

# Diversity of shapes



# How do complex shapes form?



Heart



Lungs



Liver



Bladder



Spleen



Large  
Intestine



Small  
Intestine



Gallbladder



Pancreas



Stomach



Kidneys

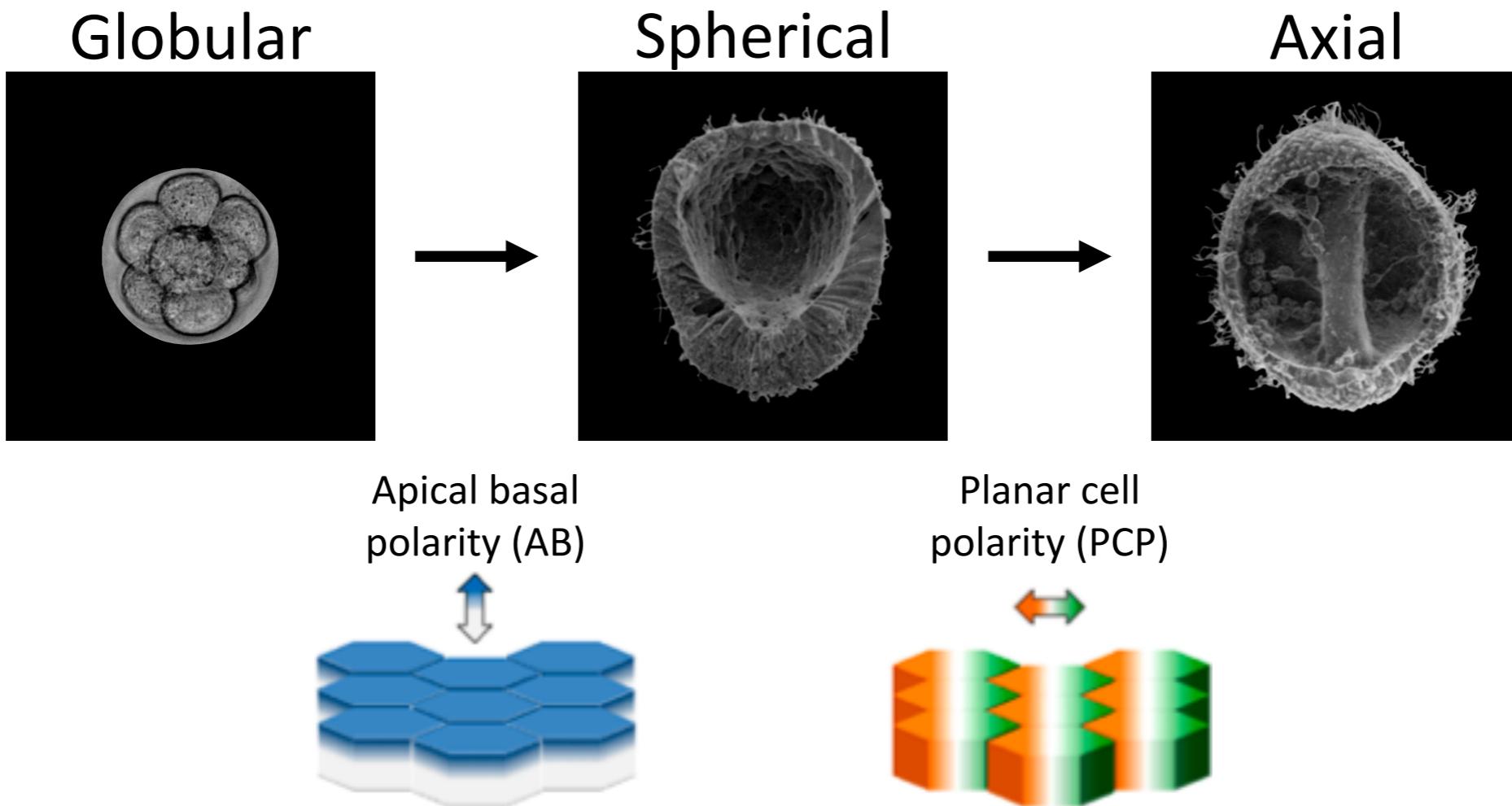


Uterus

All organs have an inside-outside and a given flow direction

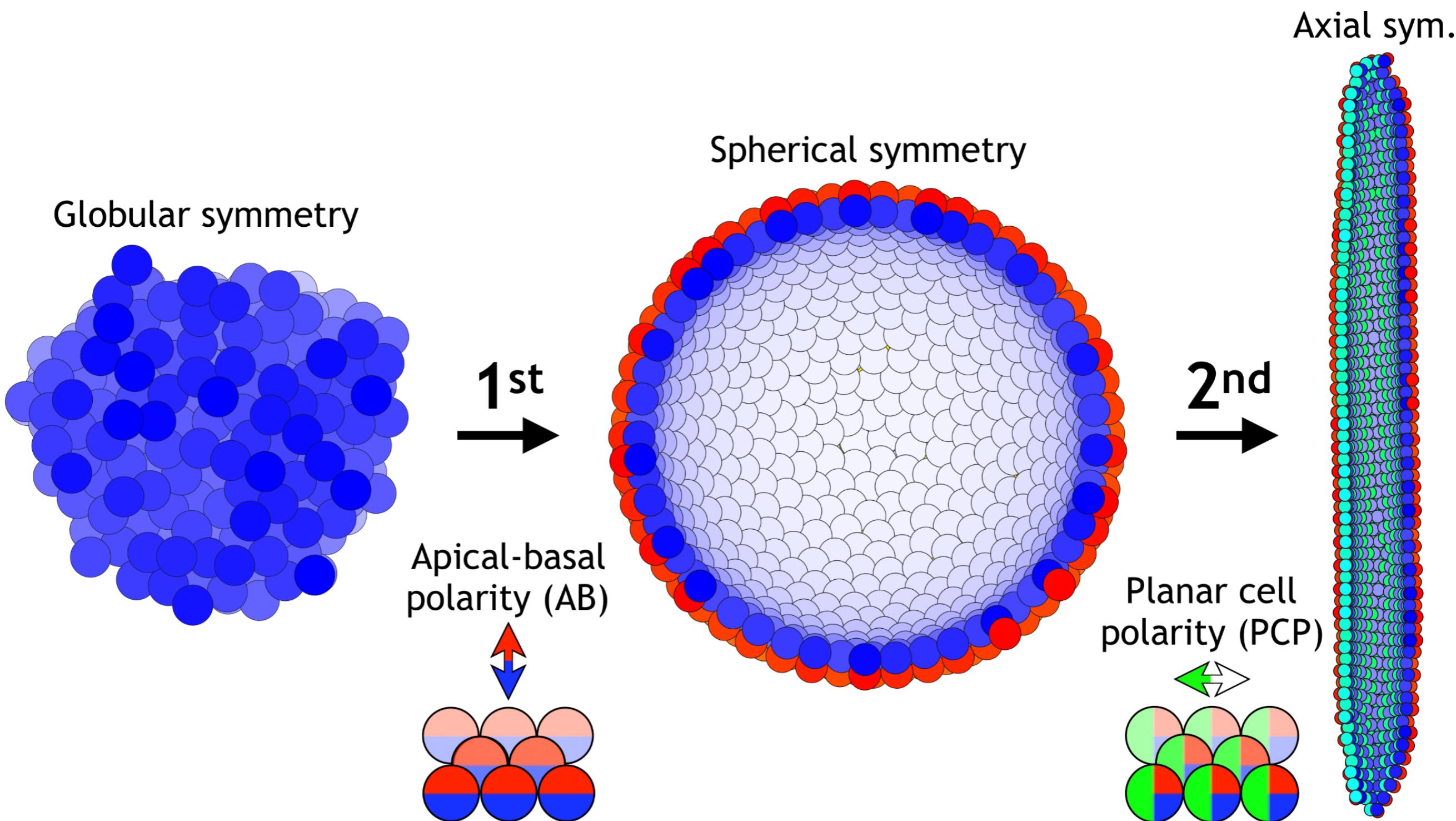
# General pattern in organogenesis?

Two symmetry breaking events:



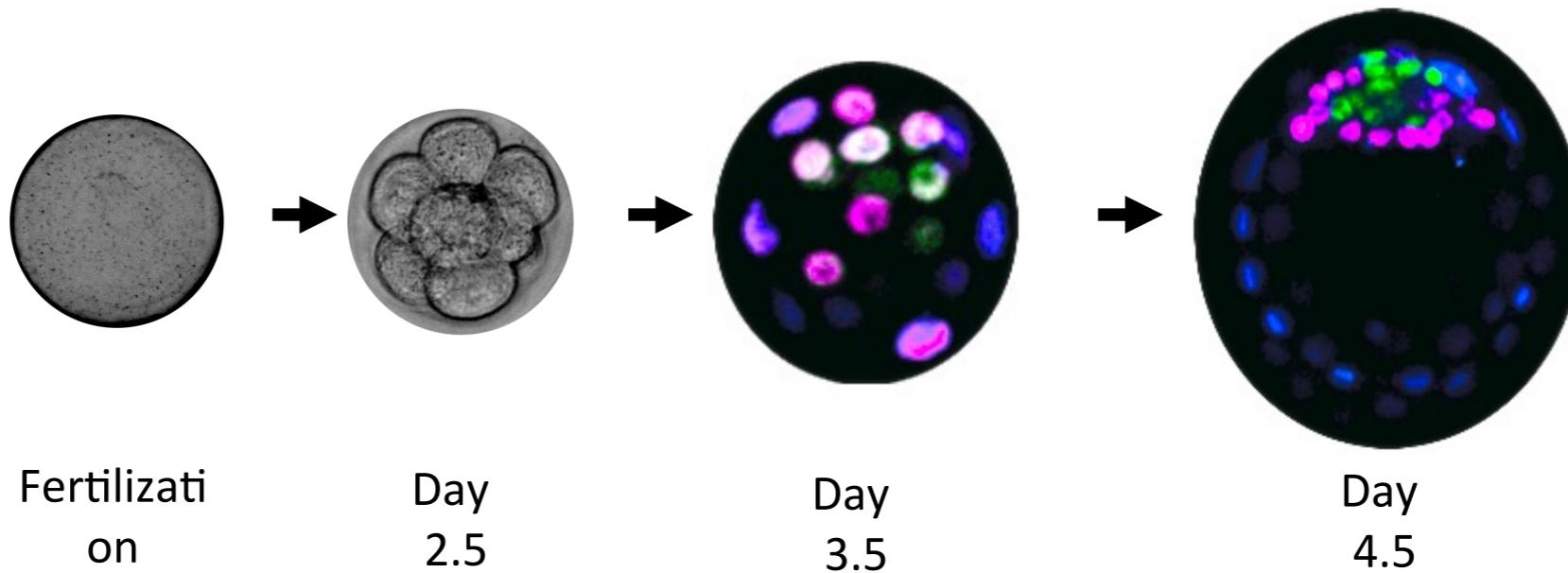
Is this sufficient for organogenesis?

# Symmetry breaking events in Life:

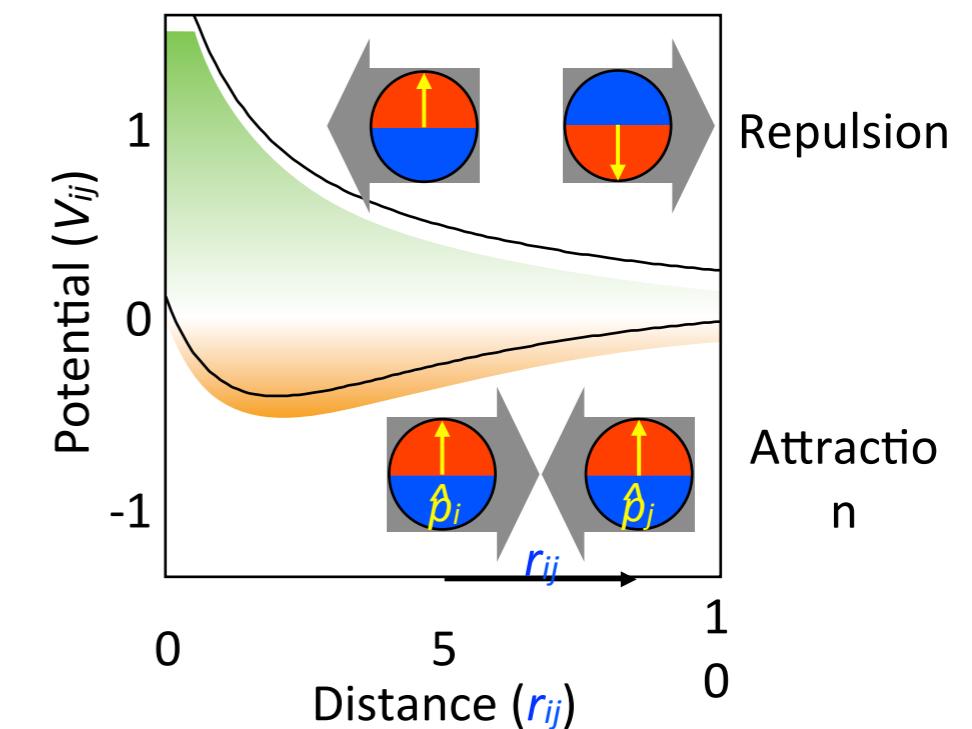
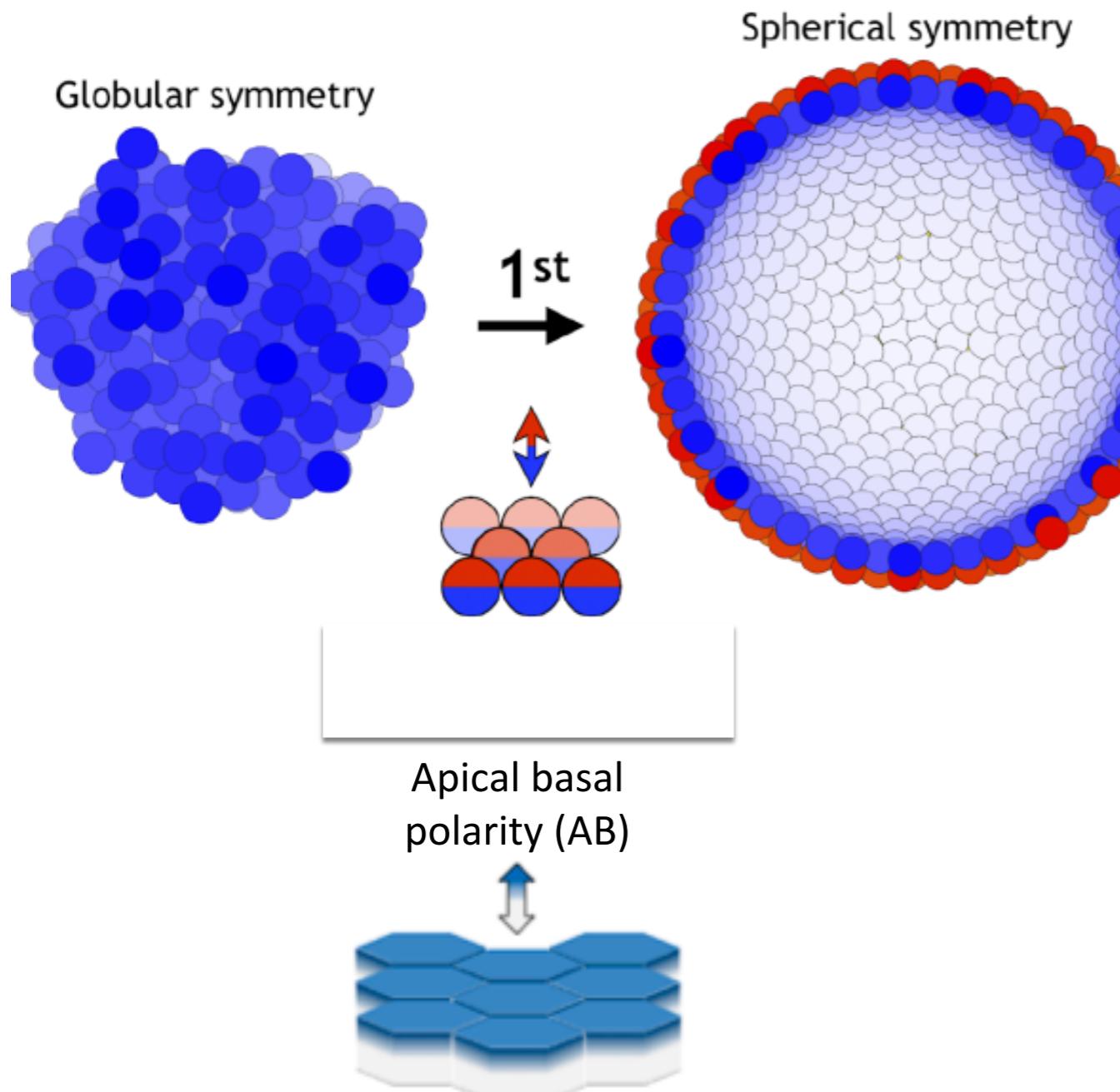


