bifurcations

## TED Ed

### TED Ed

Is our climate headed for a mathematical tipping point?

### Lead-in to Tipping Points

### Collapse



Easter Island

### Lead-in to Tipping Points

### Collapse



Easter Island

What factors contributed to the collapse of the society?

#### Fishbanks: A Renewable Resource Management Simulation



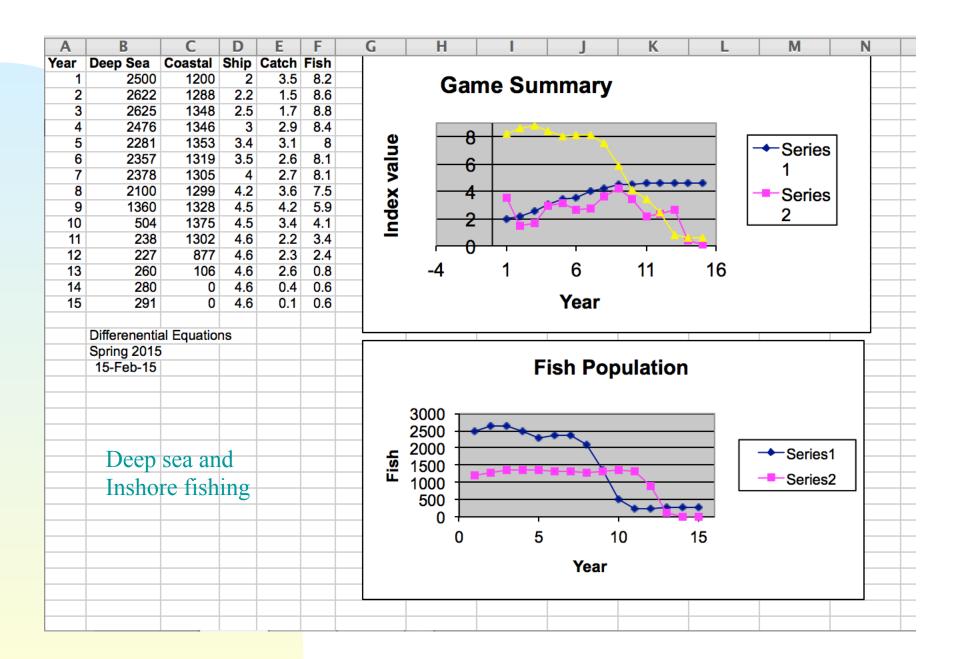
**DEVELOPERS**Dennis Meadows, John Sterman and Andrew King



#### Goal: Maximize your profit

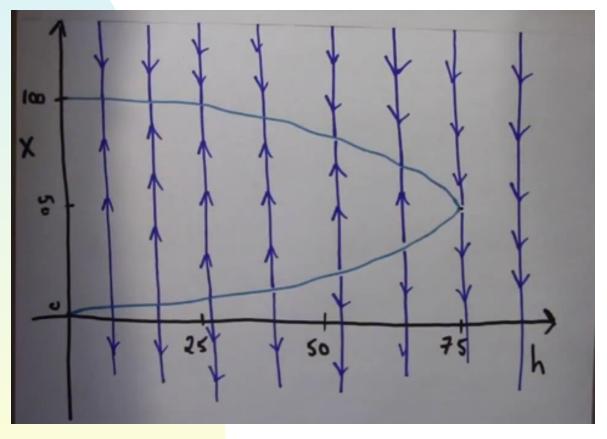






### Bifurcation Diagram

$$\frac{dP}{dt} = kP(1 - P/N) - h$$



Created by class via "jig-saw" exercise.

### Bifurcation – Tipping Point:

A small change in the condition of the system (parameter) can lead to drastically different outcomes.