*Planes (spheres) respectively Tubes (torus)*

# 1) Formation of Blastocyst



# AB polarity (sheets):



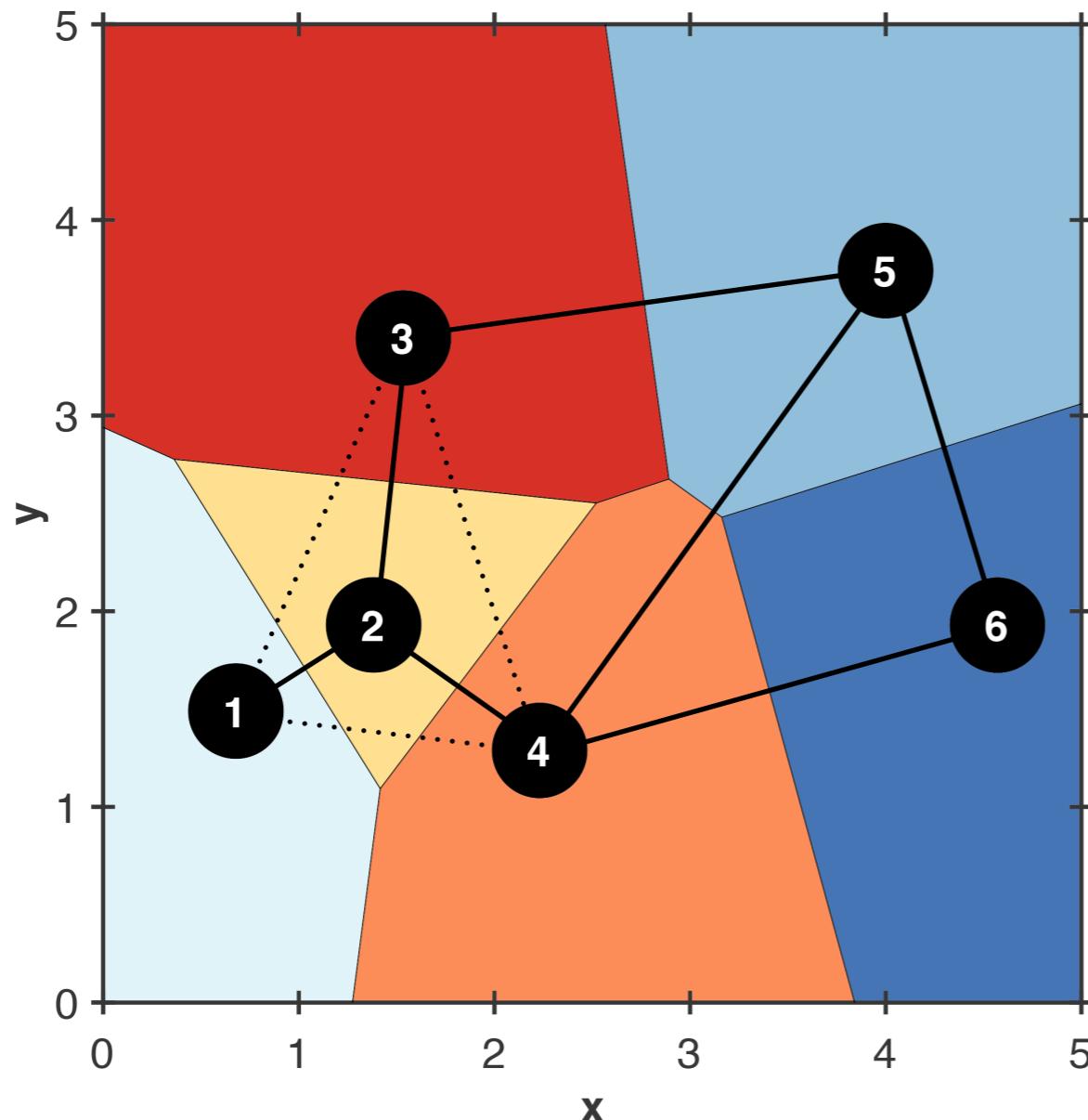
Epithelial sheet

$$S_1 = (\hat{p}_i \times \hat{r}_{ij}) \cdot (\hat{p}_j \times \hat{r}_{ij})$$

$$V = \exp(-r_{ij}) - S_1 * \exp(-r_{ij}/5)$$

# Interacting neighbors

Who interact?



$$V_i = \sum_j V_{ij}$$

$$\frac{d\vec{r}_i}{dt} = -\frac{dV_i}{d\vec{r}_i} + \eta$$

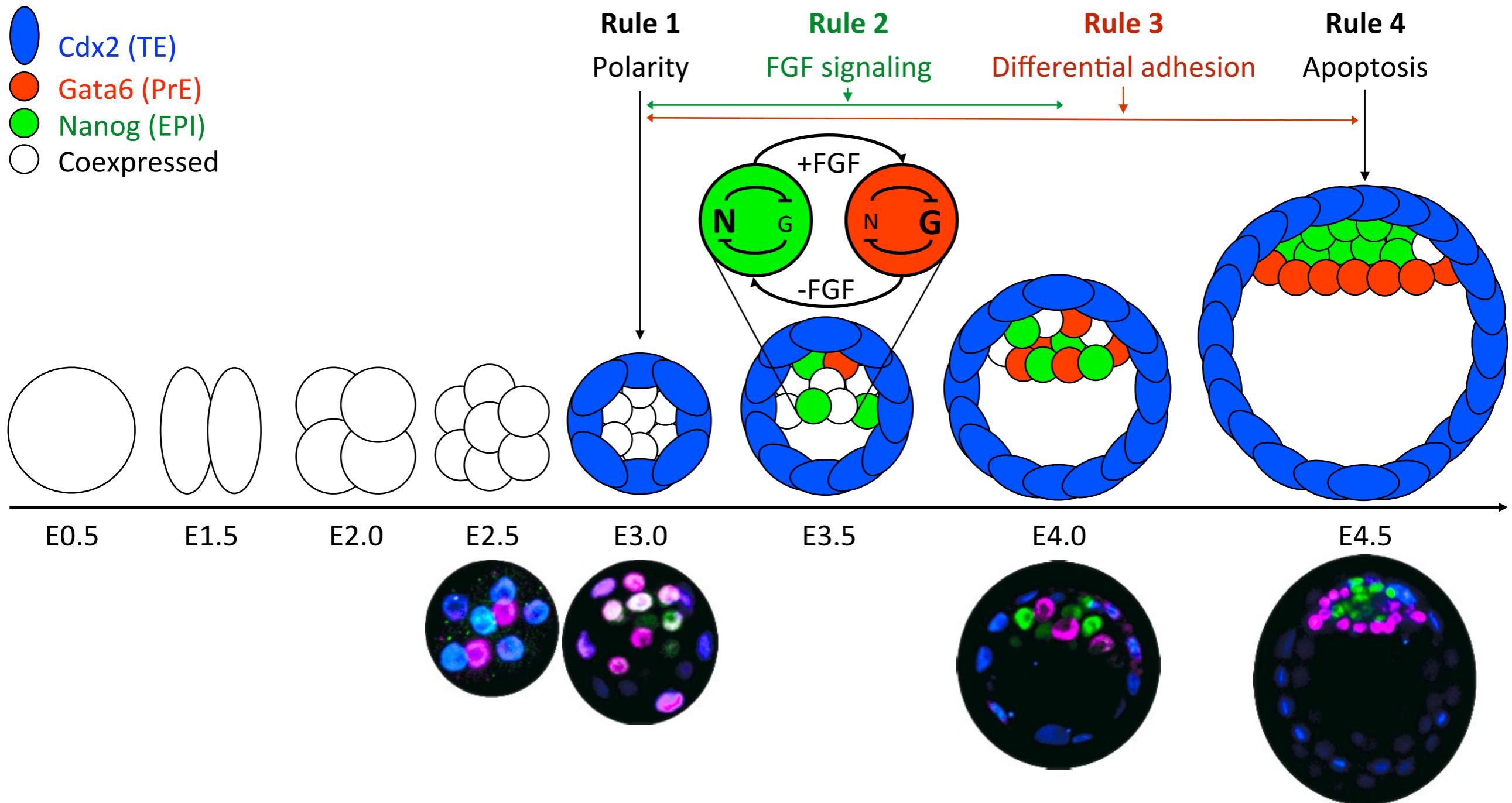
$$\frac{d\vec{p}_i}{dt} = -\frac{dV_i}{d\vec{p}_i} + \eta$$

$$\frac{d\vec{q}_i}{dt} = -\frac{dV_i}{d\vec{q}_i} + \eta$$

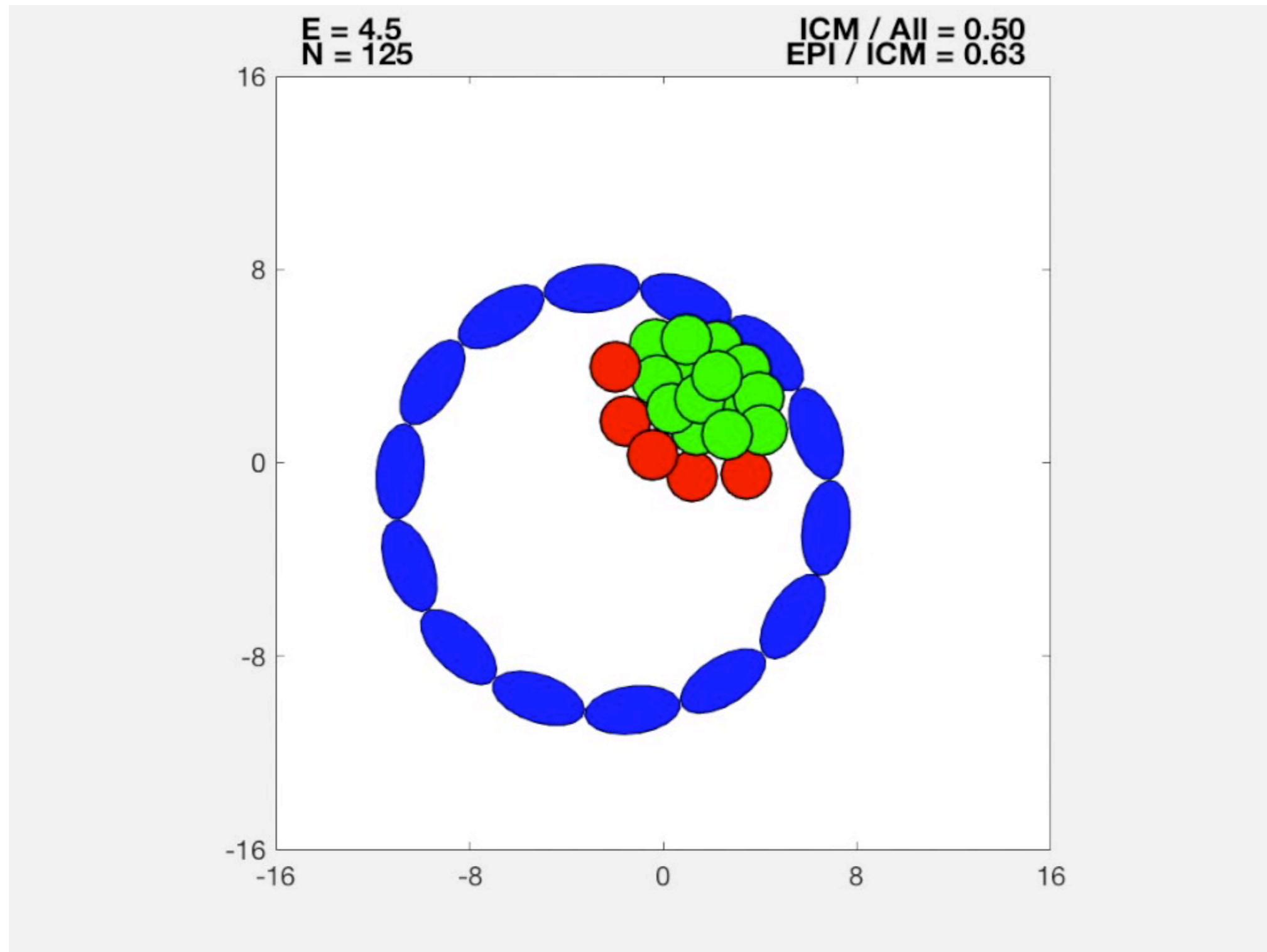
Solid lines do, dashed do not

# Four simple rules for early embryonic development

-  Cdx2 (TE)
-  Gata6 (PrE)
-  Nanog (EPI)
-  Coexpressed



# Four simple rules for early embryonic development

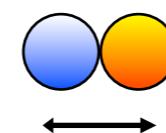


## 2) Playing with AB polarity..... ....:

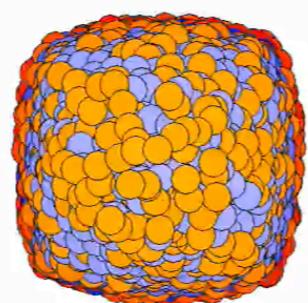


# Compact aggregate unfolds

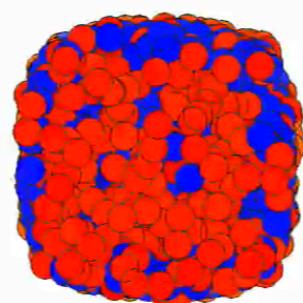
Each cell



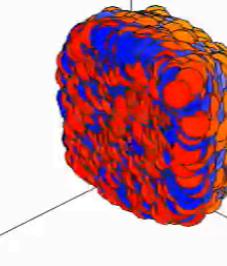
Outside



Inside

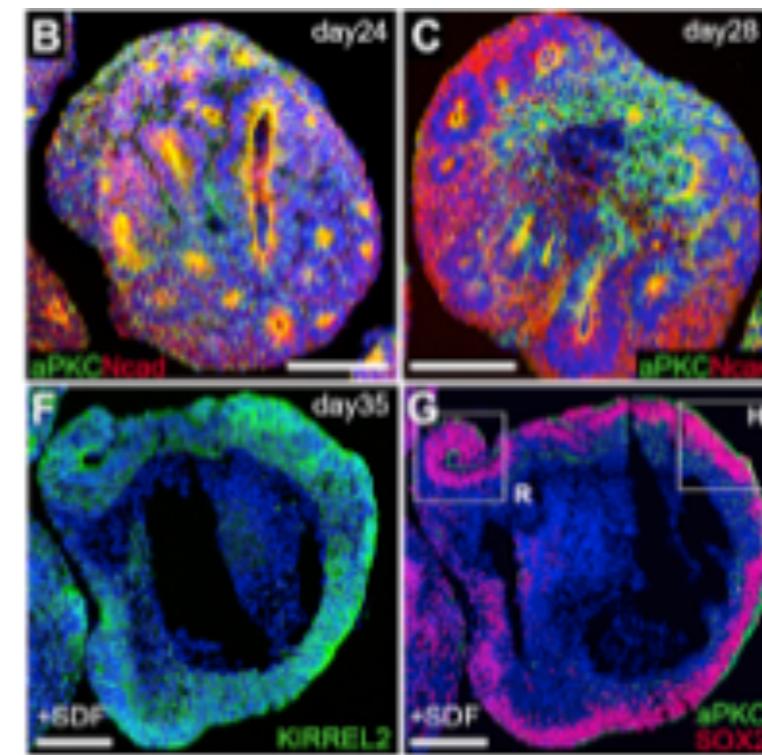
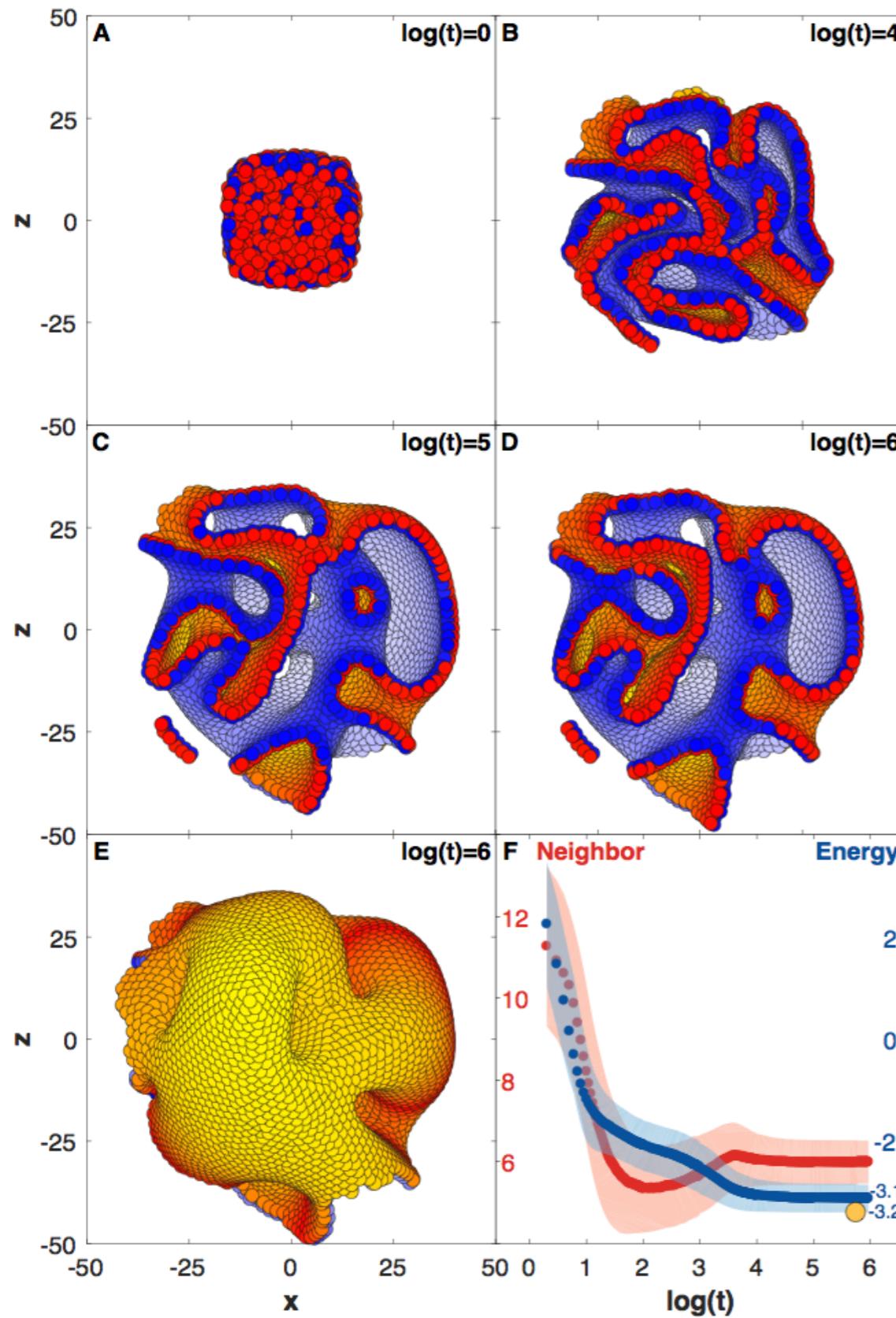


Rotated

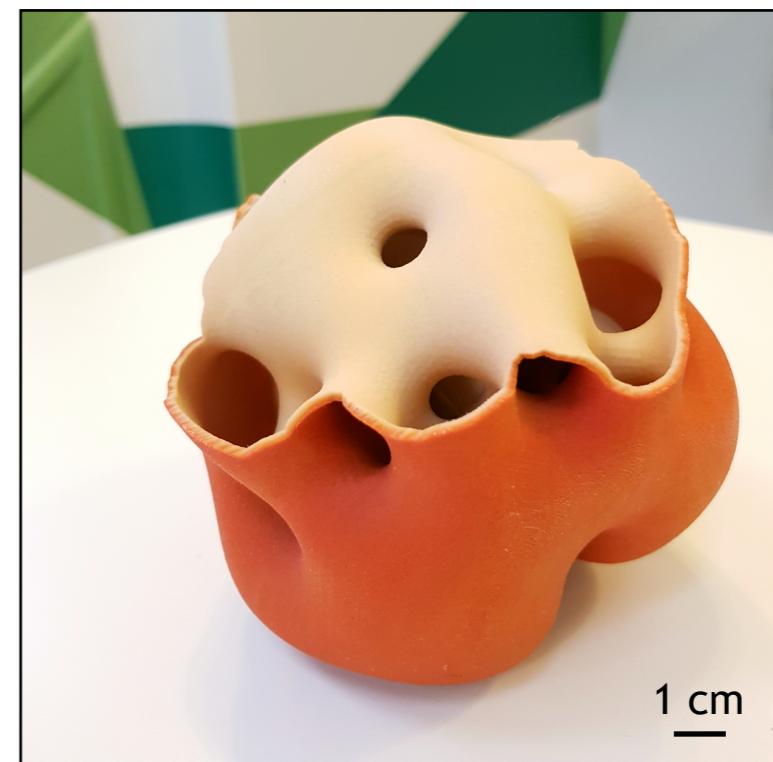


$$\log(t) = 0$$

# Stable complex shapes emerge

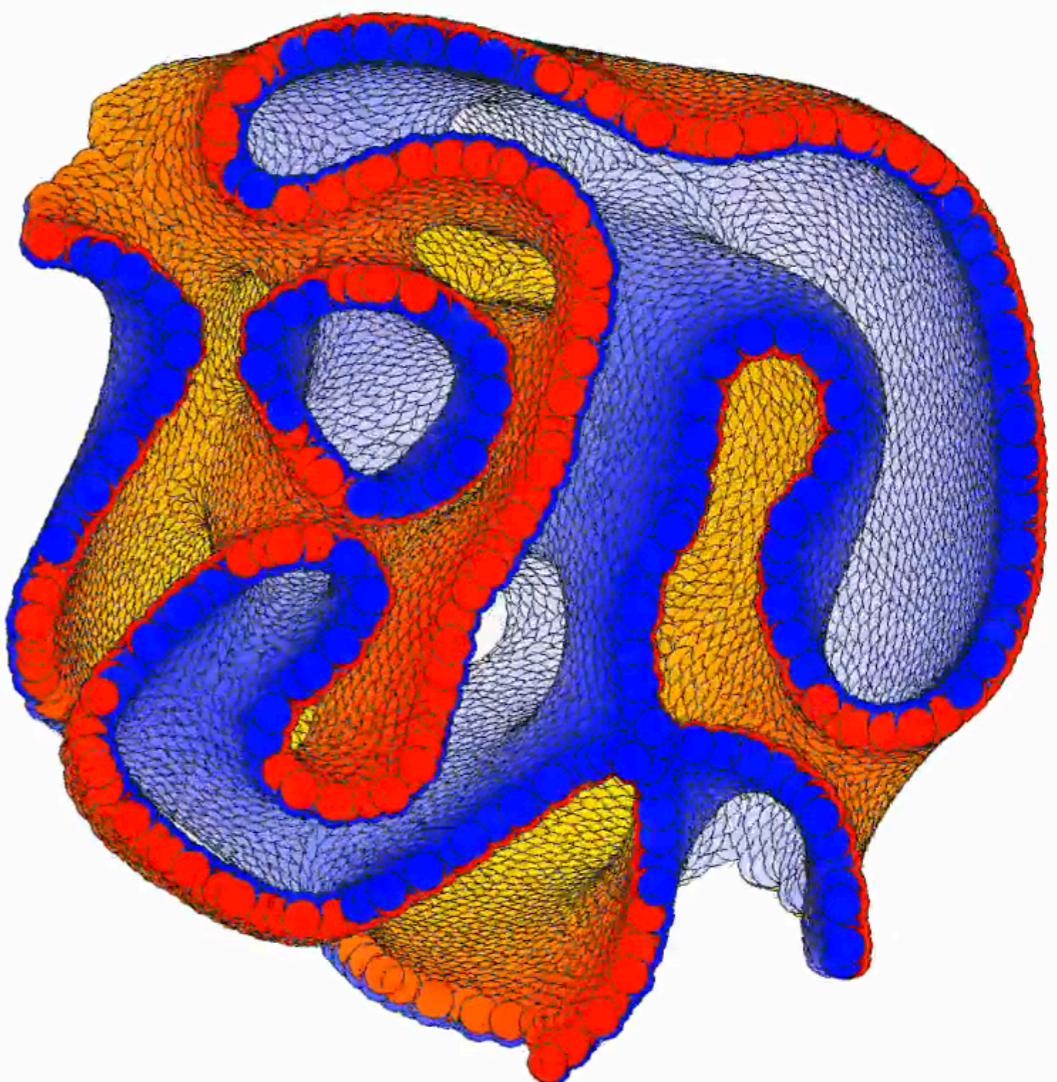
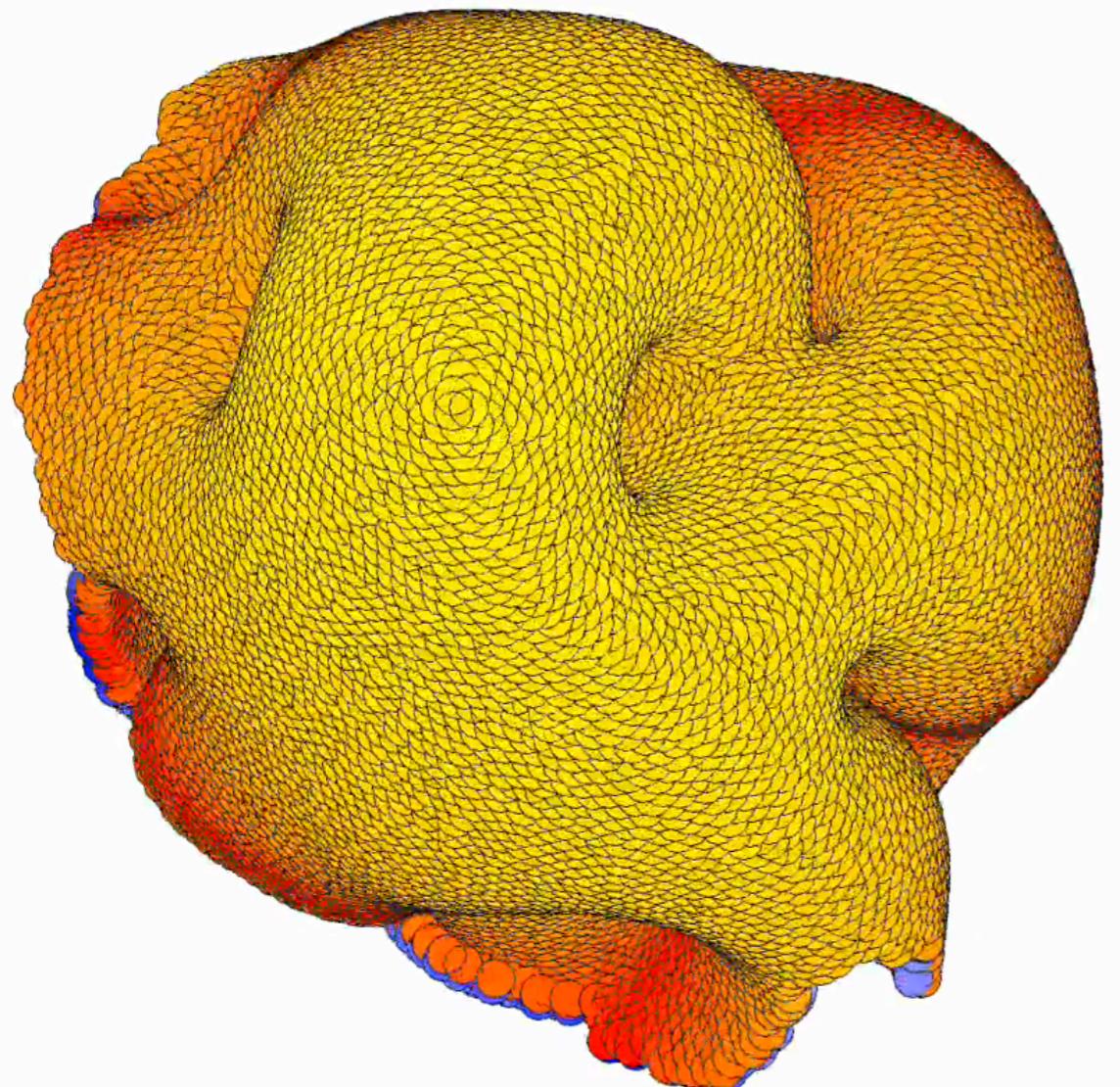


Muguruma et al. (2015)