Critical value  $h_{cr}$  of fishing/harvesting levels

If  $h > h_{cr}$  then the population will *crash* 

$$\frac{dP}{dt} = kP(1 - P/N) - h$$

"h" fish caught per year

#### Sustainability Improves Student Learning (SISL) http://serc.carleton.edu/sisl

Ben Galluzzo, Shippensburg University Corrine Taylor, Wellesley College

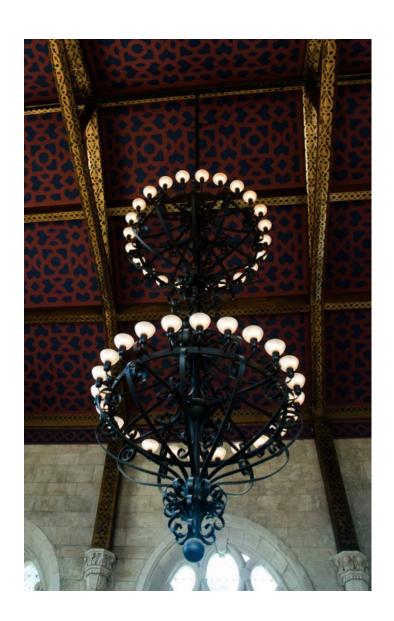




#### Replace CF bulbs with LED.







### Assignments:

II. a. Find article about mathematics in newspaper, on web. Post on class website; write a one paragraph summary.

b. Read three other posts and write comments.

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#### Math and Sustainability Summer Institute for Teachers

#### All materials from this institute available free at:

https://docs.google.com/document/d/1Ma9wYo83i10OLBf6R8WdYov0pd534n0yZbcObScYMUw/edit

	Basic 75	Energy   Smort	Phillips   LED
Brightness	1190	1500	1100
(lumens)	5700	4600	9060
Power.	75	90	17
(watts)	71	19	15
leat (°F)	<b>438</b>	159	88
Cost (5)	1	5	40
[per bulb] Tubular f	120066	10pm ks	50,000 112
Tubular f	luoresci	ent bu	1bs (3)
icie measu	wed to	r near	output
hesult: 12 further Inv surface area	7°F,	\$ a.50	per bulb
surface aced	(flux)	bright	ress w more
	- (TIME)	control	5.



Is it "worth it" to change bulbs?







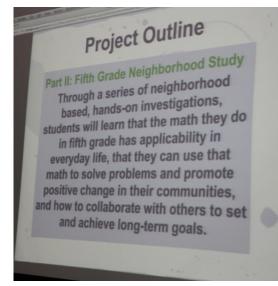


#### Math and Sustainability Summer Institute for Teachers















### Workshop: Engaging Mathematics

Victor Donnay, Bryn Mawr College, Brainstorming lessons around recycling and trash to support Philadelphia SD

Tony Dunlap, Normandale Community College, Math Modeling in a "Math for Liberal Arts" course. Lake volumes, creek flow, storm water runoff

Cathy Evans, Barbara Gonzalez, Roosevelt University, College Algebra: Modeling the Chicago Homicide Rate

Alioune Khoule, Mangala Kothari, Marina Nechayeva, LaGuardia Community College,

Elementary Statistics: Learning concepts through social and environmental issues.

- 1. Demographics of my class, my college and my neighborhood
- 2. Global warming
- 3. Basal Metabolic Rate (BMR)

Frank Wattenberg, United States Military Academy,
Data analysis courses at all levels. Keeling Atmospheric Carbon Dioxide
Concentration Data to Practice Data Fitting and to Tell a Cautionary Tale About Using Data Fitting for Prediction.

#### Summary

Launch lesson/unit by connecting to students' previous experience

Give up control

Trust the students and their natural love of learning

Let students have voice – power of student voices to bring about change

Use real data

Link classroom learning with student action

Bring your whole self to the classroom

"If you want to build a ship,
don't drum up people to collect wood and
don't assign them tasks and work, but rather
teach them to long for the endless immensity
of the sea."

Antoine de Saint-Exupéry
As cited in *A Mathematician's Lament* 

Thanks Ellie Goldberg, Brown Summer HS Program

Any object not interesting in itself may become interesting through becoming associated with an object in which an interest already exists. The two associated objects grow, as it were, together: the interesting portion sheds its quality over the whole; and thus things not interesting in their own right borrow an interest which becomes as real and as strong as that of any natively interesting thing.

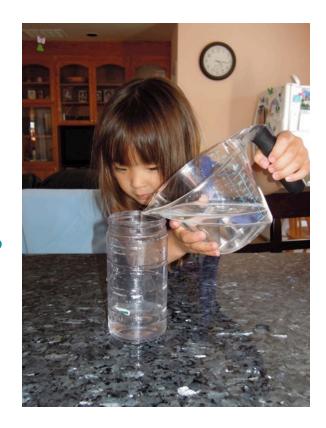
William James, Talks to Teachers, 1899.

http://www.uky.edu/~eushe2/Pajares/tt10.html

Thanks David Burns, SENCER

### Related Rates:

1. A cylindrical tank with radius 5m is being filled with water at a rate of 3m³/min. How fast is the height of the water increasing?