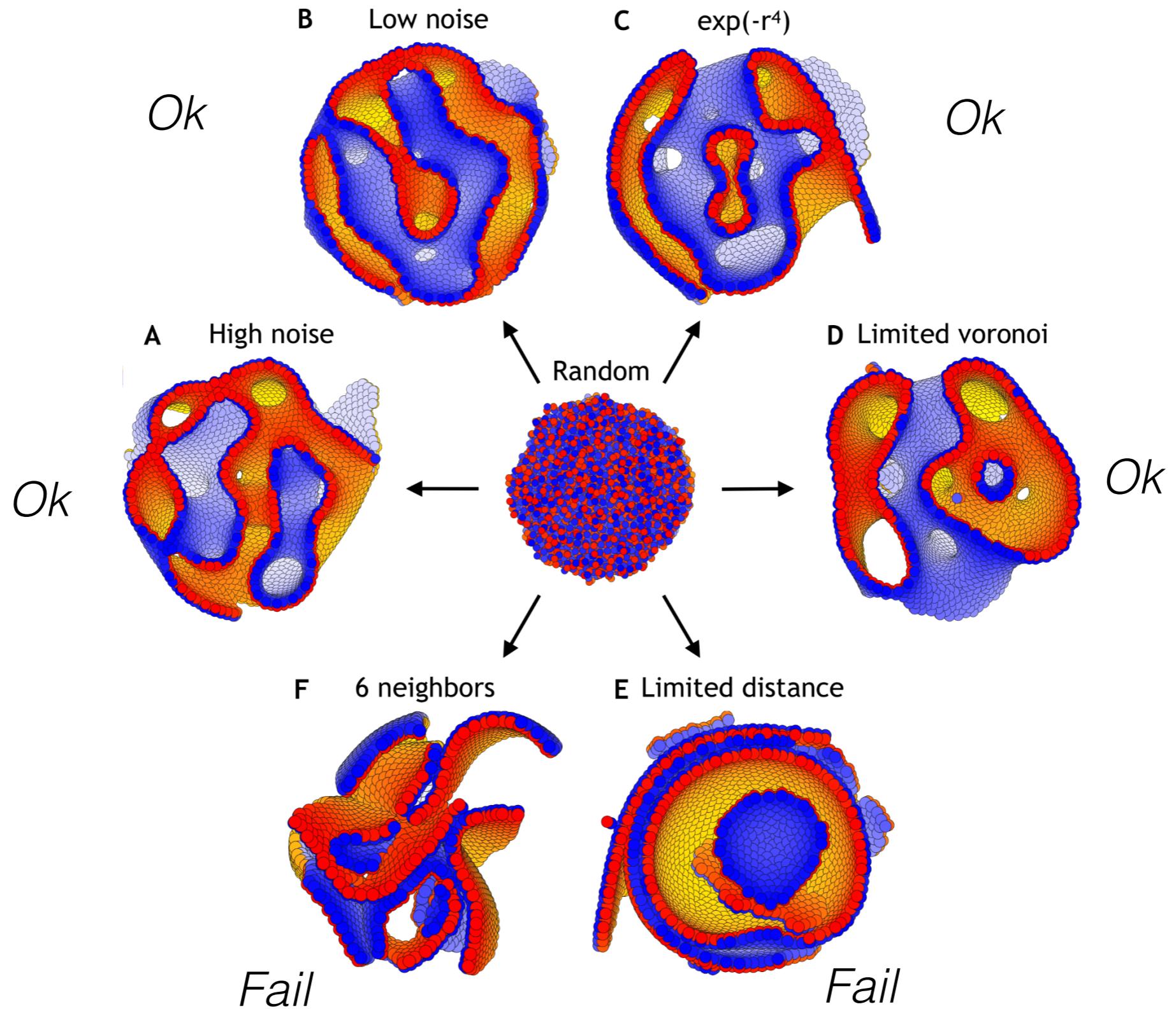


# Robustness: Against growth

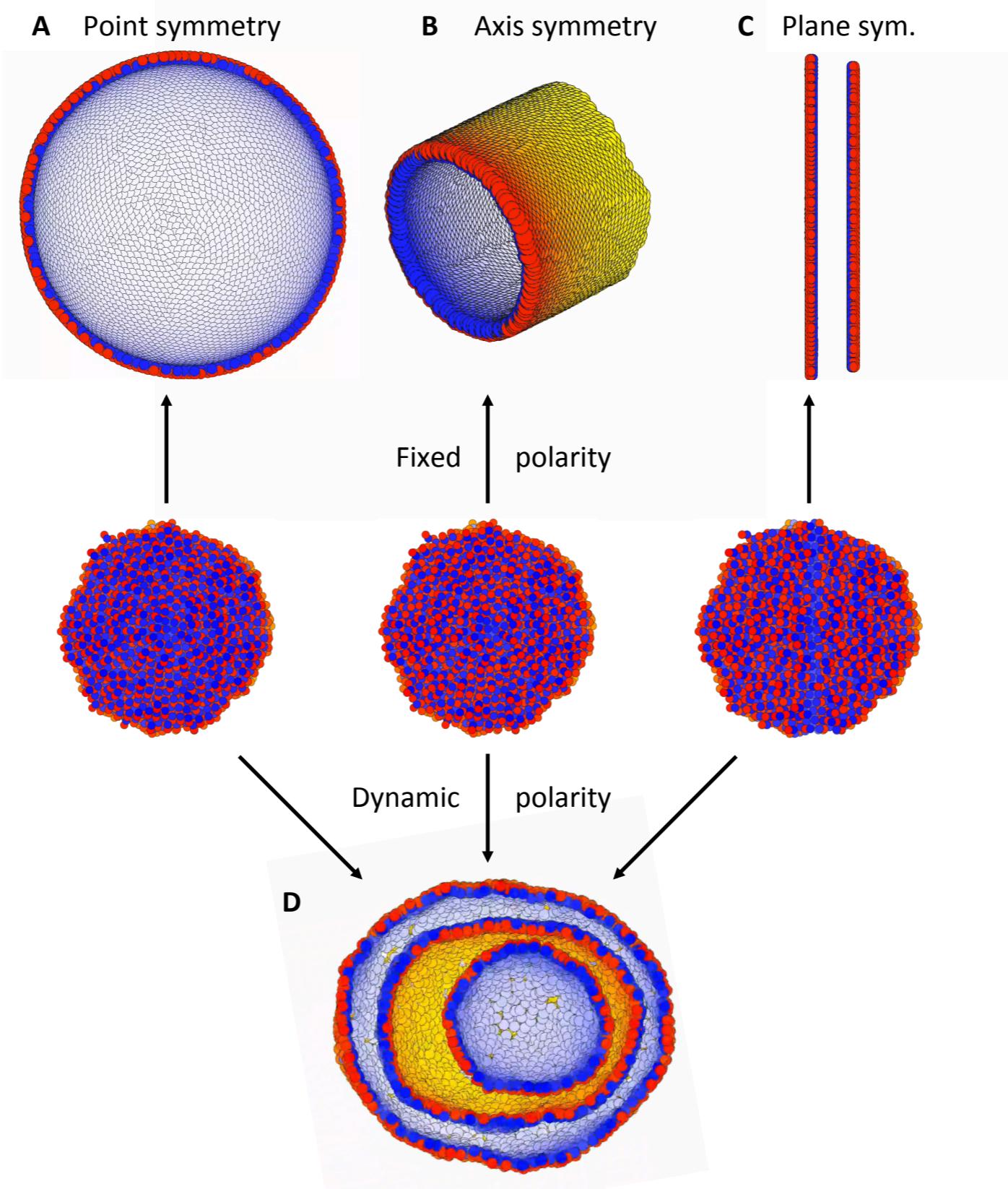
Grow from 8k cells to 25k cells



# Robustness/Variants



# Sensitivity to Boundary Conditions (/constraints):



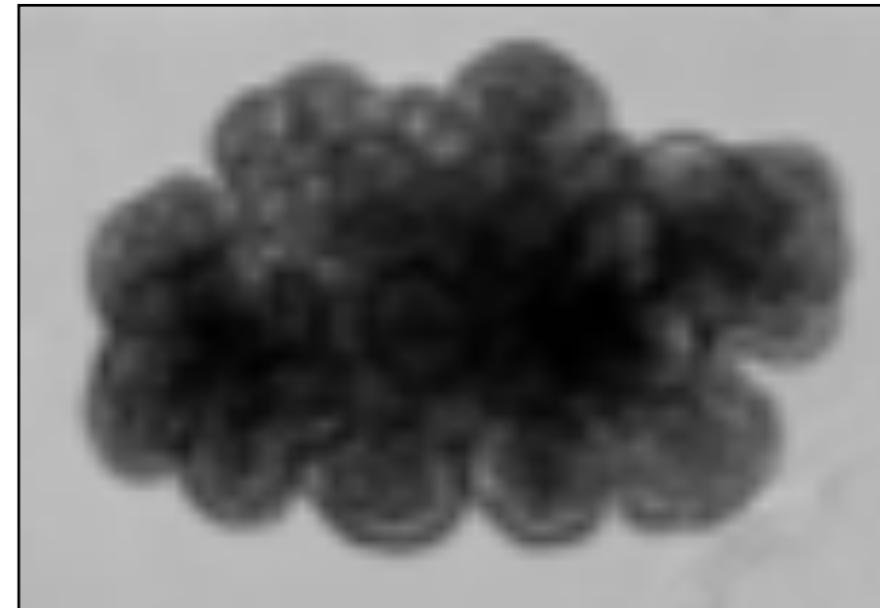
# From spherical to folded organoids

If grown in medium A



all sizes are spherical

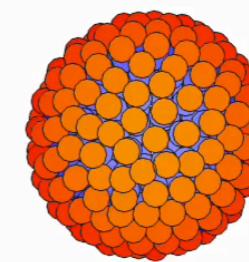
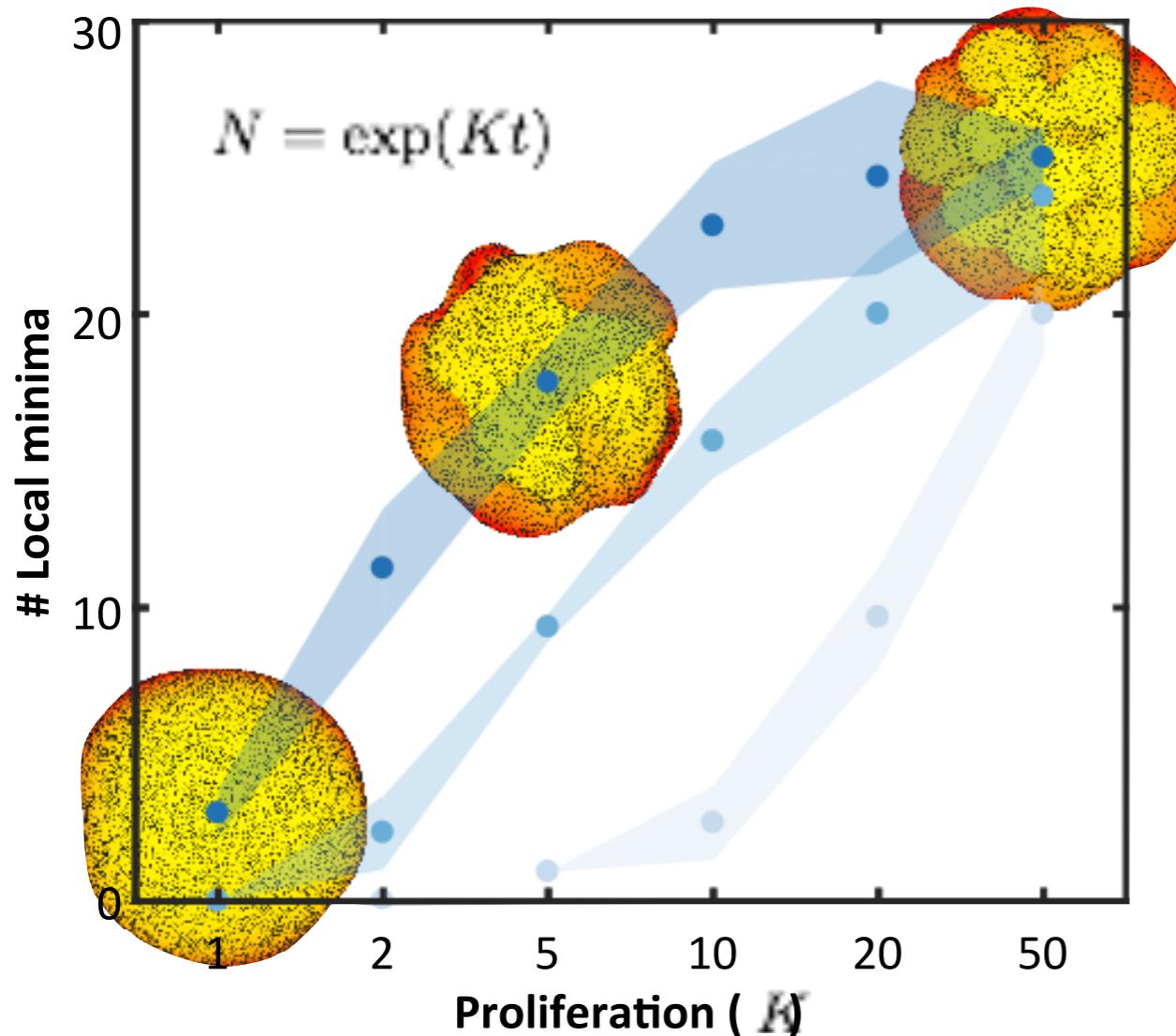
If grown in medium B



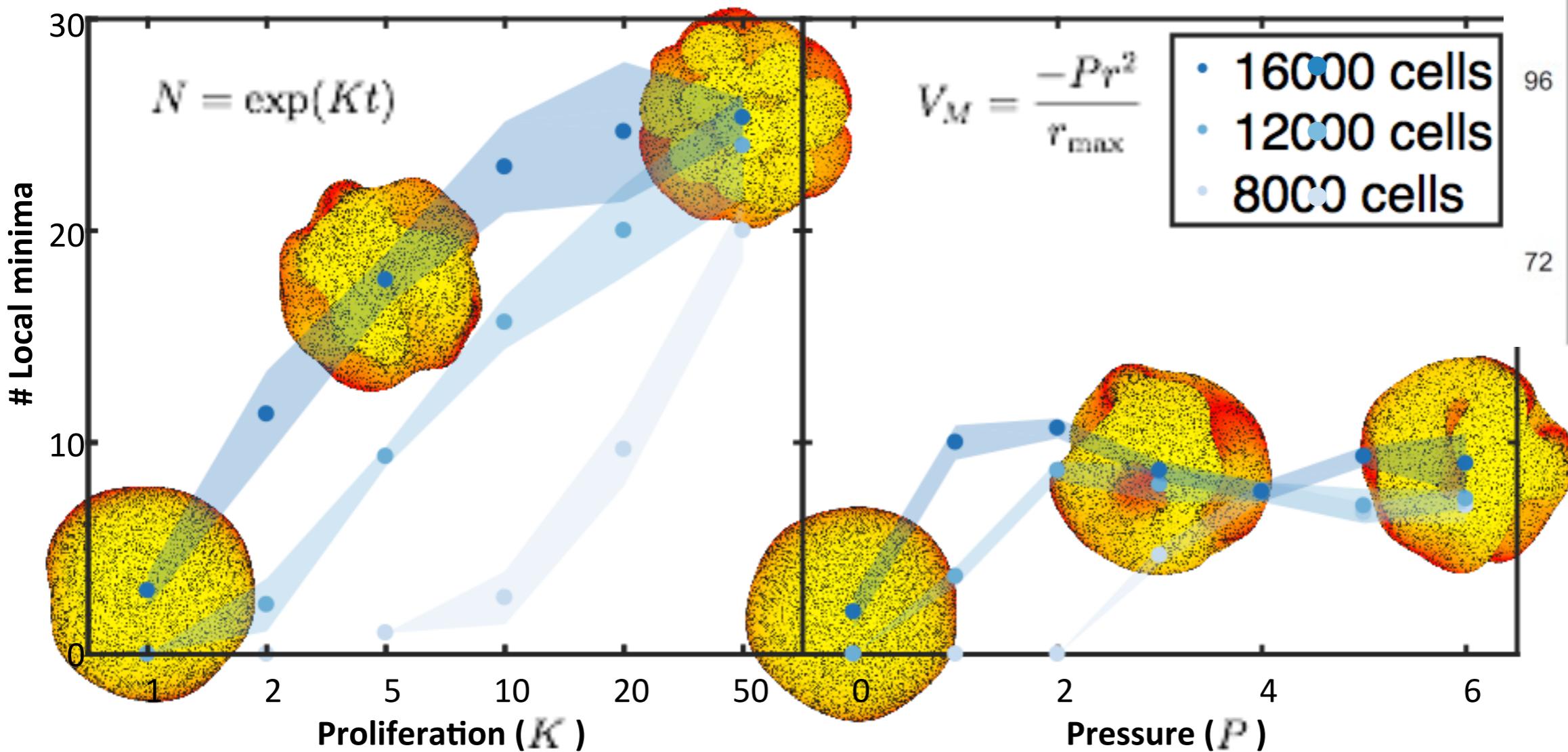
small are spherical  
while large are folded

Greggio et al. (2013) *Development*

# How do folded organoids form?

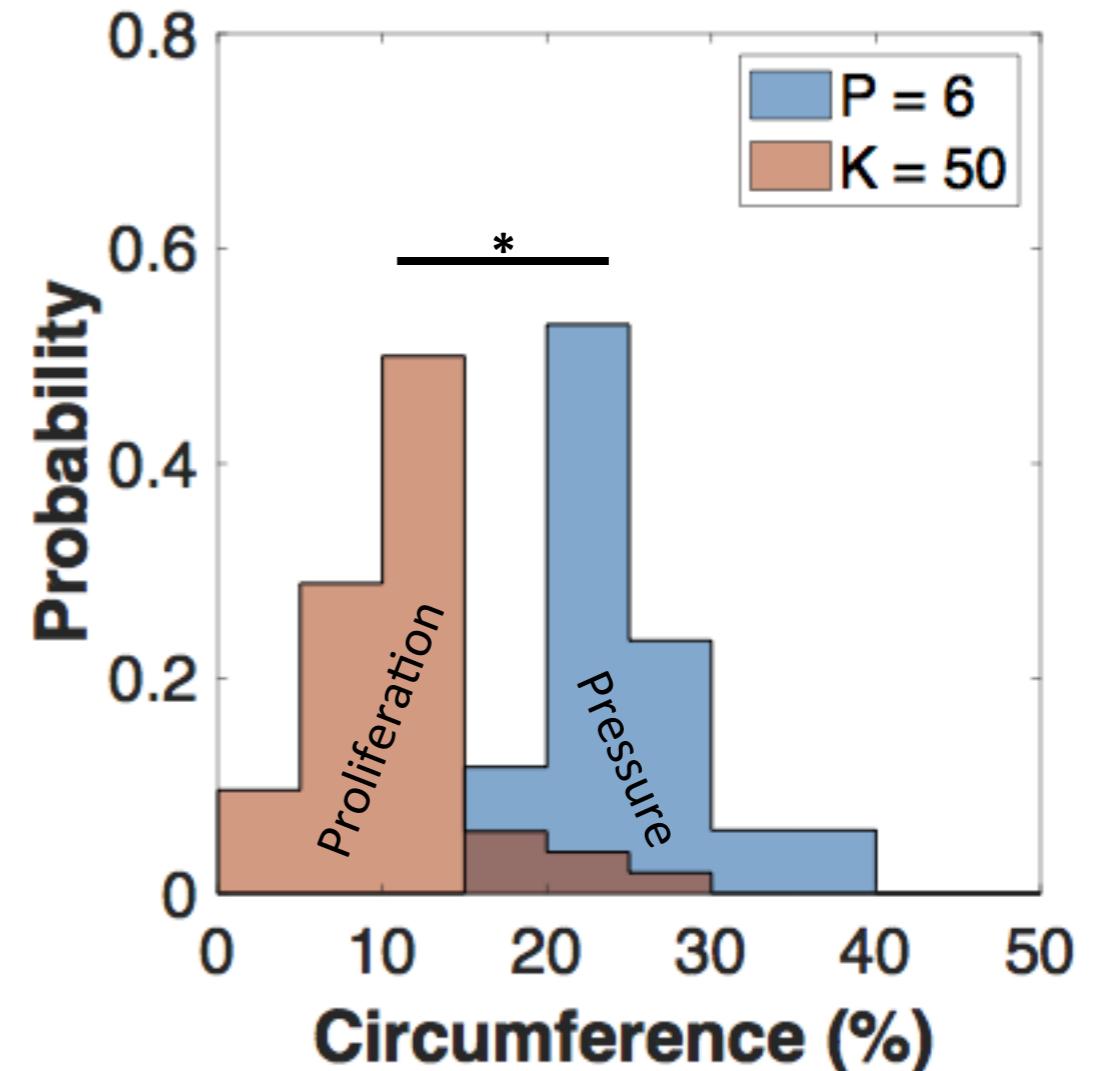
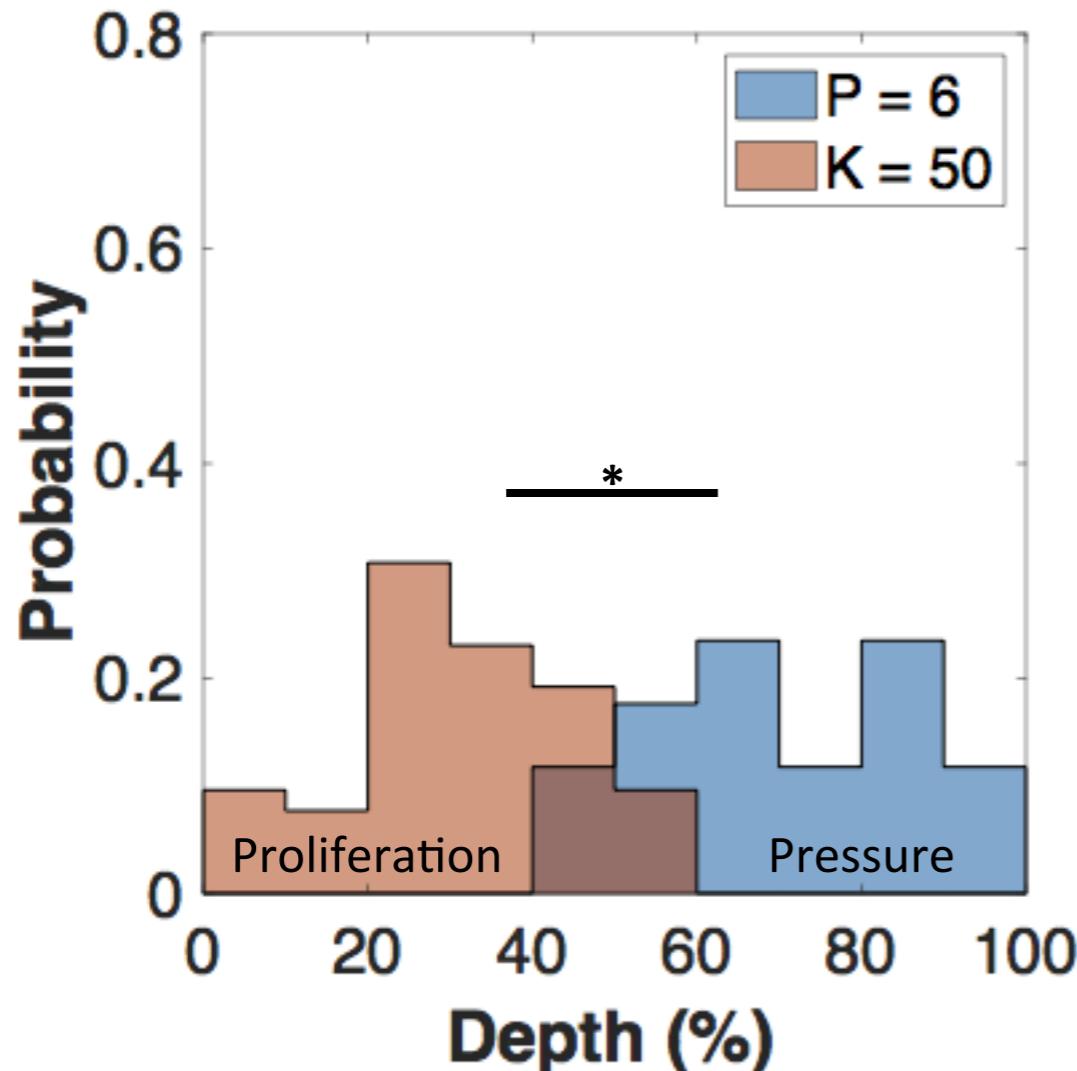


# How do folded organoids form?



Svend Steffensen  
Manuel F.-Larsen  
& Anne Graphin-Bottou  
& Kim Sneppen (2016)

# Different depth and length of folds



**Prediction:** Pressure and proliferation make distinct folds

# Tubulogenesis

**How do tubes with certain width and length form?**

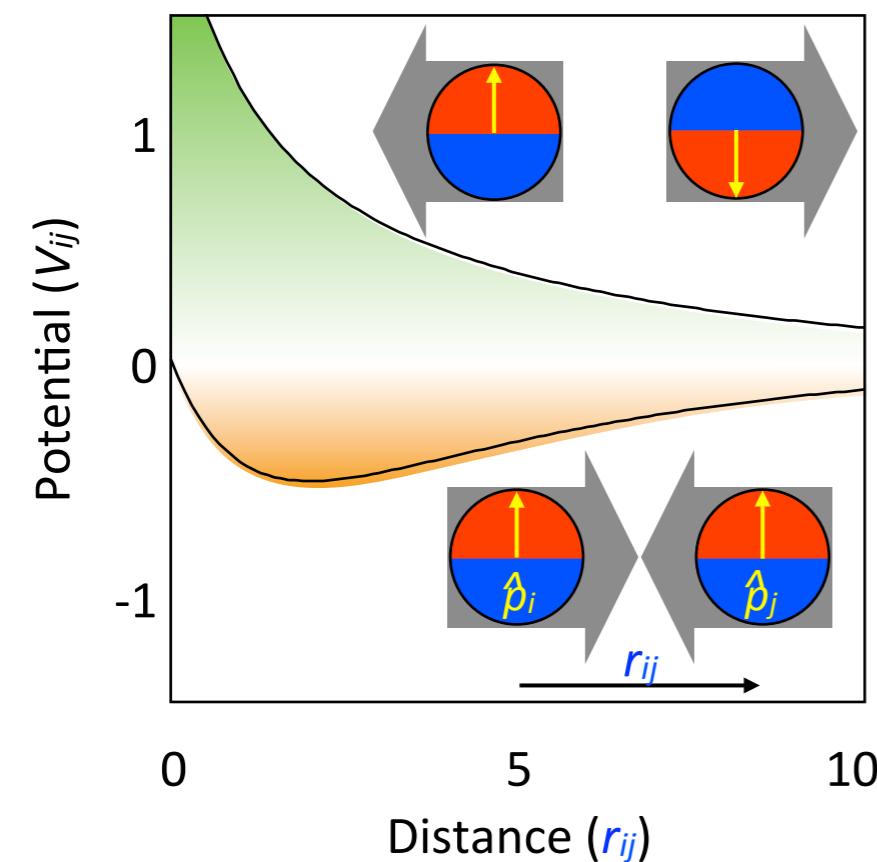
Adding a second polarity, the  
Planar Cell Polarity

AB=skin in/outside  
PCP=hair direction on your skin

## 4) AB+PCP polarity:

Potential between cells

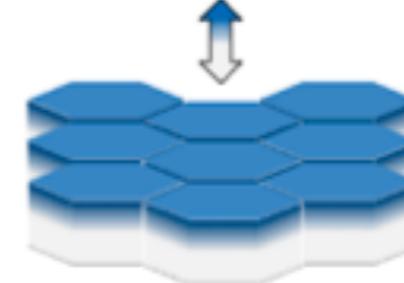
$$V_{ij} = e^{-r_{ij}} - (\lambda_1 S_1 + \lambda_2 S_2 + \lambda_3 S_3) e^{-r_{ij}/\beta}$$



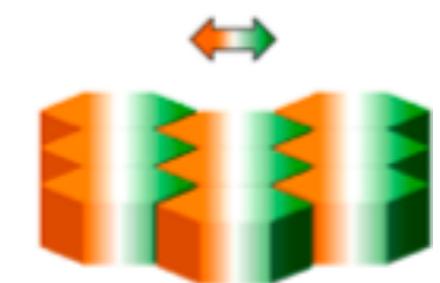
Parameters

$$\lambda_1 + \lambda_2 + \lambda_3 = 1$$

Apical basal  
polarity ( $\hat{p}$ )

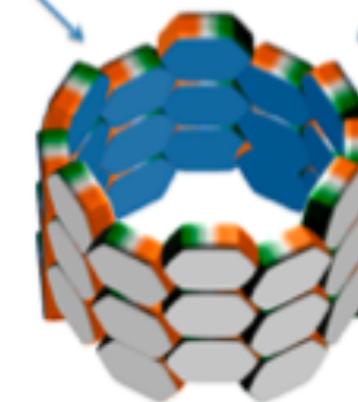


Planar cell  
polarity ( $\hat{q}$ )