Real World: How fast is sea level rising if the ice in Greenland is melting at a rate of 195 km<sup>3</sup>/year

2. Airplane A is going east at 420 mph.
Airplane B is going north at 375 mph. How fast are they moving apart from one another.



#### Real World:

Consider two children born to families in different socio-economic groups. One child is born into a middle class family; one into a working class family. The vocabulary of the child with the middle class parents increases at 350 words per year. The vocabulary of the child with working call parents increases at 150 words per year. At what rate is the difference in the size of their vocabularies growing?



### Math and Sustainability

- Interdisciplinary topic.
- Authentic issue facing the world.
- Opportunities for Community Based/Service Learning

### Assignment:

**Connections Paragraphs:** 

Take a HW problem and describe how the mathematics involved might be used to address a real world problem.

Post your paragraph on Blackboard. Read three other students' posts.

Calculus 1 and 2.

## What are students interested in?

## What are students interested in?

Ask them!

# SUSTAINABLE BY DESIGN



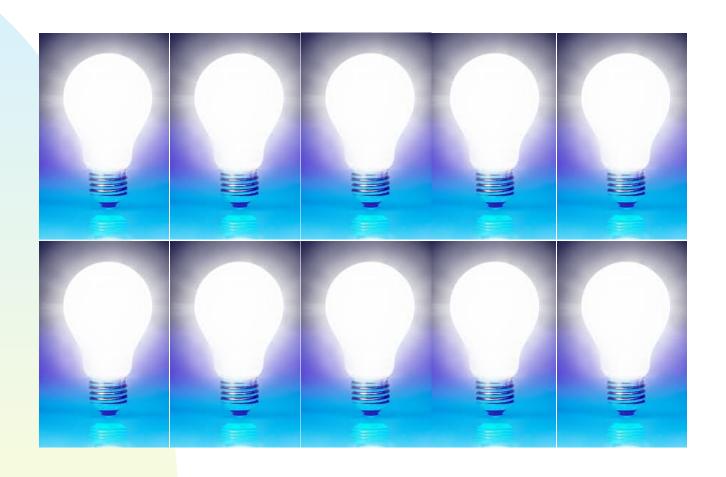
#### Examine Lesson Plan about Solar Energy

100 watt

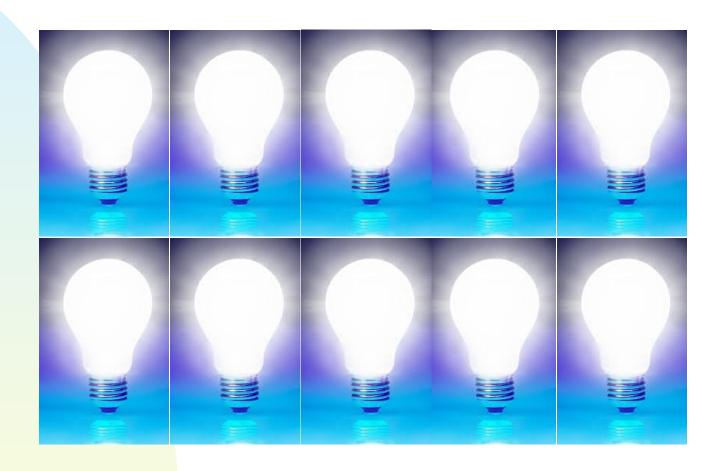


Power

 $10 \times 100 \text{ watt} = 1000 \text{ watts} = 1 \text{ kw} = 1 \text{ kilowatt}$ 



#### $10 \times 100 \text{ watt} = 1000 \text{ watts} = 1 \text{ kw}$



Lights on for 5 hours:

Energy used = 1 kw x 5 hours = 5 kw-hours = 5 kwh

# Key Concept of the Lesson

# Key Concept of the Lesson Integration

## Key Concept of the Lesson

Integration

How People Learn:
Brain, Mind, Experience, and School

National Academy of Science Washington, D.C.

Free online

#### Additional References:

How People Learn: **Brain, Mind, Experience, and School,** National Academies Press, <a href="http://www.nap.edu/openbook.php?isbn=0309070368">http://www.nap.edu/openbook.php?isbn=0309070368</a>

Sustainable Energy – Without the Hot Air, David JC MacKay, <a href="http://www.withouthotair.com/">http://www.withouthotair.com/</a>

Great book that does all types of interesting calculations to model the potential for scaling up renewable energy use to a national scale. Only requires high school math.