Repulsion

Attraction



Epithelial sheet

$$S_1 = (\hat{p}_i \times \hat{r}_{ij}) \cdot (\hat{p}_j \times \hat{r}_{ij})$$

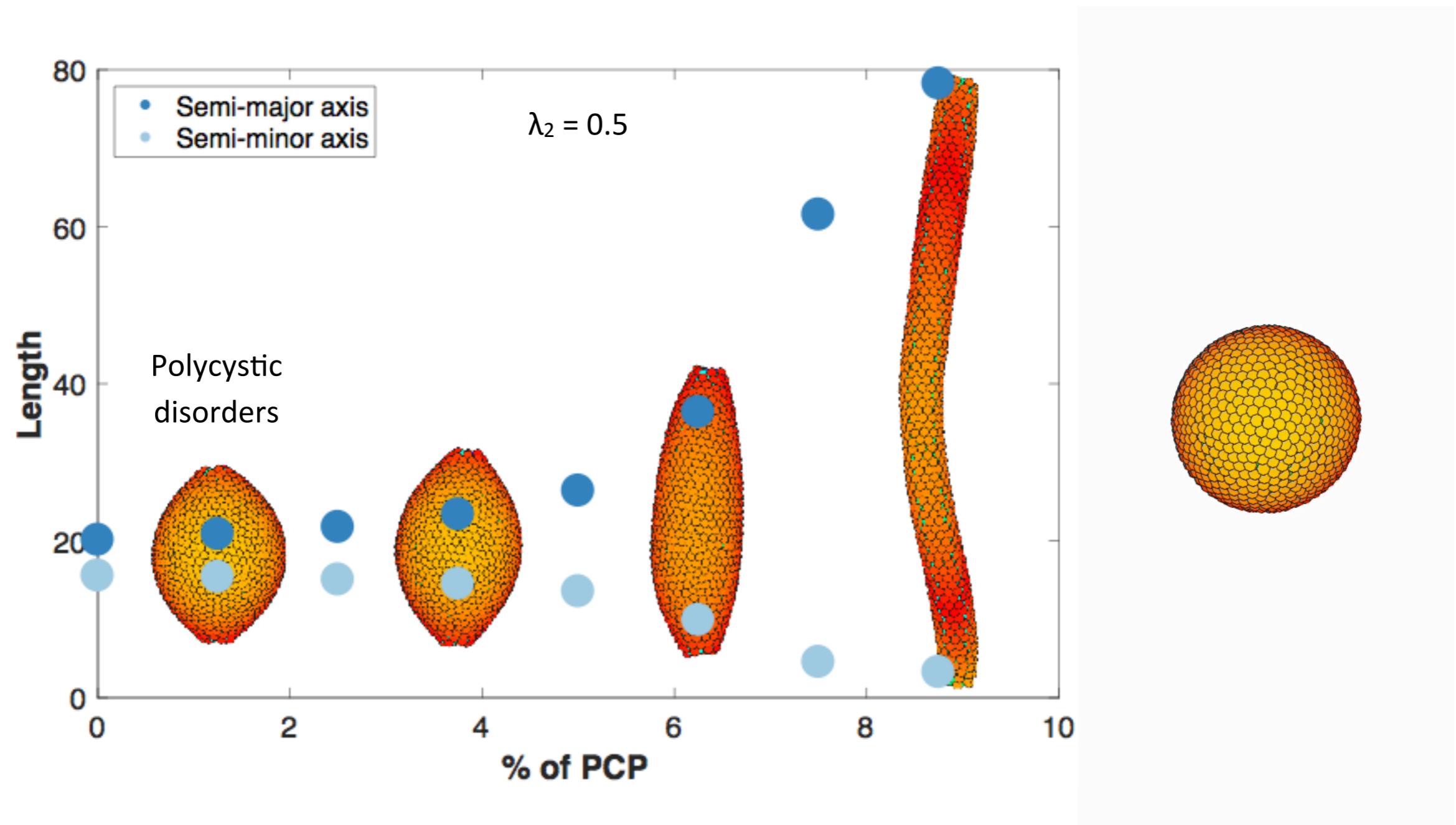
90° between polarities

$$S_2 = (\hat{p}_i \times \hat{q}_i) \cdot (\hat{p}_j \times \hat{q}_j)$$

Convergent extension

$$S_3 = (\hat{q}_i \times \hat{r}_{ij}) \cdot (\hat{q}_j \times \hat{r}_{ij})$$

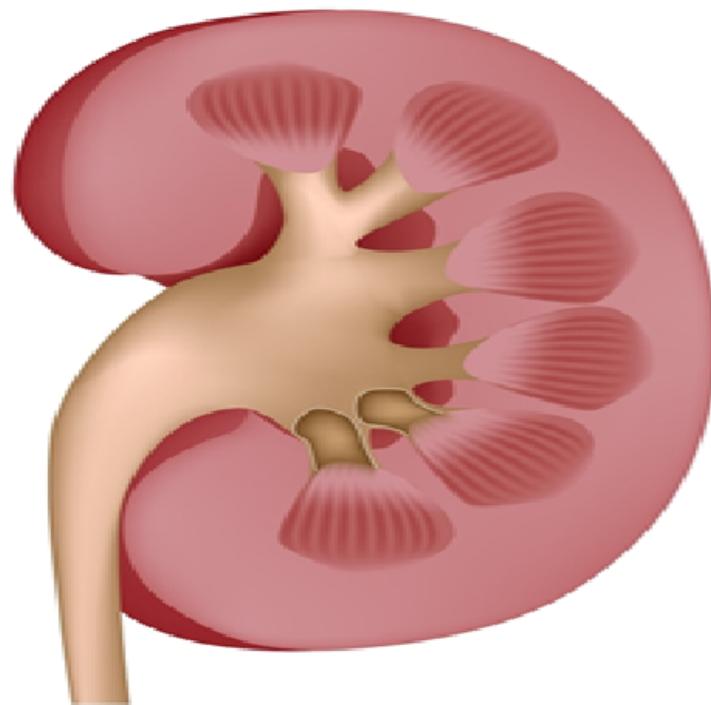
## 4a) How do tubes form:



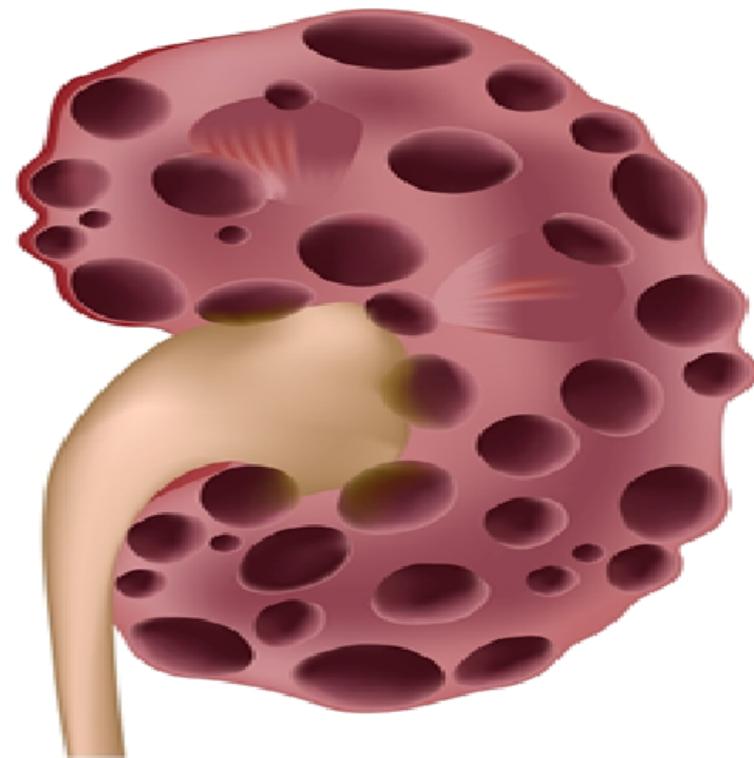
**Prediction:** Strength of AB vs. PCP controls length and width

# Polycystic Kidney Disease

Normal kidney



Diseased kidney



Absence of PCP,  
less tubes,  
Instead spherical holes

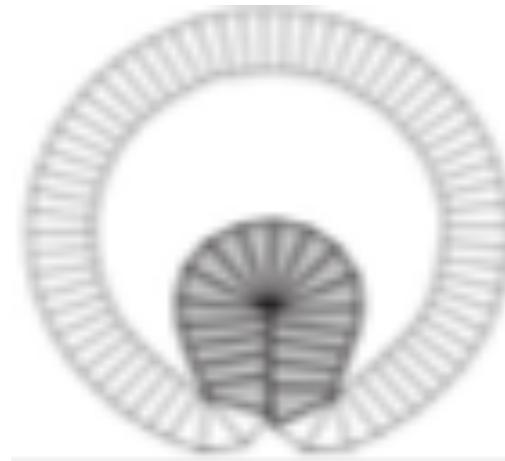


# Invagination

**What drives invagination across species?**

# Vertex models

Gastrulation



Brezavscek et al. (2012)

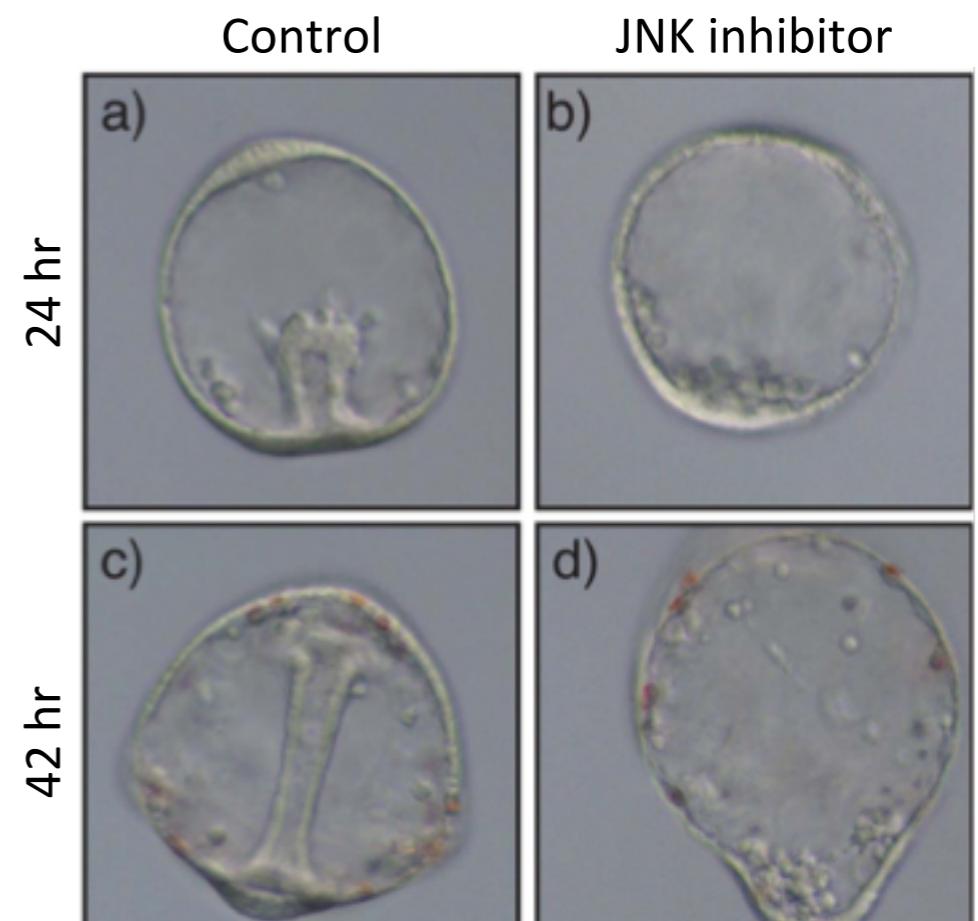
Neural tube formation



Alt et al. (2017)



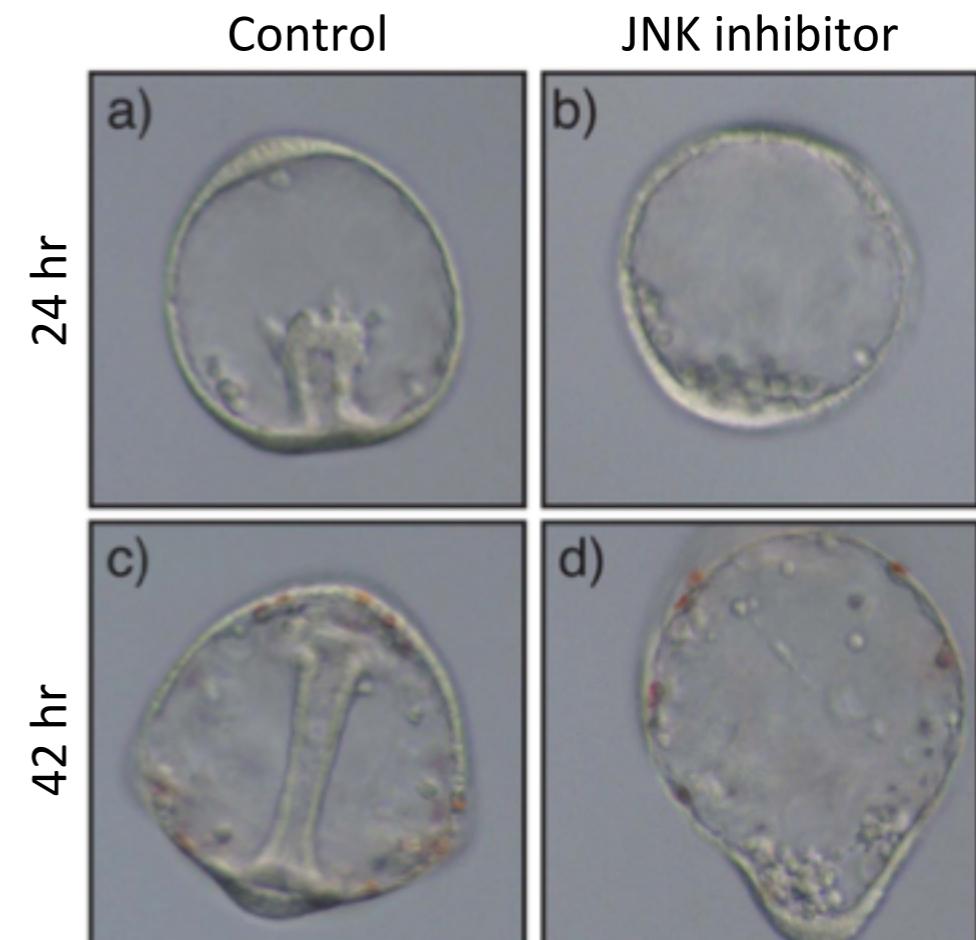
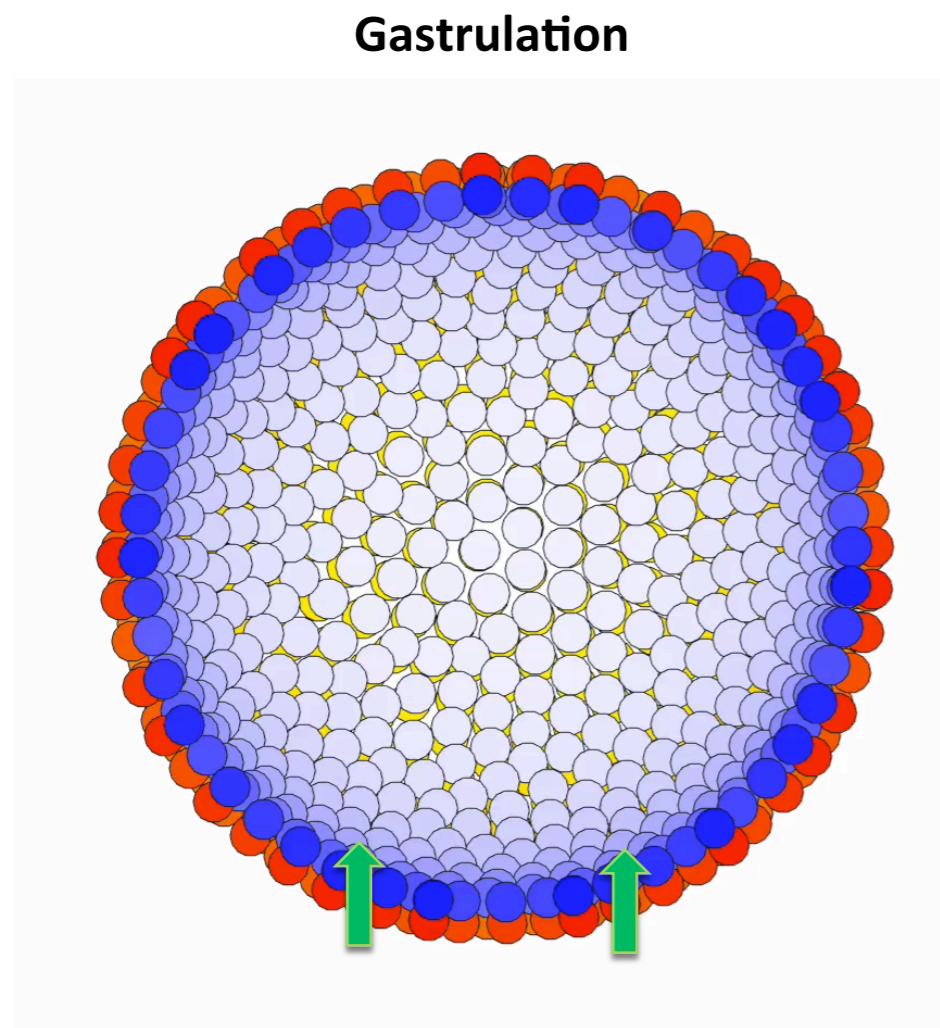
# What drives invagination?



Long et al. (2015)



# What drives invagination?

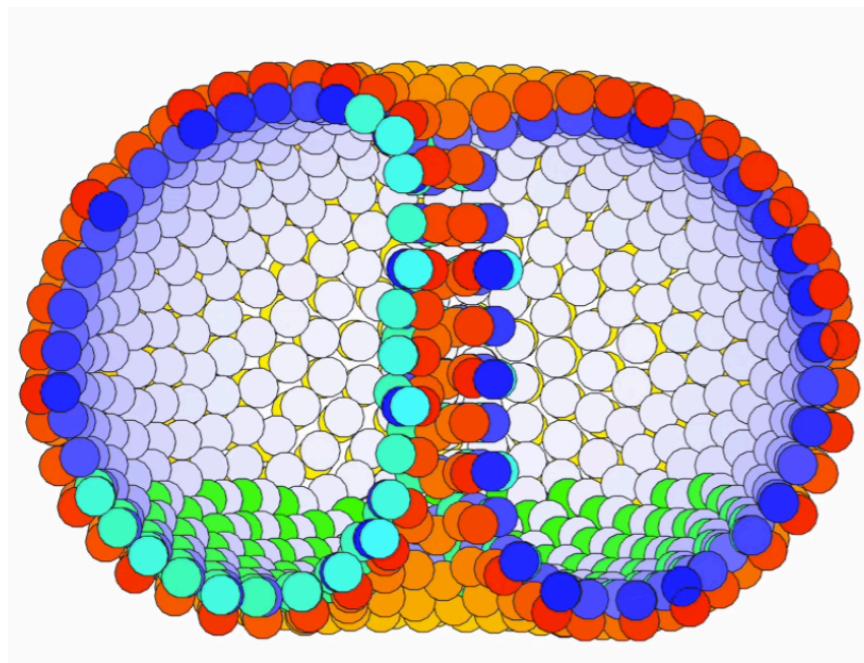


Long et al. (2015)

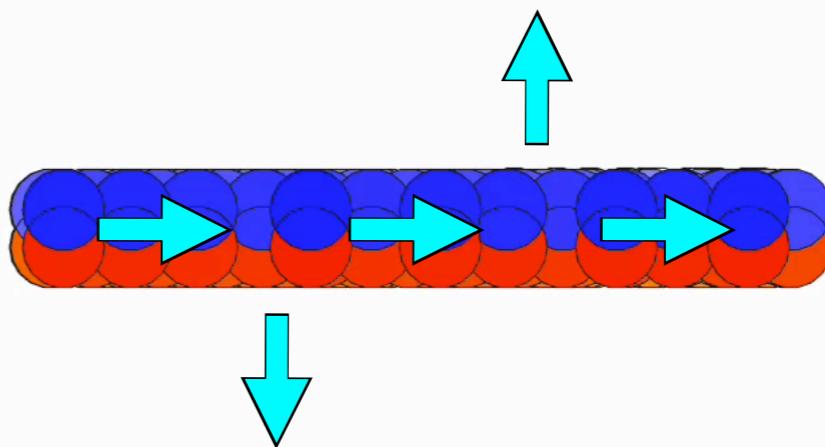


# What drives invagination?

Gastrulation



Neurulation



**Prediction:** Different initial conditions give different types of invagination

# Conclusion

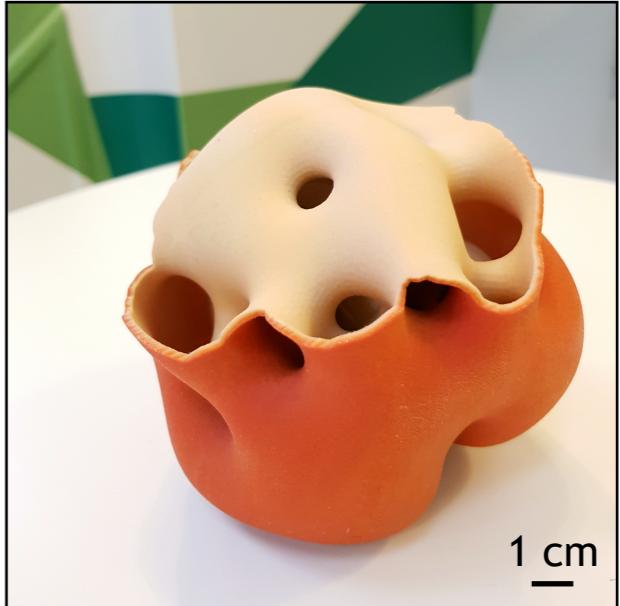


Take home messages

# Conclusion



1. Tool to model impact of cell polarities
2. Complex diverse stable shapes
3. Distinct organoid fold morphology
4. Tube length and width given by PCP
5. PCP drives gastrulation and neurulation



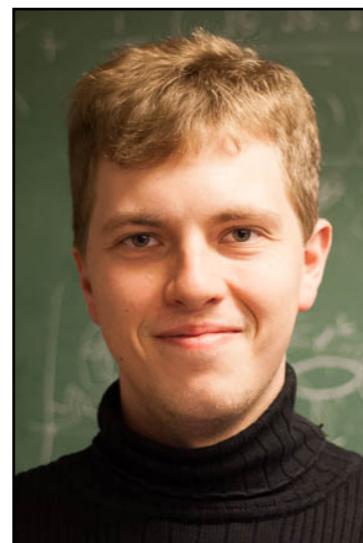
# Collaborators:



Silas Boye Nissen  
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Steven Rønhild  
NBI

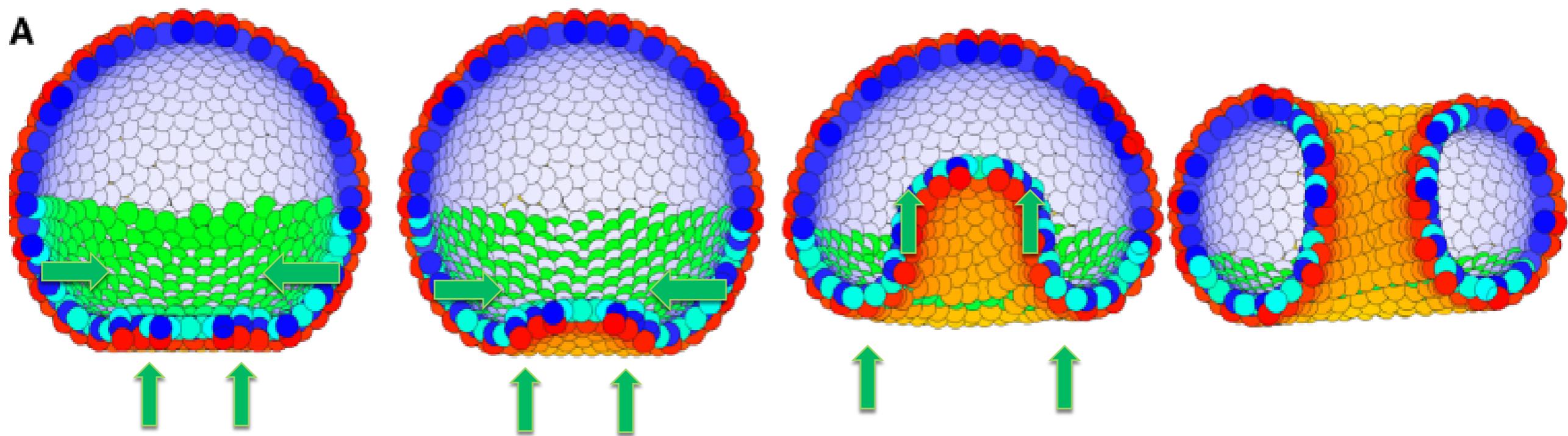


Sophie M. Morgani  
DanStem



Joshua M. Brickman  
DanStem

# (Sea-Urchin) Gastrulation



PCP is sufficient for neural plate bending and neural tube closure



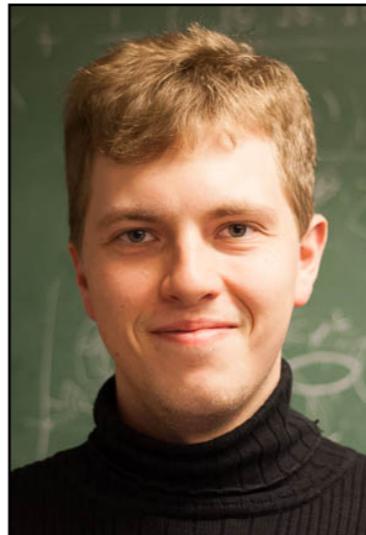
# Coauthors



Mogens H. Jensen  
Niels Bohr Inst.



Silas Boye Nissen  
NBI



Steven Rønhild  
Niels Bohr Inst.



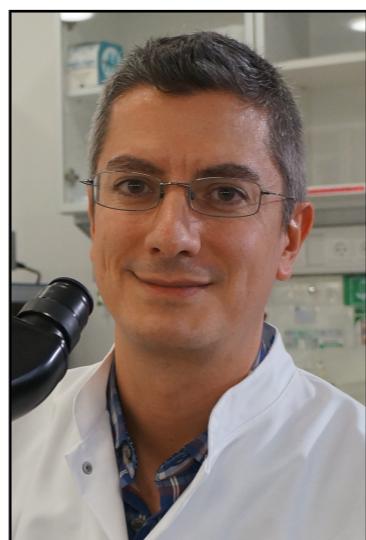
Ala Trusina  
Niels Bohr Inst.



Marta Perera  
DanStem



Sophie M. Morgani  
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Javier M. Gonzalez  
DanStem



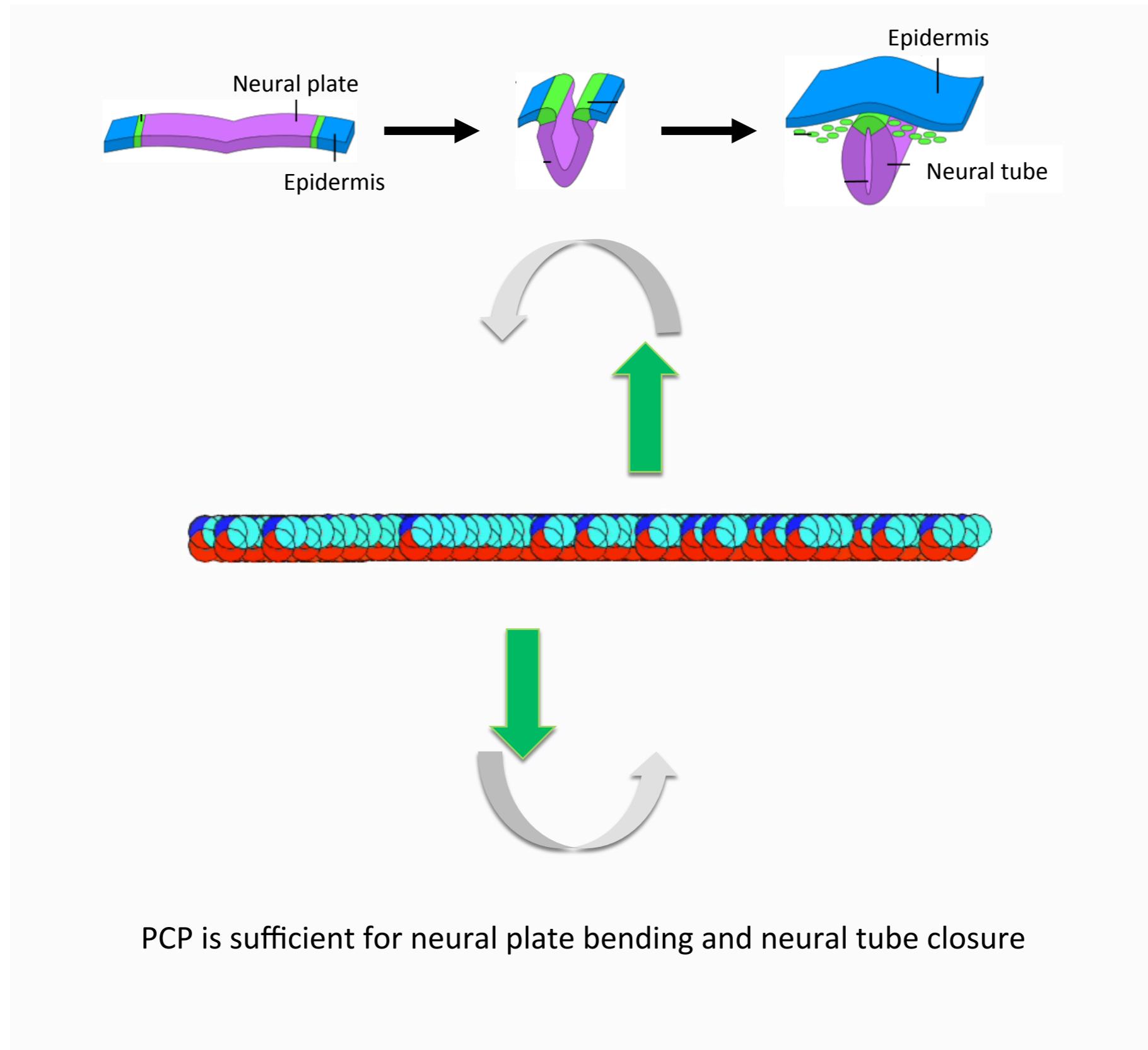
Joshua M. Brickman  
DanStem



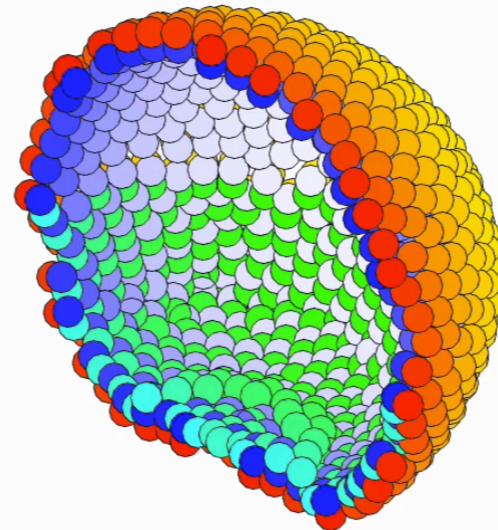
Danmarks  
Grundforskningsfond  
Danish National  
Research Foundation