The materials from Mathematics Awareness Month 2013 – Mathematics and Sustainable are archieved and available at:

http://www.mathaware.org/mam/2013/

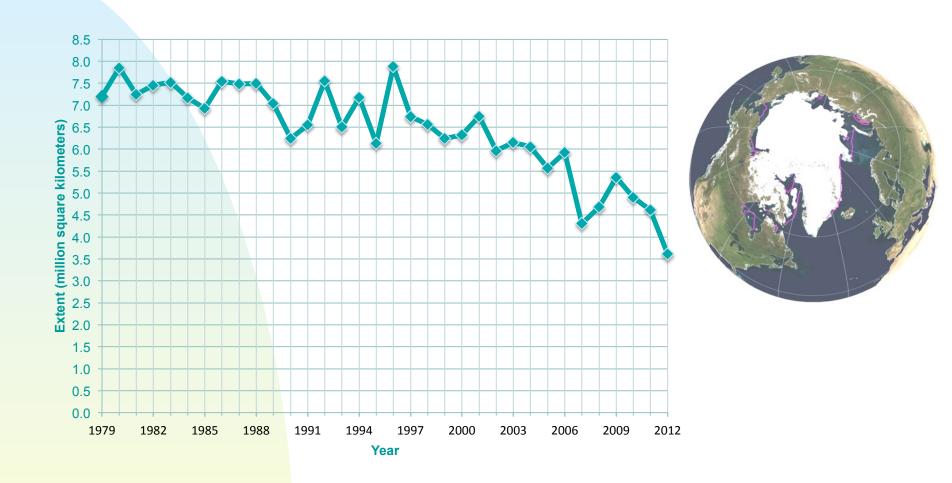
Essays at: <a href="http://www.mathaware.org/mam/2013/essays/">http://www.mathaware.org/mam/2013/essays/</a>

Sustainability Counts! Educational materials:

http://www.mathaware.org/mam/2013/sustainability/

Other Resources: <a href="http://www.mathaware.org/mam/2013/related/">http://www.mathaware.org/mam/2013/related/</a>

#### Curve Fitting: When will the Artic be ice free in summer?



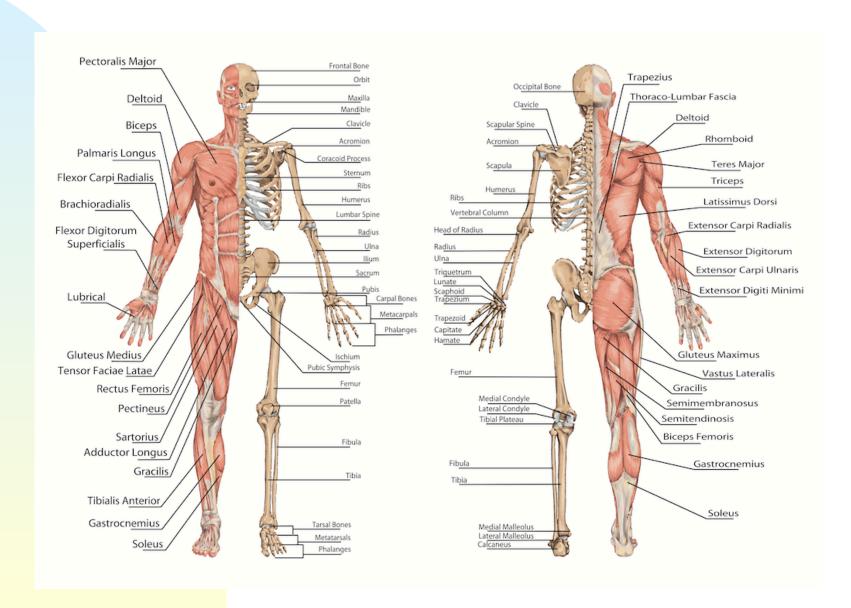
All images courtesy of NASA and the National Snow and Ice Data Center, U.C., Boulder. (<a href="http://nsidc.org">http://nsidc.org</a>). Lesson plan by William Bauldry, Appalachian State University, Victor Donnay, Bryn Mawr College, Thomas J. Pfaff, Ithaca College.

#### What the Best College Teacher Do

Ken Bain

**Teaching Anatomy** 

## **Teaching Anatomy.**



## Teaching Anatomy.