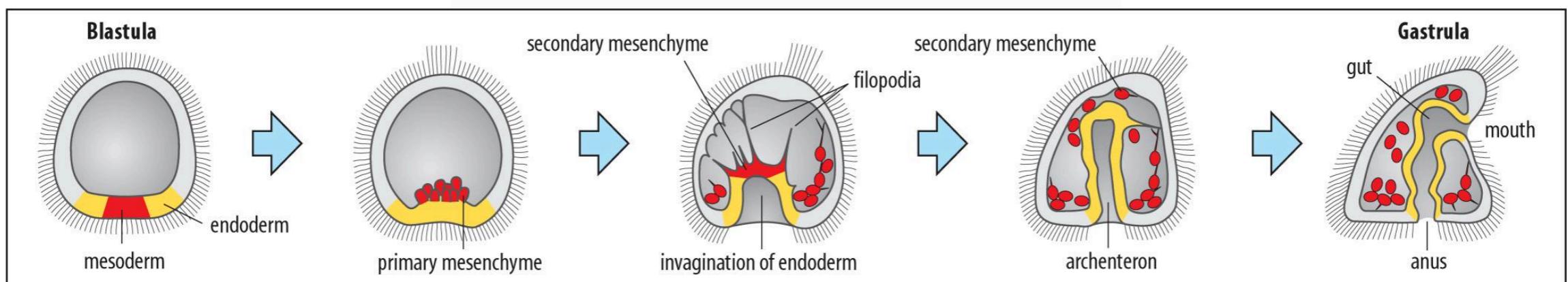
## 4b) Neural tube formation



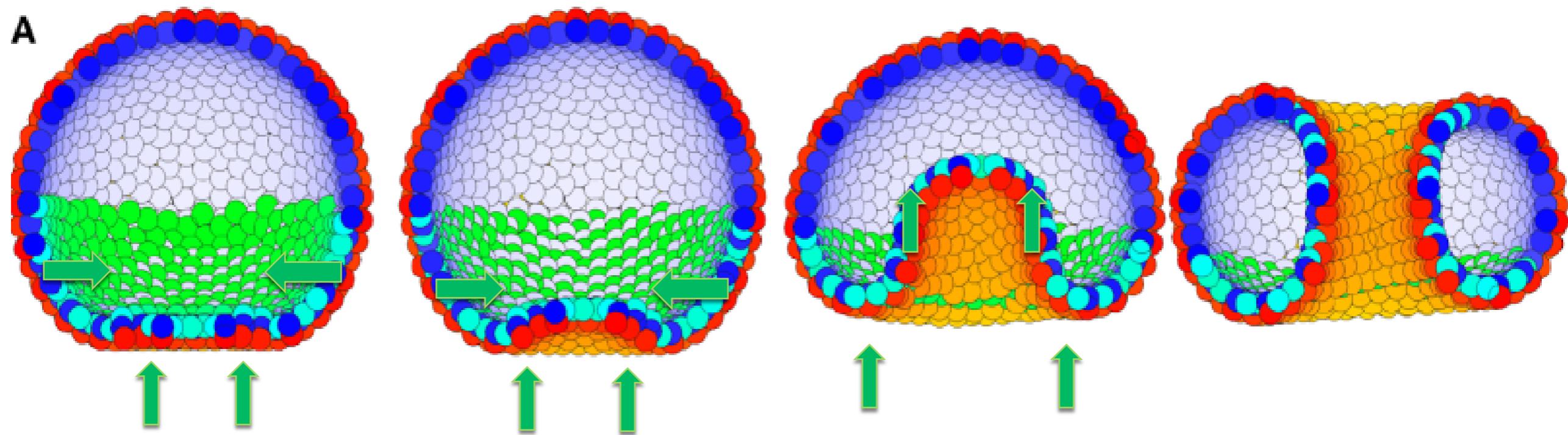
## 4c) Gastrulation in Sea Urchin



PCP is sufficient to initiate invagination and drive elongation



# (Sea-Urchin) Gastrulation



PCP is sufficient for neural plate bending and neural tube closure

# Acknowledgments



Silas Boye Nissen  
NBI



Ala Trusina  
NBI



Steven Rønhild  
NBI

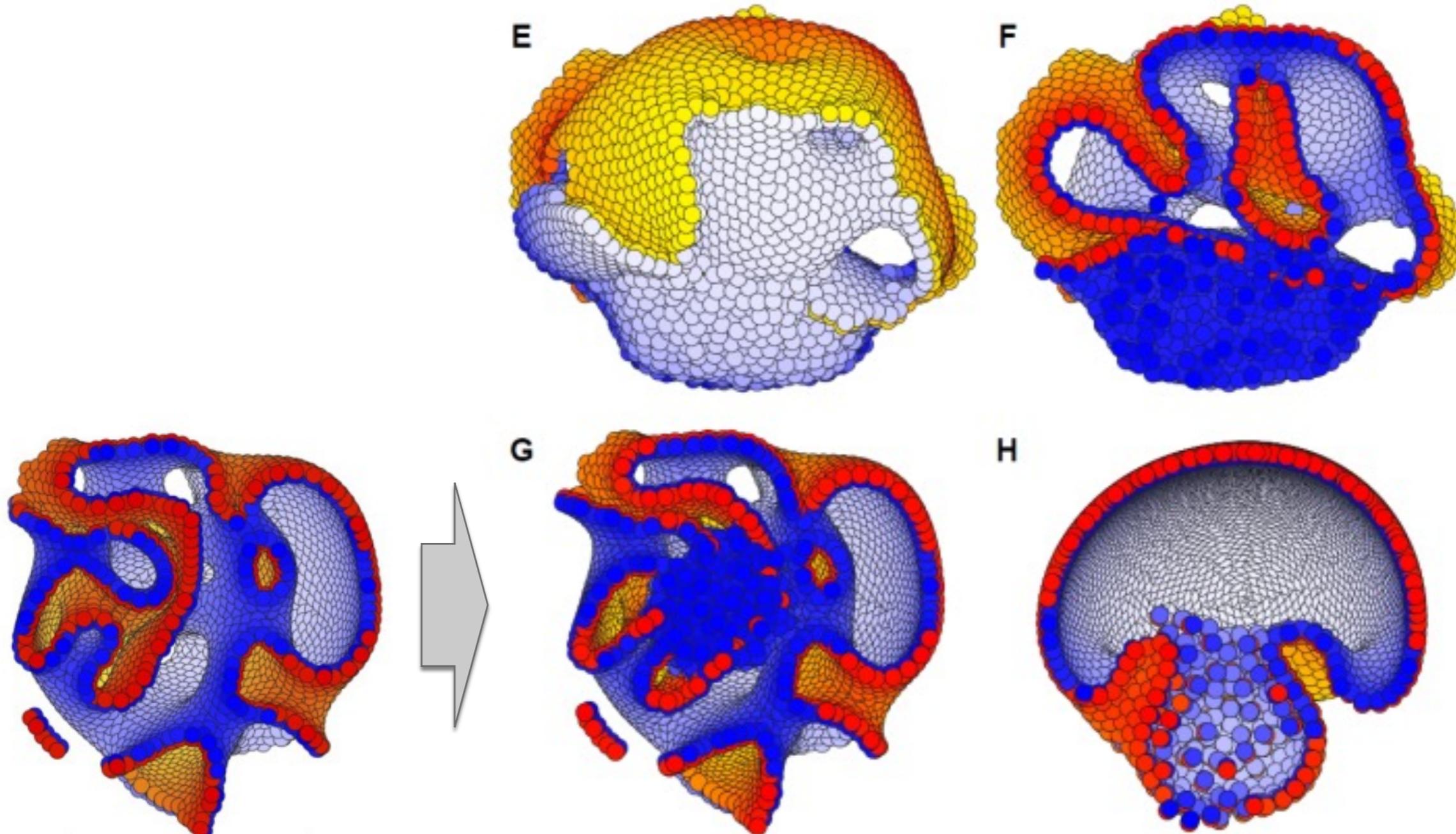


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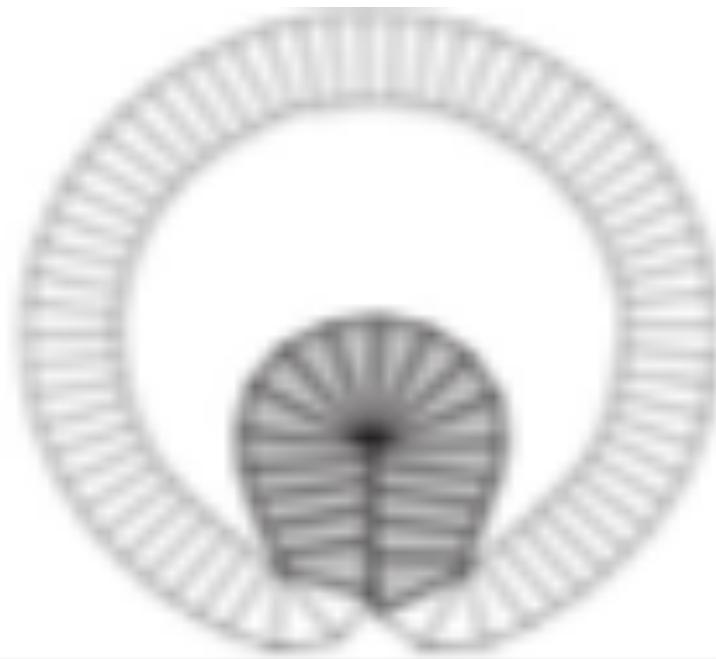
Joshua M. Brickman  
DanStem

## 5) Note: Tumor = loss of polarity



# Vertex models

## Gastrulation



Brezavscek et al. (2012),  
buckling from favoring free cell  
surface against interacting cells.  
(2d model, each cell a deformed  
square)

## Neural tube formation

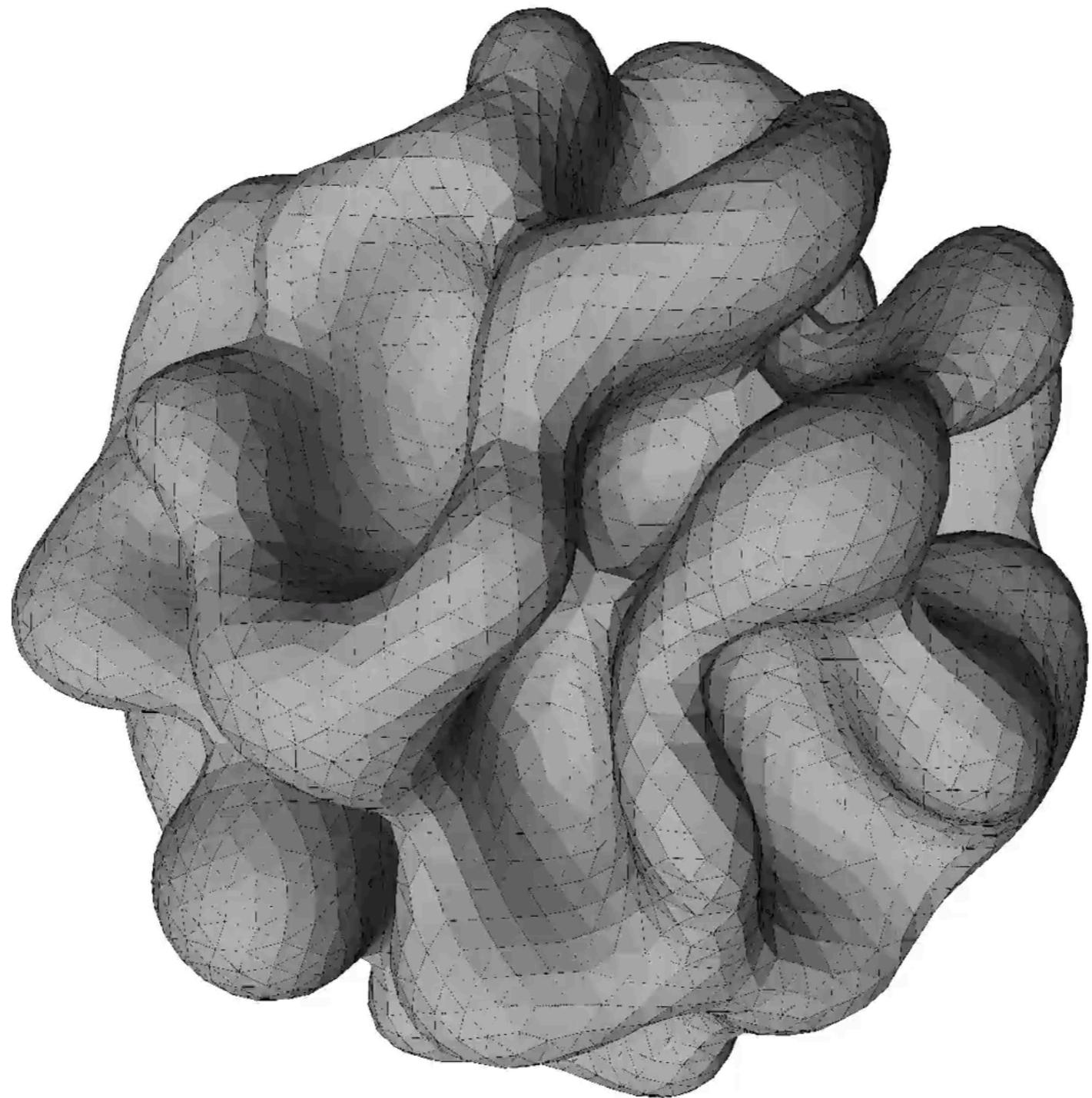


Alt et al. (2017), Monier et al. (2015)  
vertex models: assign a value to polygon cell  
edges representing the density of planar  
polarity proteins. Monier use apoptosis to  
drive above formation

Next step...:



# Online STL viewer

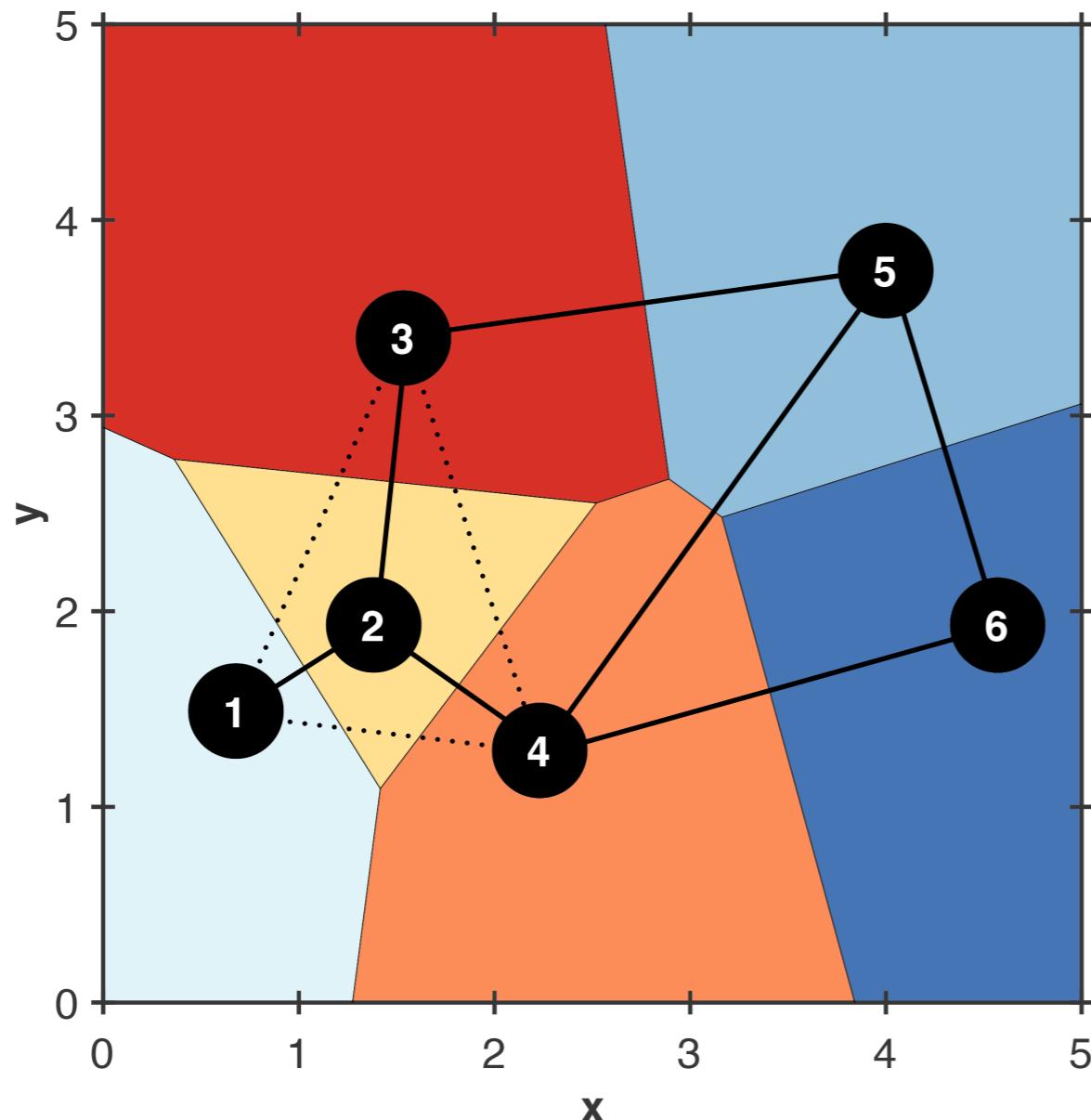


<https://www.viewstl.com/>



# Interacting neighbors

Who interact?



Solid lines do, dashed do not

$$V_i = \sum_j V_{ij}$$

$$\frac{d\vec{r}_i}{dt} = -\frac{dV_i}{d\vec{r}_i} + \eta$$

$$\frac{d\vec{p}_i}{dt} = -\frac{dV_i}{d\vec{p}_i} + \eta$$

$$\frac{d\vec{q}_i}{dt} = -\frac{dV_i}{d\vec{q}_i} + \eta$$